# Cybersecurity (in Critical Systems)

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## Course organization

Office hours:
 Mondays, 15:15-17:00

Practicals:

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## Course organization

## Objectives:

- 1. Present software development standards in the European space industry and techniques of their implementation.
- 2. Learn how to assess and manage critical system software quality in an IT project.
- 3. Gain basic hands-on experience in bug tracking and reporting in a software project.

## Literature

- IEEE Software and Systems Engineering Standards, <u>http://standards.ieee.org/findstds/standard/software</u>
   <u>and systems engineering.html</u>
- Space engineering Software, ECSS-E-ST-40C, 6
   March 2009, European Cooperation for Space Standardization, ESA-ESTEC,
  - http://ecss.nl/standards/ecss-standards-online/active-standards
- Space product assurance Software product assurance, ECSS-Q-ST-80C Rev.1, 15 February 2017, European Cooperation for Space Standardization, ESA-ESTEC,
  - http://ecss.nl/standards/ecss-standards-online/active-standards

# Grading

#	hrs	%	Content
L1	18	30	Definition of tests for selected attributes
L2	915	30	Test execution and reporting
Т	115	40	All weeks (lecture part)
	=	100	towards the final score

## Pass/fail criteria

- 1. Total score of 50% minimum
- 2. Attending the final test (any non-zero score accepted)
- 3. All assignments must be submitted in the due time. No late assignments accepted, except of a valid medical excuse.

# Different types of cybersecurity

#### 1. Network security

Identification and blocking of attacks on data and infrastructure

#### 2. Cloud (platform) security

 Policies and services to protect an organization's entire cloud deployment (applications, data, infrastructure, etc.) against attack

#### 3. Endpoint Security

 Creating micro-segments around data wherever it may be (end-user devices, anti-phishing, anti-ransomware, anti-virus,...)

#### 4. Mobile security

Mobile devices accessing corporate/organization assets

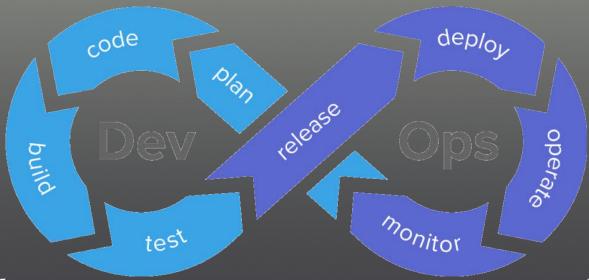
#### 5. IoT Security

Takeover of the end device

# Different types of cybersecurity

#### 6. (Software) application security

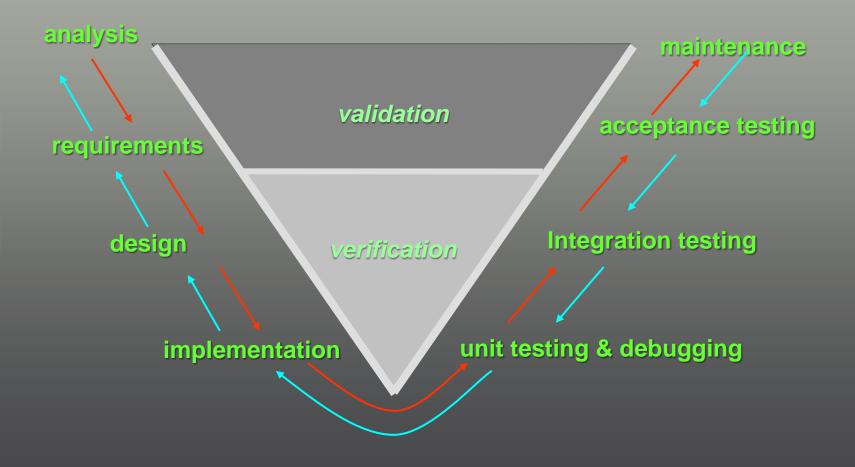
- Interaction with applications and APIs (people, insider and outsider threats)
- Development proces (policies, standards)
- Implementation technology (qualification, validation)
- Testing & monitoring (DevOps)



- A. Product life-cycle vs. its testing cycle
- B. VVT processes
- C. Planning of VVT processes
- D. Static analysis techniques
- E. Error, program and run-time environment models
- F. Black-box (functional) testing
- G. White-box (structural) testing

# A. Product life-cycle vs. its testing cycle

## Model "V"



## Objectives

#### Validation

Assess whether the system (or its component) meets its requirements specification

 $\rightarrow$  Are we building the right product?

## Objectives

### Verification

Assess whether the product of a given phase meets the assumptions made at the beginning of this phase

 $\rightarrow$  Are we building the product right?

## Objectives

## Testing

Analysis of the system behavior (or its component) in order to measure (assess) its quality

 $\rightarrow$  How good is (or will be) the system?

## Object:

 $\rightarrow$  A library routine for sorting matrices

## Object:

-Testing

→ A library routine for sorting matrices

 $\rightarrow$  Does the object return a sorted matrix?

Object:

→ A library routine for sorting matrices

-Testing

- → Does the object return a sorted matrix?
- -Verification

→ Does the object sort matrices?

## Object:

 $\rightarrow$  A library routine for sorting matrices

-Testing

- $\rightarrow$  Does the object return a sorted matrix?
- -Verification

→ Does the object sort matrices?

- -Validation
  - → Can the procedure be included in the existing system library?

run-time environment models

run-time environment models

program models

run-time environment models

program models

error models

instrumentation

run-time environment models

program models

error models

instrumentationtest casesrun-time environment modelsprogram modelserror models

instrumentation
test cases

run-time environment models
program error models

bugs

test scenarios

instrumentation

run-time environment models

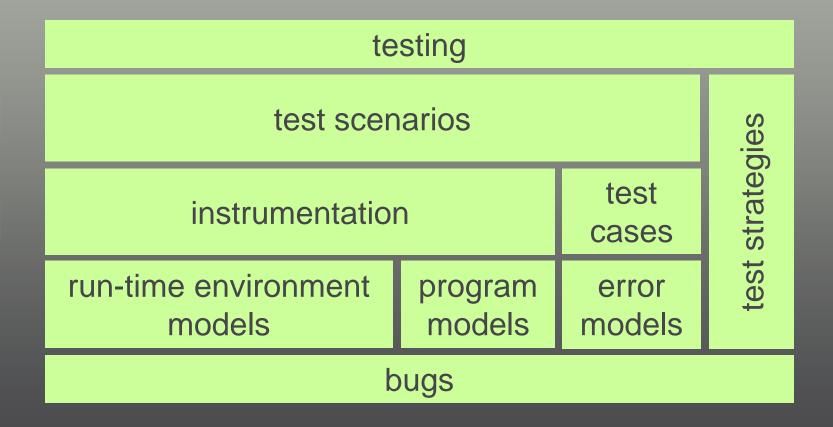
bugs

test cases

test cases

rerror models

bugs



### Test case

A single element selected from an enumerable set of program behaviors

Test completion criterion

A set of test cases defined based on the program behavior model

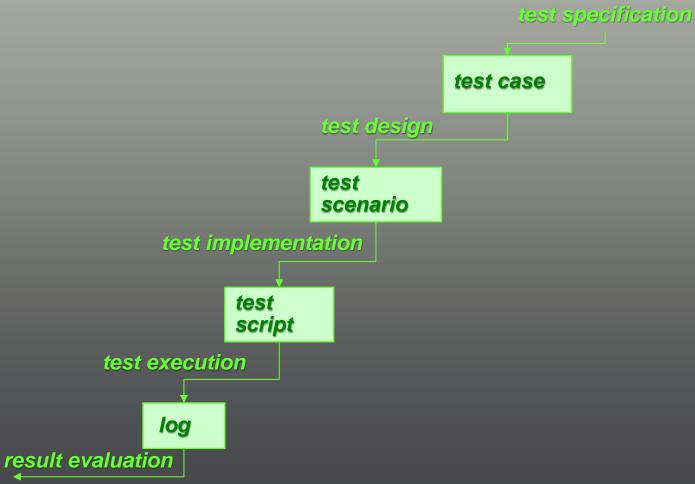
Testing strategy

A set of rules for selecting test cases to a (possibly finite) set according to some adopted criterion

#### Test scenario

Systematic observation of the expected behavior of an IT product conducted in a supervised mode

## Test case "life cycle"



## Testing levels

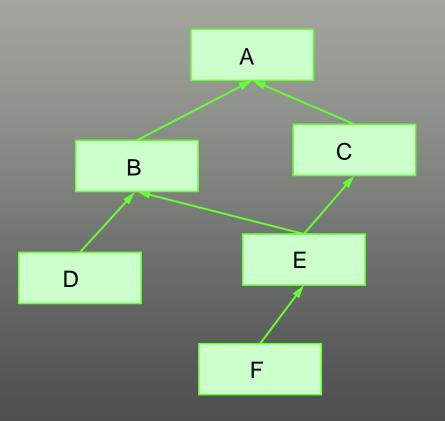
- Unit/module testing
- Integration testing
- System testing
- Acceptance testing
- Alfa/Beta-testing

## Unit testing

- Locating and removing errors
- Test completion
- Regression testing
- Test harness

# Integration testing

- Strategies:
  - incremental
  - big-bang



# Bottom-up method

1 unit D 2 unit F 3 connected units E+F 4 connected units D+E+F+B 5 connected units C+E+F 6 connected units A+B+C+D+E+F   D  driver D driver E driver E  driver B, driver E  formed units A+B+C+D+E+F	I	step	environment	۱
2 unit F 3 connected units E+F 4 connected units D+E+F+B 5 connected units C+E+F 6 connected units A+B+C+D+E+F		1 unit D	driver D	
3 connected units E+F 4 connected units D+E+F+B 5 connected units C+E+F 6 connected units A+B+C+D+E+F				П
4 connected units D+E+F+B driver B, driver E 5 connected units C+E+F driver C, driver E 6 connected units A+B+C+D+E+F				
5 connected units C+E+F driver C, driver E 6 connected units A+B+C+D+E+F				
		5 connected units C+E+F		
		6 connected units A+B+C+D+B	E+F	
D				E
D				1
D				
			D	
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# Top-down method

step	environment				
1 unit A	stubs B & C				
2 connected units A+B	stubs C, D & E				
3 connected units A+B+C	stubs D & E		_		
4 connected units A+B+C+D	stub E		Α		
5 connected units A+B+C+D+E	stub F				
6 connected units A+B+C+D+E+F					
		D		С	
		В		1	
			E		
	D		<u> </u>		
			1		
			F		
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# System testing

category	features	systems
functionality	every "what" the system	dedicated systems
	does	
volume	voluminous input data	file/Big Data systems
stress	input data of high	RT (control) systems
	intensity	
usability	user-friendliness	system HCI
security	break-in attempts	secure systems
performance	system dynamics	RT (control) systems
	measurements	
storage	memory use	memory critical systems
configuration	optional system	S/H upgrades
	configurations	
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# System testing

ı	category	features	systems
ı	compatibility	older versions data	new releases
	installability	installation procedures	complex installation
ı	reliability	statistics (logs, incident	characteristics
			(MTTF, MTTR)
	recovery	"destructive' data	fault tolerant systems
	serviceability	maintenance procedures	administered systems
	documentation	useful in testing?	administered systems
	procedure	required personnel	command/decision systems
		activities	

# Acceptance testing

- Ownership rights transferred from the developer to the client
- Demonstration that all acceptance criteria have been met

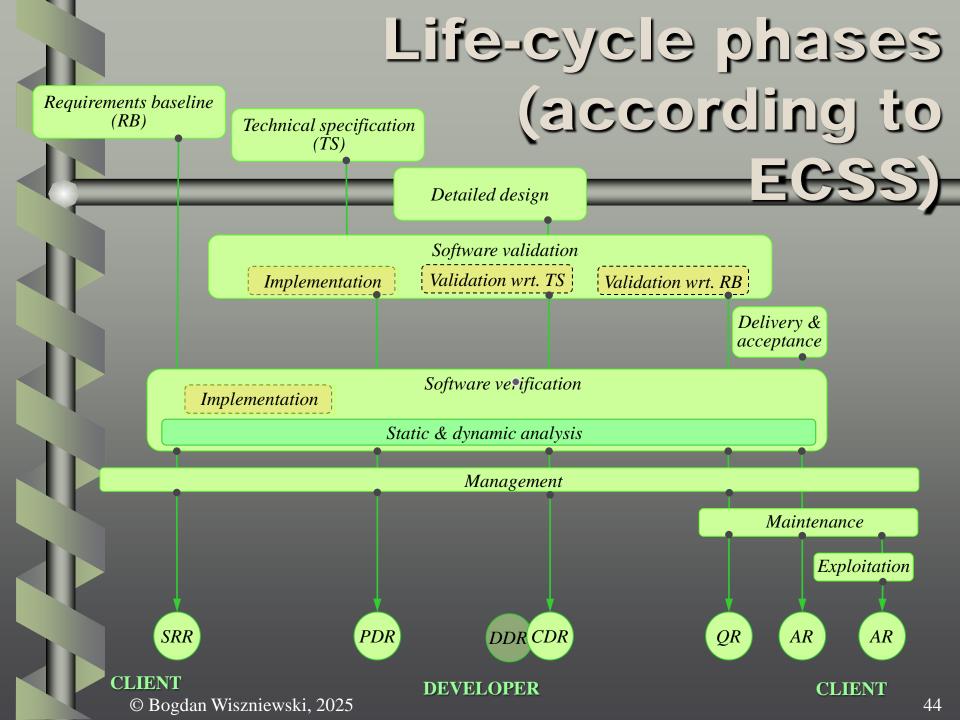
→ requirements specification

- Acceptance: phased, final
- "α-testing": customers test the product at the developer's facility (laboratory).
- "β-testing": customers test the product at their own facility (laboratory)

# B. VVT processes: life-cycle validation, verification and testing

# Responsibility, time schedule

- VVT processes:
  - early error detection
  - continuity of the development activities
  - better understanding of the product
  - decision criteria for the life-cycle phases



## Requirements baseline (RB)

 functional and performance requirements for the planned software provided by the client

## Technical specification (TS)

- a formal specification (logical model) of what the software is supposed to do,
- physical design of the software structure mapping individual functions of the logical model to its components,
- definition of control and data flows between them, the first part of the answer to the question of how the software is supposed to do something).

## Detailed design

- design of algorithms and data structures (physical model), the second part of the answer to the question of how the software is supposed to do something,
- justification of all design decisions,
- implementation of units (code writing/generation),
- testing of code units to demonstrate their compliance with requirements.

### Software validation

 Demonstrating that the system meets all assumed quality goals → quality attributes

## Detailed design

- design of algorithms and data structures (physical model), the second part of the answer to the question of how the software is supposed to do something,
- justification of all design decisions,
- implementation of units (code writing/generation),
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### Software validation

 Demonstrating that the system m goals → quality attributes

- Functionality
- Performance
- Dependability
- Security
- Usability

ıality

## Detailed design

- design of algorithms and data structures (physical model), the second part of the answer to the question of how the software is supposed to do something,
- justification of all design decisions,
- implementation of units (code writing/generation),
- testing of code units to demonstrate their compliance with **RAMS**:

requirements.

### Software validation

Demonstrating that the syste goals → quality attributes

• reliability,

• availability,

maintainability

safety

ality

### Software verification

- confirm that for each activity (phase) of the life cycle there is an appropriate set of documents specifying the requirements for the product of a given phase,
- demonstrate that the product of a given phase is correct and fully compliant with these requirements.

### Implementation

- create code units (coding, adaptation, modification, automatic code generation),
- integrate system units

### Maintenance

 keep the system running after bug fixes, modifications, reinstallations, hardware replacements, etc.

### Delivery and acceptance

- Install the system in its target environment,
- Assess it formally based on the created documentation (RB & TS).

### Exploitation

 Provide support to the end system user (installation, ongoing administration, etc.).

### Management

- project planning (activities, checkpoints, products, techniques and procedures),
- risk identification, countermeasure methods,
- principles of organizing and conducting reviews,
- management of configuration and information flow in the team, time, budget and risk
- ECSS management standards ('M' series):
  - o ECSS-M-ST-10-01C Organization and conduct of reviews
  - o ECSS-M-ST-10C Project planning and implementation
  - o ECSS-M-ST-40C Configuration and information management
  - o ECSS-M-ST-60C Cost and schedule management
  - ECSS-M-ST-80C Risk management

## Life-cycle milestones

- SRR system requirements review:
  - The developer and client agree on the requirements baseline specification (is complete and consistent).
- PDR preliminary design review:
  - The developer and client agree that the technical specification correctly reflects all basic requirements
- DDR detailed design review:
  - Assessment of the possibility of moving to the next phase (all units designed correctly, realistic testing and integration plan, sufficient budget, unresolved issues addressed, existing software may be reused)

## Life-cycle milestones

### CDR - critical design review:

- a key decision to continue or close the project

### QR - qualification review:

- The tools are adequate and the product is mature enough (TRL-8) for acceptance.

### AR - acceptance review:

- all required test cases performed and completed correctly by a given software version in its target environment,
- final approval of the product.

## Product maturity

 Technology readiness levels (NASA):

#### TRL9

•Actual system "flight proven" through successful mission operations

#### TRL8

 Actual system completed and "flight qualified" through test and demonstration (ground or space)

#### TRL 7

System prototype demonstration in a space environment

#### TRL 6

 System/subsystem model or prototype demonstration in a relevant environment (ground or space)

#### TRL 5

Component and/or breadboard validation in relevant environment

#### TRL 4

Component and/or breadboard validation in laboratory environment

#### TRL 3

 Analytical and experimental critical function and/or characteristic proof-ofconcept

#### TRL 2

Technology concept and/or application formulated

#### TRL 1

Basic principles observed and reported

# Quality attributes of a critical software system

### Basic (ECSS standard definitions):

- reliability
  - absence of errors that prevent the system from properly performing all functions required in its RB
- safety
  - no threat to its environment (people, environment, property and infrastructure)
- maintainability
  can always be brought to a state in which any required function
  will be performed properly
- security
   correctly and completely achieves only the goals consistent with
   the owner's intentions

# Quality attributes of a critical software system

- Complex (ECSS standard definitions):
  - availability
    - System is capable of performing the required function at a given moment or time interval
  - dependability

    Ability to build trust in the quality of system services in the long term
- RAMS characteristics
  - reliable + available + maintainable + safe

## Severity number (SN):

Effect	SN	Dependability	Safety
0		Progressive break-down (propagation of a series of failures)	Loss of life, health or permanent disability of crew members or ground staff
phic			Loss of the system
Catastrophic	1		Permanent loss of connection to the manned flight control system
Cat			Destruction of the launch pad
			Serious damage to the natural environment

## Severity number (SN):

Effect	SN	Dependability	Safety
		2 Mission loss	Temporary inability to perform certain activities or illness of crew or ground staff
l g			Serious damage to the link to the manned flight control system
Critical	2		Serious damage to ground infrastructure
			Significant damage to private or public property
			Other environmental damage

## Severity number (SN):

Effect	SN	Dependability	Safety
Significant	3	Significant threat to the mission	Mission dependent
Negligible	4	Minor threat to the mission	Mission dependent

- Non-execution or incorrect execution of the code and other anomalies in its operation cause the system to fail with the following consequences:
  - catastrophic (category 'A')
  - critical (category 'B')
  - significant (category 'C')
  - negligible (category 'D')

## C. Planning of VVT processes

- Verification of the Requirements Baseline (RB) document by recipients (to do list):
  - Comprehensive description of the operating (target) environment
  - Characteristics of the system and devices
  - Key points where to control the system and observe its operation
  - Possible system malfunctions and ways to eliminate their effects
  - Specification of the initial system settings
  - Specification of user scenarios

- Verification of the Technical Specification (TS)
   document by recipients (to do list):
  - System hardware and software requirements are consistent
  - Software requirements are verifiable
  - System architecture is feasible
  - All hardware and software implementation limits have been identified
  - An appropriate verification method is defined for each requirement

- Verification of the system architecture design by developers (to do list):
  - System architecture design accurately reflects the requirements
  - Detailed system design is implementable
  - all dynamic aspects of system operation are correctly considered (processes/threads, their priorities, synchronization mechanisms, resource sharing management)

- Verification of the system detailed design by developers (to do list):
  - Is correct, internally consistent and clearly follows the system architecture design
  - Is testable:
    - o data entry points and triggers, measurement data collection points
    - o temporary and invariant values in key places of the system structure
    - fault injection possible
  - ability to perform maintenance and operational activities
  - all dynamic aspects of system operation are correctly considered (processes/threads, their priorities, synchronization mechanisms, resource sharing management)

## System code verification by developers (to do list):

- its structure and content consistent with requirements (TS, RB), architecture and detailed design
- is correct, testable and compliant with established coding standards
- all possible consequences of run-time errors are under control of the code
- there are no memory leaks
- 100% code execution coverage for assignment and conditional statements in the event of possible catastrophic (category 'A') or critical (category 'B') consequences

- Verification of the unit testing plan and results by developers (to do list):
  - unit tests are consistent with the system design and requirements documents
  - Each unit test ensures examining (at least):
    - execution of each conditional code statement (while, for, if) for the limit values of its predicate
    - o access (read or write) to each global variable
    - o input data outside of their valid ranges, causing incorrect function computations
    - high volume/intensity data inputs to test the unit's performance limits as specified in the requirements
  - all results obtained are as expected and the completion criteria for each test have been met
  - all unexpected results and anomalies of each tested unit are documented in the report.

- Verification of the system integration by developers (to do list):
  - consistency with the system architecture design document
  - testing objectives for system interfaces (adequate and complete list)
  - obtained results obtained are consistent with the expected ones

- Verification of the system validation process by developers wrt RB and TS documents (to do list):
  - results of the validation process were obtained based on test cases, test procedures, inspections and design reviews covering the entire scope of requirements included in TS/RB documents
  - all obtained results of the validation process are consistent with the expected ones

- Verification of the system documentation by developers (to do list):
  - the content of the documentation is adequate, complete and consistent
  - all documents are prepared within the deadlines set up in the project time schedule
  - management of the process of creating/merging documents follows the previously defined procedures

- Hard real-time system analysis:
  - 1. the system is predictable, all worst case scenario events are handled within the required time limits (TS, RB)
    - o an adequate analytical model was used,
    - o alternatively (if not possible) valid simulation experiments were carried out
    - o feasibility of the architectural structure design demonstrated
  - 2. time analyzes were updated at the detailed construction stage...
  - 3. ... and (again) repeatedly, during code verification, unit testing, and integration phases (based on information collected during dynamic analysis of the target system code).

# Validation process

## TS validation activities:

- Test specification (test cases)
  - ✓ for each requirement of each code unit (input data, expected results, test completion criteria)
- Test design (test scenarios)
  - ✓ volume and stress tests, data limit and/or special values
  - ✓ testing the system ability to isolate or reduce the effects of errors
    (soft-fail systems, fault tolerant systems, interactive systems)
  - ✓ correct operation in various valid configurations of the target environment (supervised mode)
  - ✓ data interfaces (protocols, data ranges, time dependencies)
  - ✓ user interfaces (average user error rate, average time to learn)

## Validation process

#### RB validation activities:

- Test specification (test cases)
  - ✓ for each single requirement the mission's intended inputs, expected results, and acceptance criteria
- Test design (test scenarios)
  - ✓ volume and stress tests, data limit and/or special values
  - ✓ testing the system ability to isolate or reduce the effects of errors (softfail systems, fault tolerant systems, interactive systems)
  - ✓ correct operation in various valid configurations of the target environment (random mode)
  - ✓ data interfaces (protocols, data ranges, time dependencies)
  - ✓ user interfaces (average user error rate, average time to learn)

## Delivery and installation process

#### Activities:

- Installation in the target environment
  - ✓ installation plan and installation procedures development
  - testing of installation procedures (installed code, databases and services can be properly activated to function and close afterwards)
  - ✓ conducting introductory training for the end user staff (or even cyclic if requested in RB)
  - ✓ providing resources and information necessary to carry out the installation
  - ✓ testing the system ability to isolate or reduce the effects of errors
    (soft-fail systems, fault tolerant systems, interactive systems)
  - ✓ documenting all relevant events (incidents) during installation

## Acceptance process

#### Activities:

- the recipient (client) prepares the acceptance testing plan
- the recipient performs all tests specified in the acceptance testing plan
  - ✓ the tests must include generation of any executable code from the source code (!)
  - ✓ evaluation of all obtained test results must refer to RB
- developer and recipient perform a formal acceptance review
  - ✓ after completion of the software delivery, installation and acceptance processes

## Experiment management

#### 1. Quality objectives

 compliance with functional specifications, performance characteristics, code characteristics (Halstead. McCabe), test completion degree, etc.,

#### 2. Anticipated problems

description of properties and how they could occur

#### 3. Testing strategies

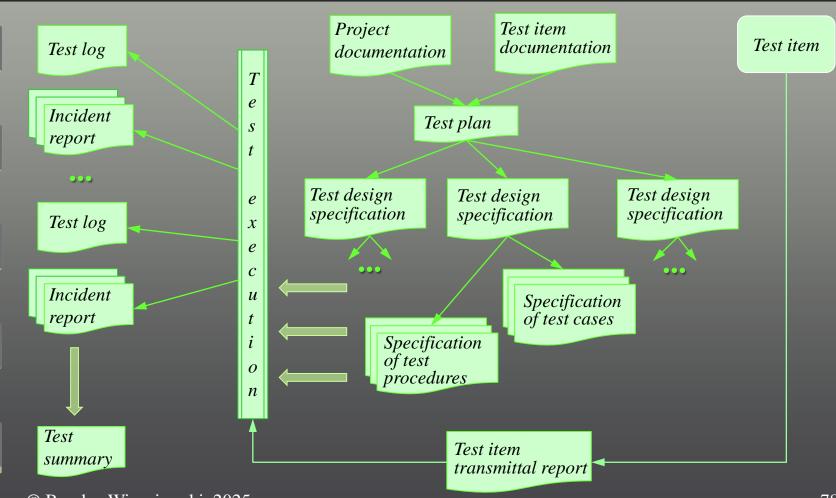
- capable of detecting anticipated problems should affect their definition
- project plan, Pareto effect

## Experiment management

#### 4. Product delivery

- incremental integration with ongoing analysis/testing, monitoring trends of detected anomalies
- 5. Change management, staff training, tools
  - project plan, Pareto effect

## Test documentation (IEEE std.)



## Permanent (static) part of test documentation

- Test plan
  - Time schedule, milestones/checkpoints, management rules
- Test design specification
  - Rationale, explanation and justification of test cases structure
- Specification of test cases
  - Input data and expected results, entry and exit conditions, events and expected reaction

## Permanent (static) part of test documentation

- Specification of test procedures
  - how to perform experiments and measure their advance
- Test completion criteria
  - Conditions to be met by each test procedure
- Test item transmittal report
  - method of delivery and format of items to be tested

## Variable (dynamic) part of test documentation

- Test log
  - recorded activities and data
- Incident report
  - list of incidents requiring further investigation
- Test summary
  - decision of the project management staff and conclusions

### Test procedures

- Disposition of test items
- Exceptional situations
- Experiment costs
- Acceptance criteria

### Disposition of test items

- Item identifier
- Item:
  - version, documentation, responsible person
- Method of delivery:
  - localization, medium
- Status:
  - deviations from documentation, previous version and/or plan, any modifications in progress
- Authorization:
  - person approving disposition

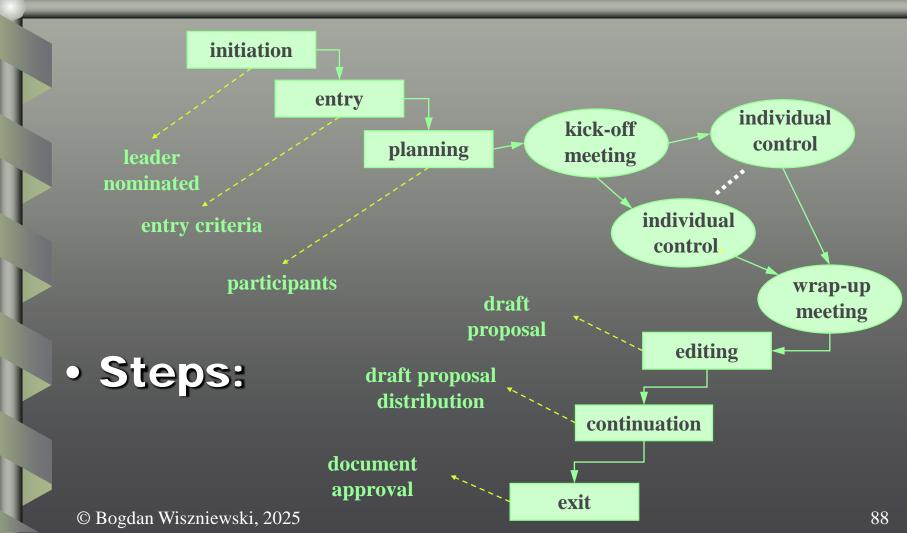
### Exceptional situations

- Any incident during the experiment requiring explanation:
  - input data, expected results, observed anomalies, date and time, step in the scenario, state of the environment, repetition attempts, people performing the test, witnesses
- Determining consequences wrt:
  - continuation of the test plan, test design, scenarios, etc.

### D. Static analysis techniques

- Visually inspect the code or design of a system component to detect:
  - errors,
  - deviations from project standards,
  - missing or incorrect comments,
  - potential portability problems,
  - other problems not "machine checkable"

- Inspection is not a part of the design process:
  - decisions are not made, focus on individual issues only, does not suggest changes or corrections, but
  - allows to detect, identify and remove defects and formally confirm product quality



- Inspection team members (roles)
  - Author: created the work product being inspected.
  - Moderator (leader): plans the inspection and coordinates it.
  - Inspector: examines the work product to identify possible defects.
  - Reader: reads through the documents, one item at a time. The other inspectors then point out defects.
  - Recorder/Scribe: documents the defects that are found during the inspection.

#### Reviews

- Developer (programmer) leads the team through a selected fragment of code
- The team asks questions and comments on potential errors

(!) a narrow and highly interactive technique

### Software audits

- Assessing software processes and products for compliance with requirements, standards, and contractual agreements;
- Ensuring software quality, accuracy, and functionality while reducing legal risks and optimizing performance efficiency;
- Strictly defined criteria and goal, independent assessment team

#### Software audits

#### · Types:

- Technical audit: the software is developed with respect to industry standards.
- Security audit: the software can protect sensitive information.
- Usability and accessibility audit (UX audit): there are no issues with User Experience in the already-deployed software.

## Identification of critical elements

- Failure Mode and Criticality/Element Analysis (FMECA/FMEA)
  - NASA since the 1960s, currently the space, aviation, nuclear and automotive industries
  - ECSS standard, ISO 9000 norm
  - analysis of the effects of defects revealing individually in the products of the architectural/detailed design phases, production phases (coding, testing, integration) as well as flaws of the production process itself
  - most (>80%) defects are detected in the production phase

## Failure mode and effects analysis (FMEA)

#### Steps:

- 1. Identification of system elements and activities of the production process
- 2. List all potential product defects and errors in the activities of individual phases of the production process
- 3. List all probable consequences of the potential defects and errors
- 4. List possible causes of the identified defects and errors
- 5. Analyze all identified defects to:
  - a. assess the materialization of risks
  - b. planning risk mitigation
- 6. Implementation of preventive actions and monitoring their effectiveness.

# Failure mode and effects analysis (FMEA)

- Criticality (CN) is the combination of end effect probability (PN) and severity (SN), CN = SN x PN
  - Criticality number (CN) to rank the risk level;
  - Severity number (SN) to rank severity for the worst-case scenario adverse end effect or state, e.g. catastrophic (4), critical (3), significant (2), negligible (1);
  - Probability number (PN) to classify of the ranges of probabilities of propagation of the effects of revealing a defect beyond the analyzed system unit, e.g.

Level	Range	PN	
High	P >10 <sup>-1</sup>	4	
Moderate	$10^{-3} < P \le 10^{-1}$	3	
Low	$10^{-5} < P \le 10^{-3}$	2	
Negligible	$P \leq 10^{-5}$	1	

## Analysis of critical system elements

#### · Identification of critical elements:

Effect	SN	Probability levels 10 <sup>-5</sup> 10 <sup>-3</sup> 10 <sup>-1</sup> 1				
		PN				
		1	2	3	4	
Catastrophic	4	4	8	12	16	
Critical	3	3	6	9	12	
Significant	2	2	4	6	8	
Negligible	1	1	2	3	4	

- the analyzed unit is critical when:

can always lead to a system catastrophic failure regardless of the defect propagation probability level or its index  $CN \ge 6$ 

#### E. Models for dynamic analysis:

- error,
- program,
- environment

## Where do errors come from?

- The error concept
- Error detection
- Characteristics of code objects under test
- Sources of errors

# The concept of a program error

#### Program error

- an event initiated by a user or the program environment,
- the program code produces an unexpected result

#### Program failure

- the program crashes
- the program is unable to perform some of its functions correctly

#### Error detection

Proof of correctness:

Objective: to prove that the

program is free of errors (is correct)

**Environment:** axiomatic

Reasoning: deduction

#### Error detection

Testing:

**Objective:** 

to demonstrate that the program has errors

**Environment:** *testing or target* 

Reasoning: inductive

### Error detection

Performance testing:

Objective: measure physical

parameters

**Environment:** *testing or target* 

Reasoning: metrics, characteristics

# Characteristics of code objects

- Linguistic metrics:
  - Lines of code (LOC),
  - Statement count (SC),
  - Halstead's metrics.
- Structural metrics:
  - Cyclomatic complexity (McCabe)
- Functional metrics:
  - Computational complexity (time, memory)

### Halstead's metrics

• Program length  $Nlok = N_1 + N_2$ 

$$Nlok = N_1 + N_2$$

Estimated program length

$$HLOC = n_1 \cdot log_2 n_1 + n_2 \cdot log_2 n_2$$

N<sub>1</sub> operators, N<sub>2</sub> operands  $n_1$  unique operators,  $n_2$  unique operands

### Halstead's metrics

Program volume

$$VOLM = (N_1 + N_2) \cdot log_2(n_1 + n_2)$$

Estimated number of errors

$$B = (N_1 + N_2) \cdot log_2(n_1 + n_2)/3000$$

 $N_1$  operators,  $N_2$  operands  $n_1$  unique operators,  $n_2$  unique operands

### Structural metrics

### • Cyclomatic complexity (McCabe):

$$M = L - N + 2P$$

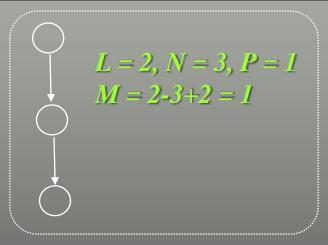
Number of edges (L),

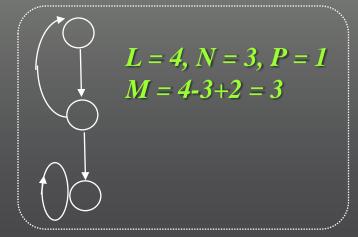
Number of nodes (N),

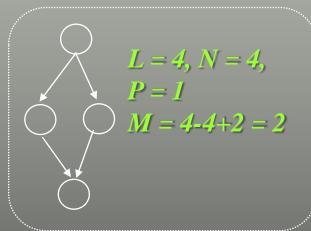
Number of connected components (P)

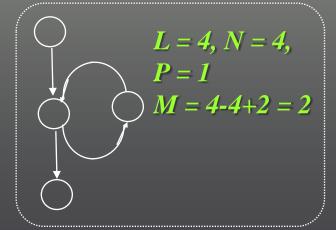
The maximum number of linear, independent paths through a program

### Cyclomatic complexity









## Cyclomatic complexity

 Text (decision instructions) and detailed design

→ Missing or redundant path

- Number of (paths) test cases ≥ M
  - (!) Control flow direction is not taken into account, e.g.M(if-then-else) = M(while-do)
- Ignore language (syntax) complexity

# Functional metrics

## Complexity level (algorithms):

Symbol	Complexity	Example
Θ <b>(1)</b>	constant	celdist desd
⊖(log n)	logarithmic	binary search
Θ <b>(n)</b>	linear	GCD of n-digit numbers
Θ(n log n)	linearithmic	Fast Fourier Transform (DFT)
Θ(n <sub>c</sub> )	polynomial	path tracking (robots)
$\Theta(\mathbf{c}_{\mathbf{u}})$	exponential	generation of prime numbers

## Sources of errors

- Requirements specification:
  - completeness
  - consistency

# Sources of errors

### • Design:

- correctness
- testability



### Sources of errors

- Coding ("translation" of an algorithm into some program code):
  - textual (typos, omissions, etc.)
  - misunderstanding semantics of the implementation language,
  - not understanding semantics of the algorithm,
  - not understanding (knowing) the requirements.

## Models

### • Program:

- Control flow,
- Events,
- Data flow,
- State transitions

## Models

#### • Error:

- Control flow errors
- Data flow errors
- State errors
- Text anomalies

### Models

- Run-time environment:
  - Sequential (stream) processing
  - Even driven sequential proccessing
  - Concurrent processing
  - Parallel processing
  - Distributed processing

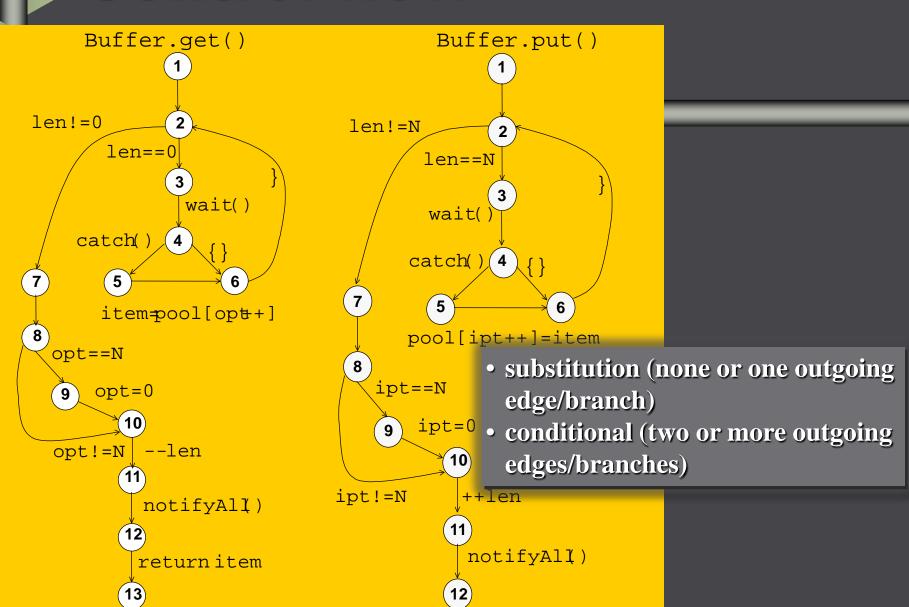
```
int N = 10; //total buffer capacity
ipt = 0; //input index
opt = 0; //output index
len = 0; //current buffer load
/** shared resource **/
char *pool = new char[N];
/** consumer **/
/* 1 */ public synchronized char get(){
        char item;
/* 2 */ while (len == 0){}
/* 3 */ try {wait(); //buffer is empty
/* 4 */ }catch(Interrupted Exception){
/* 5 */ }
/* 6 */ } //semaphore opened
/* 7 */ item = pool[opt++];
/* 8 */ if (opt == N)
/* 9 */ opt = 0; //modulo N
/*10 */ --len; //one element taken
/*11 */ notifyAll(); //buffer is not full
/*12 */ return item;
/*13 */ }
/** producer **/
/* 1 */ public synchronized void put(char item){
/* 2 */ while (len == N){
/* 3 */ try {wait(); //buffer full
/* 4 */ }catch(Interrupted Exception){
/* 5 */
/* 6 */ } //semaphore opened
/* 7 */ pool[++ipt] = item;
/* 8 */ if (ipt == N)
/* 9 */ ipt=0; // modulo N
/*10 */ ++len; // one element added
/*11 */ notifyAll(); //buffer is not empty
/*12 */ }
```

public class Buffer {

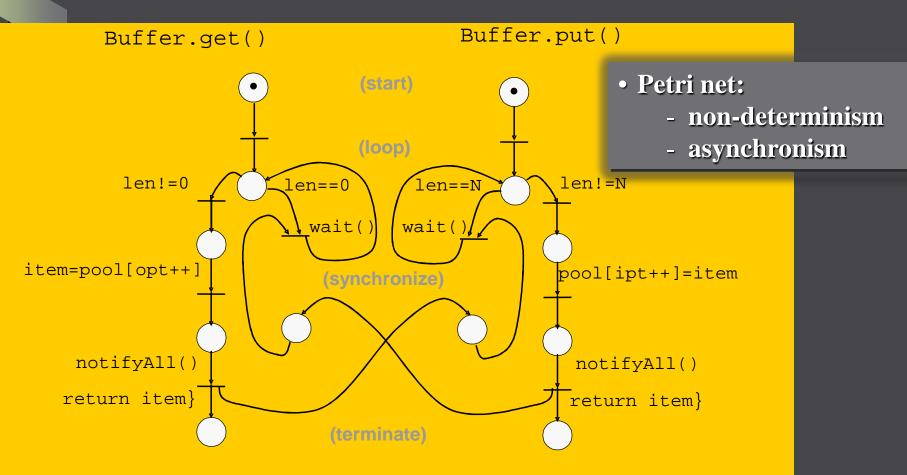
# Example

- Shared table pool with N elements
- Method Buffer.get() to fetch one character
- Method Buffer.put() to insert one character

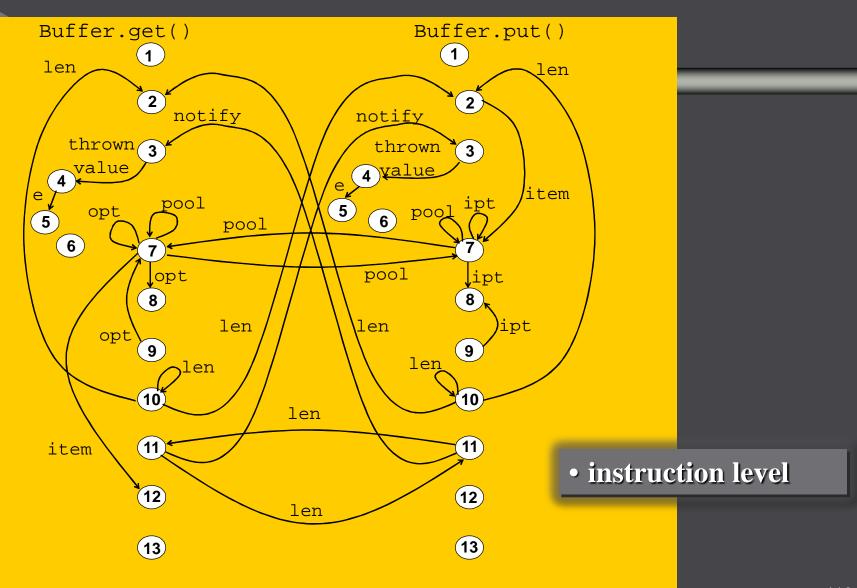
## **Control flow**



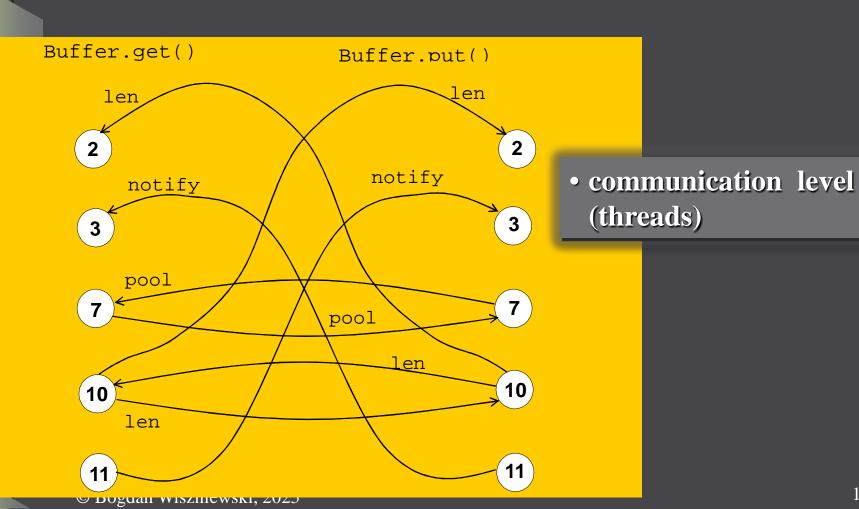
## **Events**



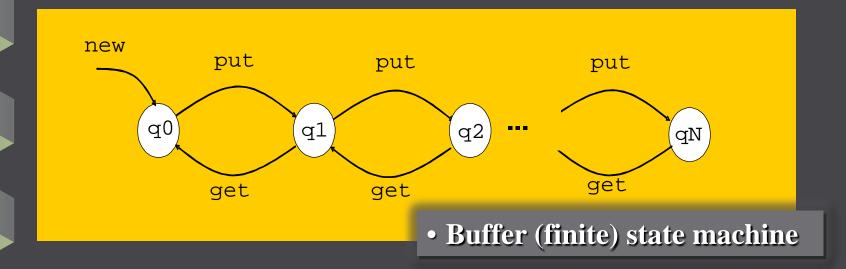
## **Data flow**



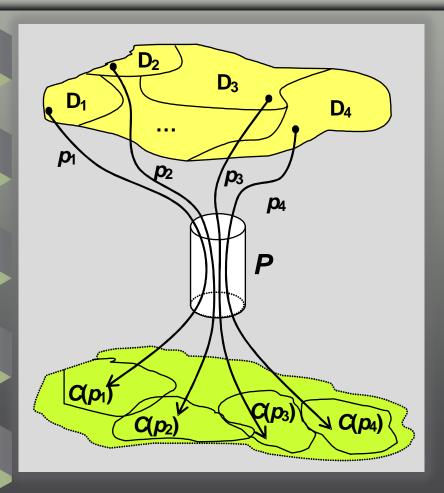
## **Data flow**



# **State transitions**



## Control flow errors



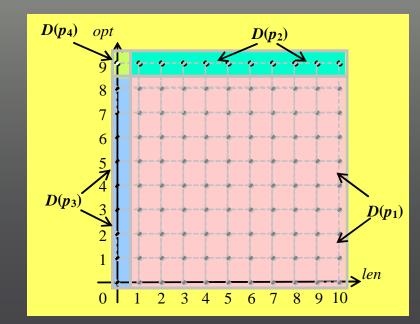
#### Path (execution) conditions:

$$p_1(\overline{x}) = (len_0 \neq 0) \land (opt_0 + 1 \neq 10)$$

$$p_2(\bar{x}) = (len_0 \neq 0) \land (opt_0 + 1 = 10)$$

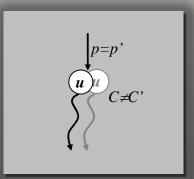
$$p_3(\overline{x}) = (len_0 = 0) \wedge (opt_0 + 1 \neq 10)$$

$$p_4(\overline{x}) = (len_0 = 0) \land (opt_0 + 1 = 10)$$

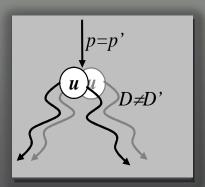


# Control flow errors

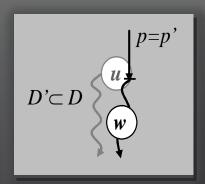
#### 1. Path 'computation' error:



#### 2. Path 'domain' error:

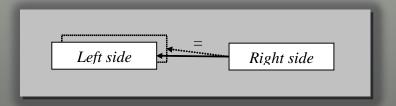


## 3. 'Subcase' (missing path) error:

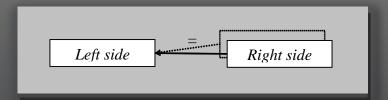


# Control flow errors

1. Value assigned to a wrong variable:



2. Variable assigned a wrong value:



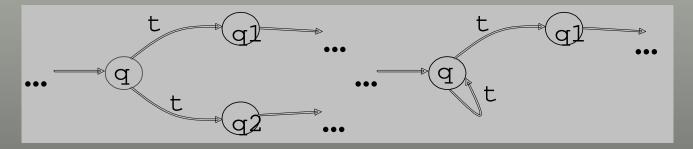
## State errors

#### Deadlock

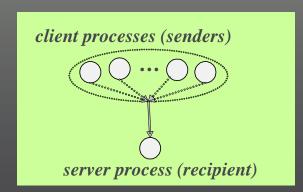
```
public synchronized char get() {
       char item;
       while (len == 0) {
            try {
                wait(); //buffer is empty
            } catch (InterruptedException e) {}
        } //semaphore opened
       item = pool[opt++];
       if (opt == N) opt = 0; // modulo N
       --len; //one element taken
       notifyAll(); //buffer is not full */
       return item;
                                 put
                                          put
                                                       put
```

## State errors

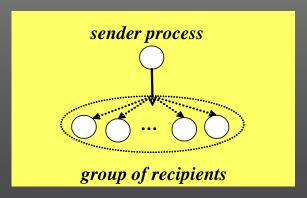
#### Races



#### - on reception:



#### - on sending:



## Text anomalies

### Interpretation of syntax

```
public synchronized char get() {
   char item;
   while (len == 0);
       wait(); //buffer is empty
      } catch (InterruptedException e) {}
   } //semaphore opened
   item = pool[opt++]; redundant semicolon
   if (opt == N);
         opt = 0 // modulo N
   notifyAll(); \( \text{/one element taken} \)
    --len; //one element taken
   return item;
                 empty statement
```

## Text anomalies

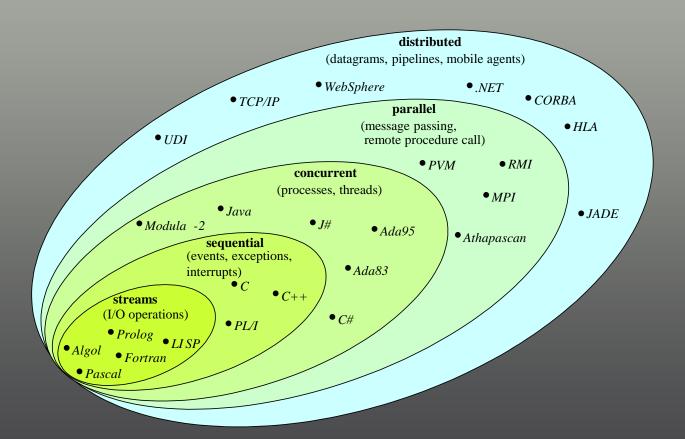
#### Side effects

```
int main() {
   int x,y;
   int *z;
   z=&x;
   z++=1; /* initialization of x */
   z=2; /* alleged initialization of y */
}
```

## Text anomalies

### Implicit type conversion

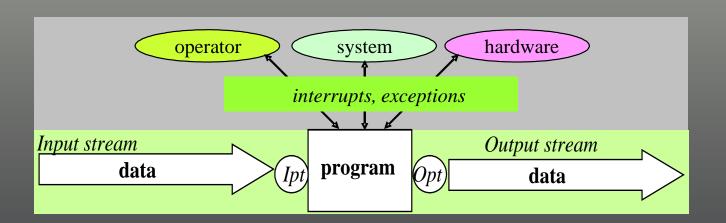
```
void ff(int); // function with one int argument
int ival=3.14; // value 3.14 narrowed to 3, ival=3;
ff(3.14); // value 3.14 narrowed to 3,
          // ff(3) called;
ival=4.0; // conversion of 4.0 to 4 (not narrowed),
ival=4;
double fval=5; // promotion of 5 to 5.0 of a "wider"
               // type, fval=5.0;
int val=1;
fval=val+3.14; // promotion of 1 to 1.0 of a "wider"
               // type, fval=1.0+3.14;
```



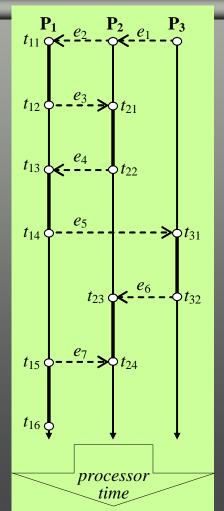
Sequential stream processing



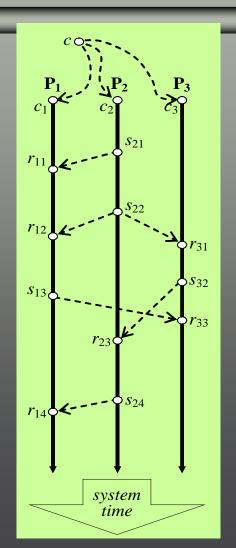
 Event driven sequential stream processing



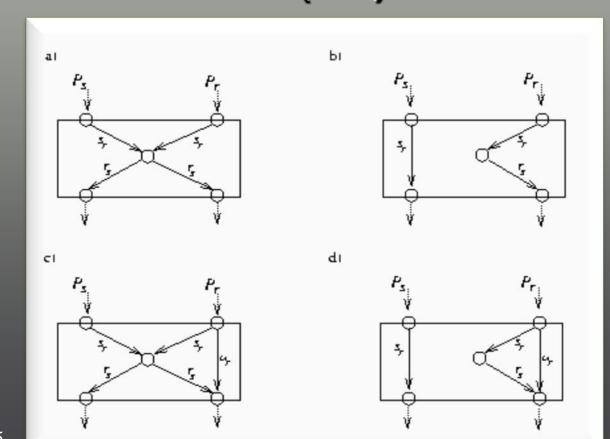
Concurrent processing



Parallel processing

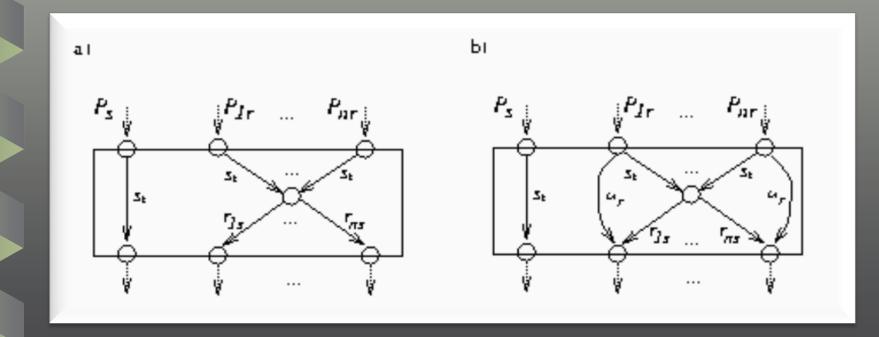


Communication events (1-1)

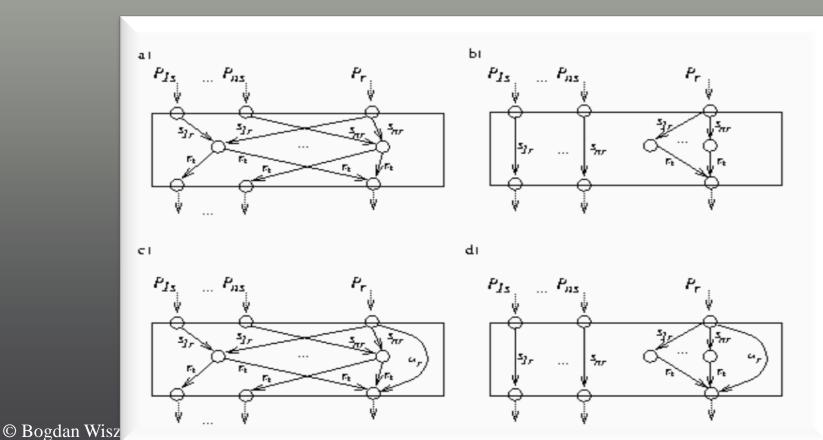


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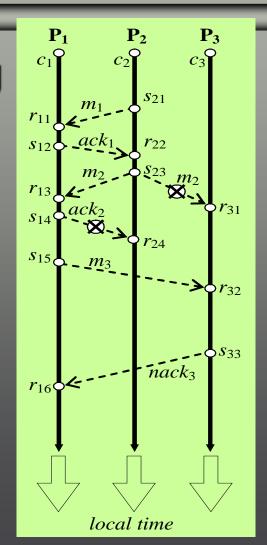
Communication events (1-n)



Communication events (n-1)



Distributed processing



# Dynamic analysis techniques

### Black-box testing:

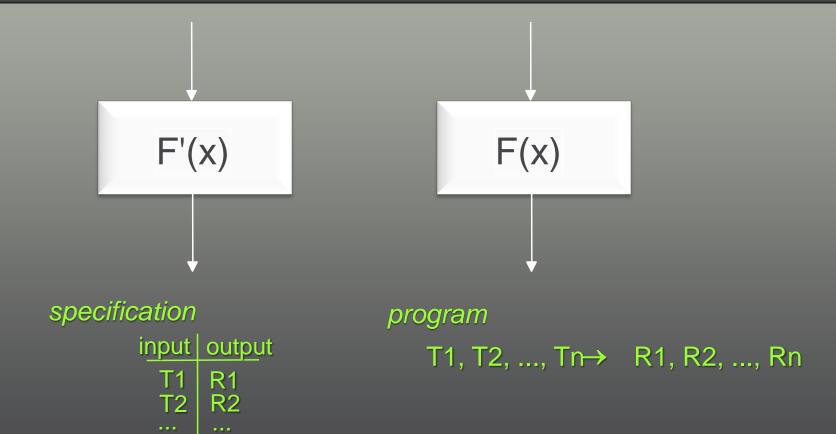
- Program = function,
- Test cases based on requirements specification
- Potentially all errors but practically in an infinite time

# Dynamic analysis techniques

- White-box (structural) testing:
  - Program = structure,
  - Test cases based on technical (architectural/detailed design) specification or the program code
  - Not all errors but in a (practically) predictable time

## F. Black-box testing

# Black-box strategies



Rn

# Black-box strategies

Mathematical property:

$$T=\{t_i\mid i=1,...,N\},\,F'(T)=F(T)\Longrightarrow F'(x)\equiv F(x)$$

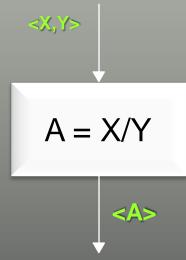
- Limitations:
  - ! Undecidability of function equivalence (even of primitive recursive functions!)
  - ! Approximate binary arithmetic (floating point error, rounded value, register overflow error)

# Black-box strategies

- Special values
- Transcendent values
- Polynomial equivalence
- Monte-Carlo testing

# Special values

#### Example

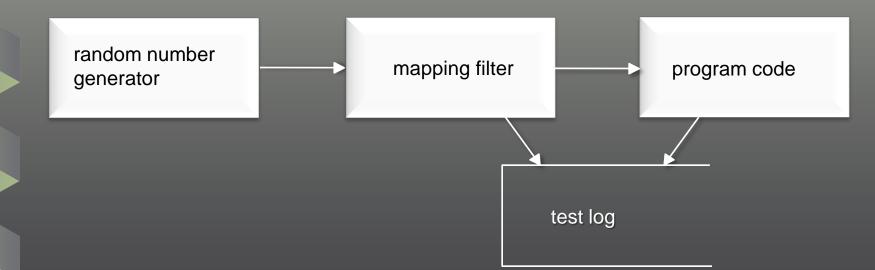


# Polynomial equivalence

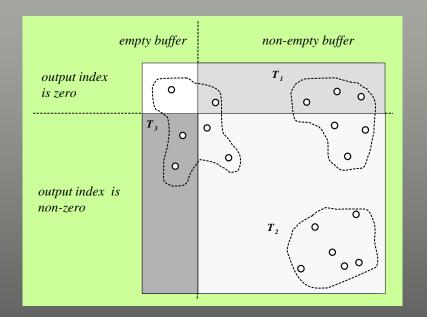
- (!) Standard math functions are computed using polynomials
- Classic polynomial algebra:
  - Class of polynomials cf(n,x),
  - Tested F, specified F' ∈ CF
  - $T = \{t_1, t_2, ..., t_{n+1}\}$
  - $-F'(T)=F(T) \Rightarrow F'(x) \equiv F(x)$

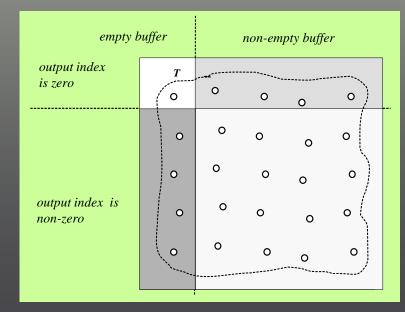
## Monte-Carlo testing

(!) Exercise the program for its most typical and common input values



# Monte-Carlo testing





#### **G.White-box testing**

- Structural model (program, system)
  - control flow testing
  - data flow testing
  - mutation testing

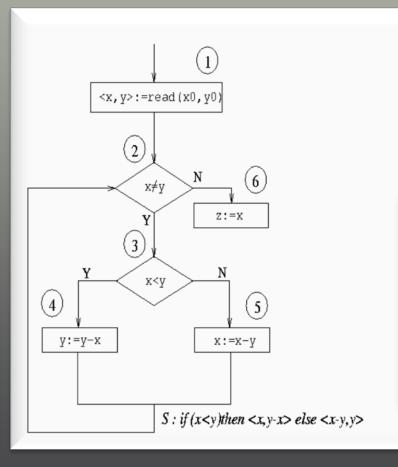
- Test evaluation:
  - quantitative (metrics) → rule of thumb
  - qualitative (model) → errors are deviations
- Passing a test:
  - all required test cases exercised
  - all results obtained consistent with the expected ones

→ test strategy

- Branch testing
- Path testing
  - boundary-interior method
  - domain testing
  - computational equivalence of paths
  - simple loop patterns

- Data flow testing
  - definition-use chains
- Mutation testing
  - Text anomalies

#### Branch testing



(!) Each predicate "true" and "false"

```
while w. "2":
    (2,3), (2,6)

if w. "3":
    (3,4), (3,5)
```

### Path testing

- (!) Incorrect control flow implies incorrect results
- (1) Paths can exercise control flow systematically

#### Program model:

- Control flow graph:
- Input variables:
- Program (input) domain:
- Program path:
- Path condition:
- Path domain:
- Path computation:

$$x = \langle x_1, x_2, ..., x_n \rangle$$

$$D=X_1\times X_2\times ...\times X_n$$

$$p=(n_0, n_1, ..., n_k)$$

$$\mathbf{p}(\mathbf{x})$$

$$\mathbf{d}(\mathbf{p}) = \{ \mathbf{x} \mid \mathbf{p}(\mathbf{x}) \}$$

$$c(p): d(p) \rightarrow R$$

## Path testing

#### Strategies:

- boundary-interior method
- domain testing
- computational equivalence of paths
- simple loop patterns

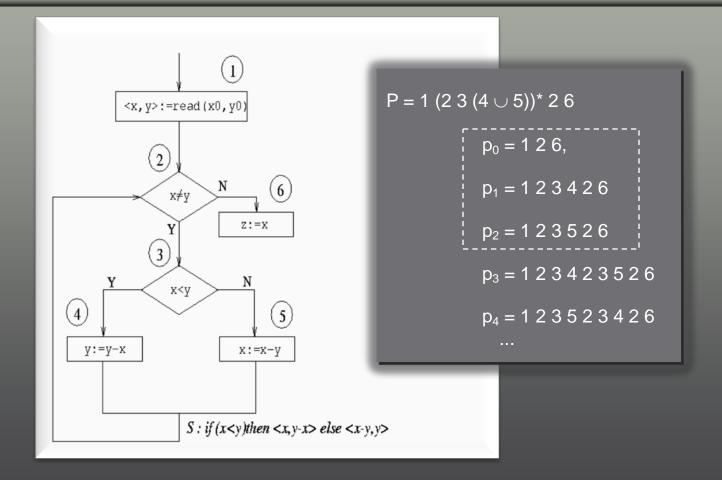
# Boundary-interior method

(!) Problem with loops

- Intuitive criterion:
  - Each loop ZERO and non-zero number of iterations,
  - Each loop MAX number of iterations

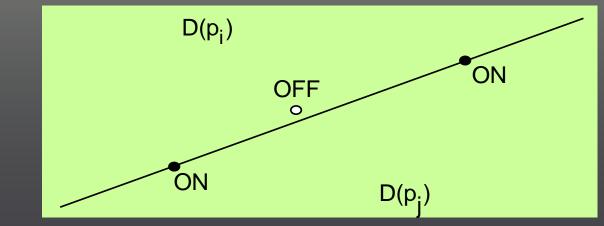
→ Similar but more demanding then branch testing

#### Example



(4) Looking for domain errors

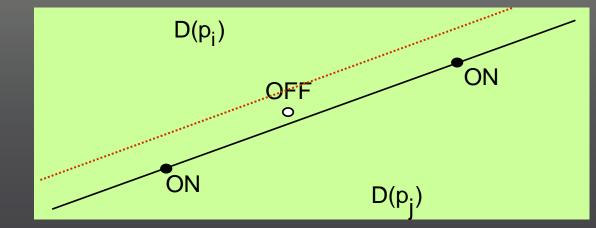
- Assumptions:
  - Predicates p(x) are linear functions on X,
  - Path computations c(p) are different,
  - No coincidental correctness.



#### (1) Looking for domain errors

#### Assumptions:

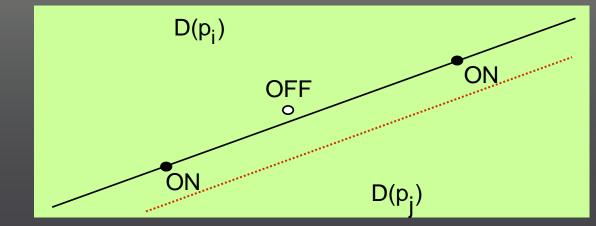
- Predicates p(x) are linear functions on X,
- Path computations c(p) are different,
- No coincidental correctness.



#### (1) Looking for domain errors

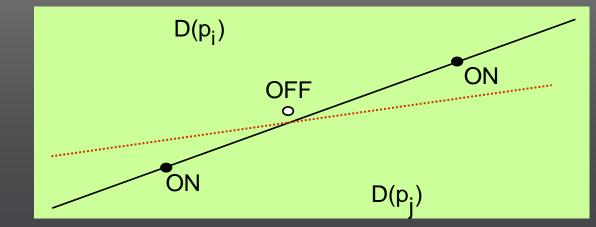
#### Assumptions:

- Predicates p(x) are linear functions on X,
- Path computations c(p) are different,
- No coincidental correctness.



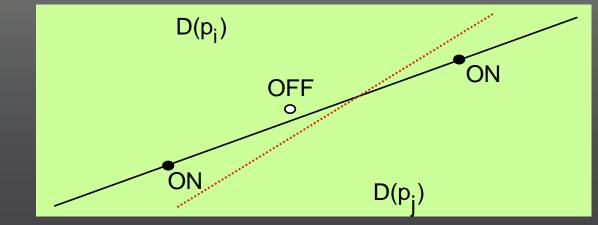
#### (1) Looking for domain errors

- Assumptions:
  - Predicates p(x) are linear functions on X,
  - Path computations c(p) are different,
  - No coincidental correctness.



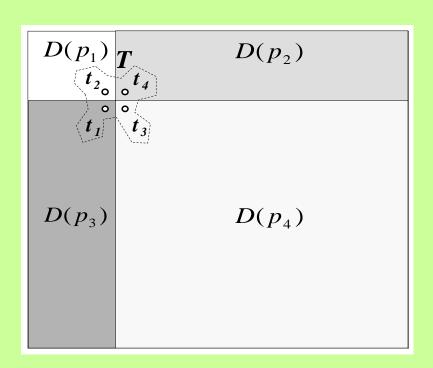
(1) Looking for domain errors

- Assumptions:
  - Predicates p(x) are linear functions on X,
  - Path computations c(p) are different,
  - No coincidental correctness.



## Example

Domain testing



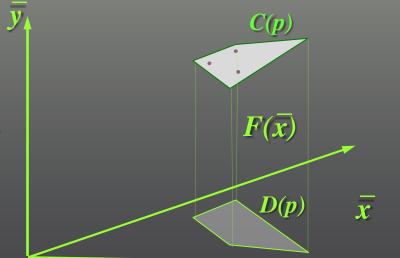
# Computational equivalence of paths

- Input data:
- Input domain:
- Output variables:
- Path computation space:

#### Test case:

path p

(n+m)-vector 
$$t = \langle d_1, d_2, ..., d_n, r_1, r_2, ..., r_m \rangle$$
  
n+m vectors  $\{t_1, t_2, ..., t_{n+m}\}$ 



### Example

#### Path computation testing:

- path

$$p_1$$
: 1-2-7-8-10-11-12-13

– computation

 $|C(p_1)| < len_0, opt_0, item, e, pool[10], len_0, opt_0 > \to < len_0, opt_0, item, e, pool[10], len_0 - 1, opt_0 + 1 > \to < len_0, opt_0, item, e, pool[10], len_0 - 1, opt_0 + 1 > \to < len_0, opt_0, item, e, pool[10], len_0 - 1, opt_0 + 1 > \to < len_0, opt_0, item, e, pool[10], len_0 - 1, opt_0 + 1 > \to < len_0, opt_0, item, e, pool[10], len_0 - 1, opt_0 + 1 > \to < len_0, opt_0, item, e, pool[10], len_0 - 1, opt_0 + 1 > \to < len_0, opt_0, item, e, pool[10], len_0 - 1, opt_0 + 1 > \to < len_0, opt_0, item, e, pool[10], len_0 - 1, opt_0 + 1 > \to < len_0, opt_0, item, e, pool[10], len_0 - 1, opt_0 + 1 > \to < len_0, opt_0, item, e, pool[10], len_0 - 1, opt_0 + 1 > \to < len_0, opt_0, item, e, pool[10], len_0 - 1, opt_0 + 1 > \to < len_0, opt_0, item, e, pool[10], len_0 - 1, opt_0 + 1 > \to < len_0, opt_0, o$ 

– hyperplane

$$\begin{bmatrix} opt \\ len \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} opt_0 \\ len_0 \end{bmatrix} + \begin{bmatrix} 1 \\ -1 \end{bmatrix}$$

## Simple loop patterns

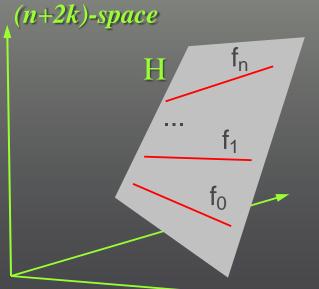
- Input variables:
- Input domain:
- Program variables:
- Program computation space:

$$f_0 = g_{sv}g_{ve}, \quad f_1 = g_{sv}hg_{ve}, \quad ..., \quad f_n = g_{sv}h^ng_{ve}, \quad ...$$
 $f_n = \begin{cases} f_0 & n=0 \\ f_{n-1}H & n>0 \end{cases}$ 
 $H = (g_{ve})^{-1}h(g_{ve})$ 

test completion criterion:

$$S = 1 + \lceil (2k-1)/n \rceil$$
 paths

$$x = \langle x_1, x_2, ..., x_n \rangle$$
 $D = X_1 \times X_2 \times ... \times X_n$ 
 $z = \langle z_1, z_2, ..., z_k \rangle$ 
 $(n+2k)$ -dimensional



### Example

```
int asynBCD(int number,int count){
            char symbol;
2: 3
             for(;;)
3: 4
             {for(;;)
4: 5
             {receive(symbol);
             if((symbol==SPACE)||(symbol==STOP))
6: 11
            break;
7: 8
             count++;
8: 9 10
             if(count>9)
                                        Input variables:
9:
             return ERROR;
10: 3
                                        symbol, number, count
11: 12
             number=10*number+count;
                                                           \rightarrow n=3
12: 13 14
             if(symbol==STOP)
13:
             return (number);
                                        Program variables:
14: 2
                                        number, count
15:
                                                           \rightarrow k=2
```

#### Data flow

#### • Simple chain:

<definition, use>

d: 
$$x = f(5) + 3y$$

...

$$u: z = 2x-y$$

#### Use chain:

<all-definition, use>

d: 
$$x = f(5) + 3y$$

...

$$u: z = 2x-y$$

...

(a:) 
$$\mathbf{w} = \mathbf{x}^* \mathbf{z}$$

#### • Live chain:

<all-definition, all-use

d: 
$$x = f(5) + 3y$$

...

٠.

a: 
$$w = x^*z$$

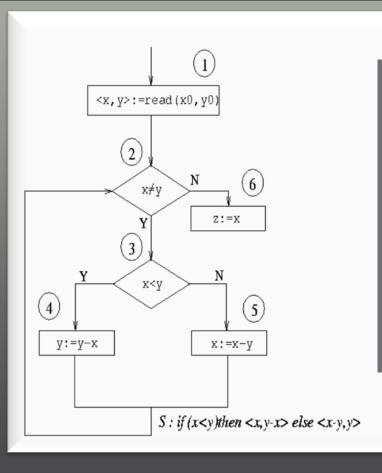
•••

$$b: y = x+w$$

#### criterion

 $\rightarrow$  Exercise each chain

## Examples



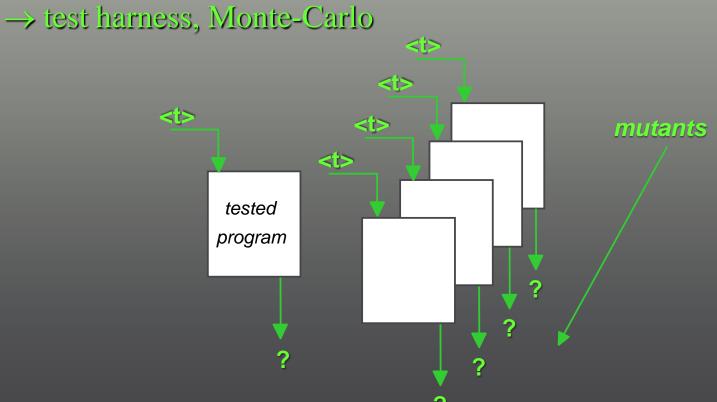
"d-u" chains (simple):

"ad-u" chains (use):

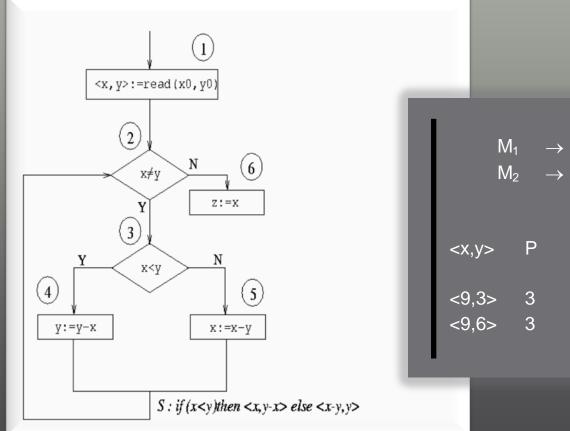
"ad-au" chains (live):

## Mutation testing

(!) errors result from occasional "typos" in the program text



### Example



```
M_1 → while (x=y) ...

M_2 → if (x=y) ...

<x,y> P M_1 M_2

<9,3> 3 9 3

<9,6> 3 - ↑
```

#### Structure of test cases

- Input data
- Expected results
- Environment settings
- Scenario context

### Test script

```
/* TeSS 1 */
/* request the master to go first (1) */
 (before 0 22 [])
                                          Logging the state
>
/* reach the voting configuration by slaves (2) */
 (before 1 26 [print stid; print ntid;)
 (before 2 26 [print stid; print ntid;])
 (before 3 26 [print stid; print ntid;])
>
/* reach the reporting configuration by slaves (3) */
  (before 1 41 [print data;])
  (before 2 41 [print data;])
  (before 3 41 [print data;])
```

## Test script

```
/* TeSS 2 */
                                             Value enforcement
/* request the master to go first (1) */
/* spoil v_size of slave #3 before voting */
 (before 0 22 [])(after 3 23 [set v_size=0;])
 /* reach the voting configuration by slaves (2) */
 (before 1 26 [])
 (before 2 26 [])
 (before 3 26 [])
/* reach the reporting configuration by slaves (3) */
 (before 1 41 [print data;])
 (before 2 41 [])
 (before 3 41 [])
/* make slave #1 winning the race */
 (after 0 22 [])(after 1 41 [])
```

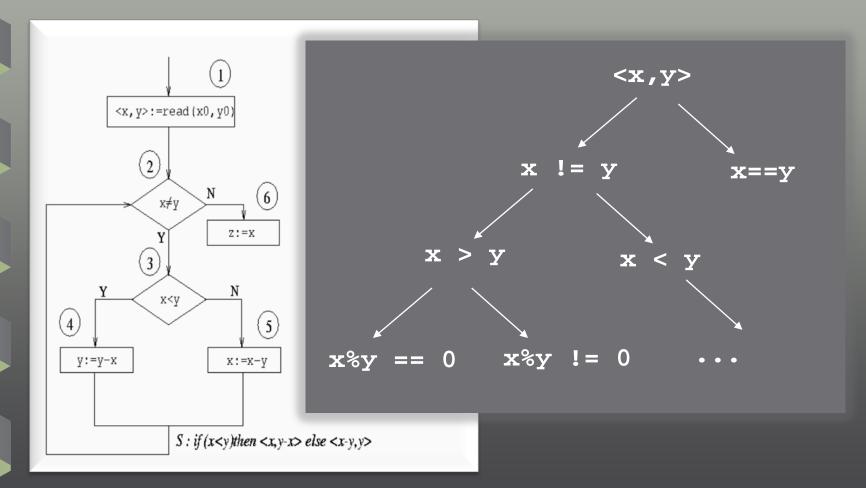
#### Attributes of test cases

- Representativeness
  - A single case represents a subset
- Feasibility
  - Non-empty set of input data exists, eg. path condition is satisfied
- Observability
  - Deterministic automaton
- Reproducibility
  - All input data identified (path condition interpretation)
  - Timing conditions under tester's control

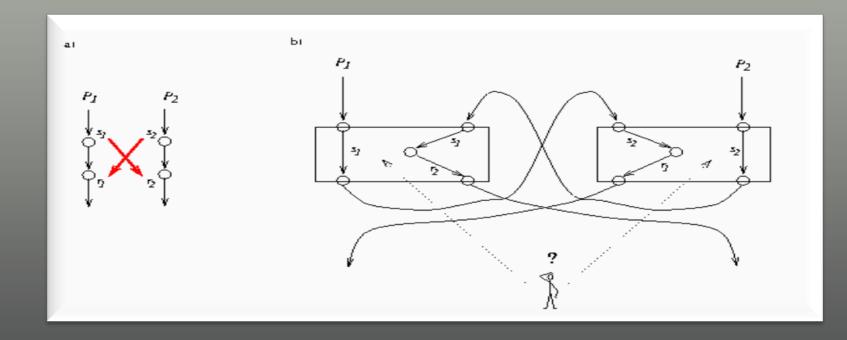
### Feasibility

```
int asynBCD(int number,int count){
            char symbol;
2: 3
            for(;;)
3: 4
            {for(;;)
            {receive(symbol);
            if((symbol==SPACE)||(symbol==STOP))
6: 11
            break;
7: 8
            count++;
8: 9 10
            if(count>9)
9:
            return ERROR;
10: 3
11: 12
            number=10*number+count;
12: 13 14
            if(symbol==STOP)
13:
            return (number);
14: 2
15:
                      !? p = 12(3457810)^{10}345789
```

# Representativeness

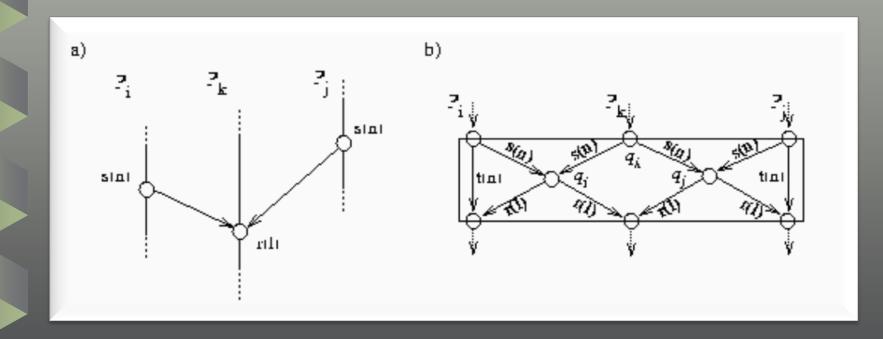


# Observability



→ Testing error

# Reproducibility



### Logging results

### Checkpoint

- static ("compiled in")
- dynamic (breakpoint)

#### Log

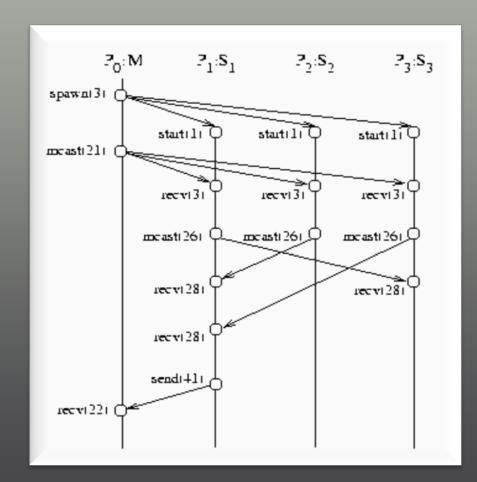
- centralized
- distributed

### Result analysis

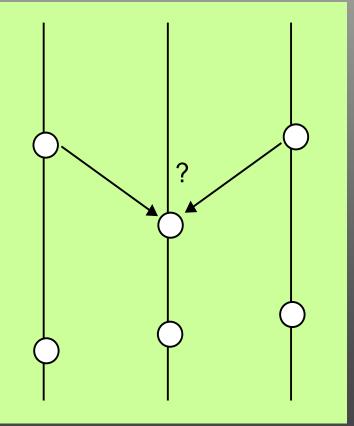
- on-line (state or event detection),
- off-line (% of test coverage, error localization)
- replay (visualization, state recovery)

## Test scenario execution mode

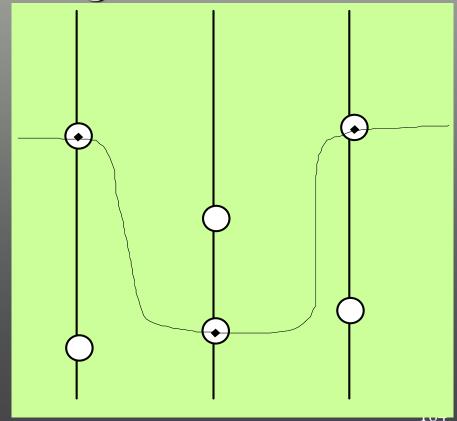
- random
- supervised
- deterministic



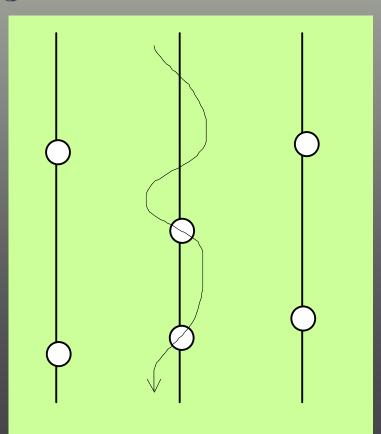
One-thread-One-time (OtOt):
 race detection



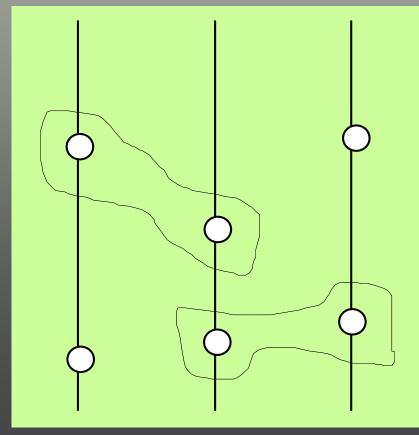
 Many-threads-One-time (MtOt): global state monitoring



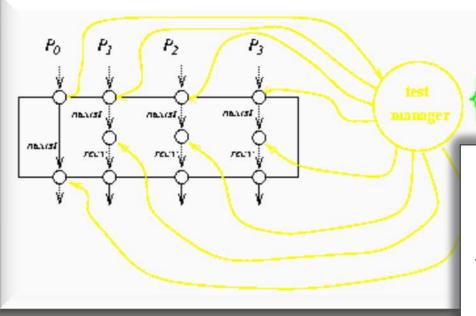
 One-thread-Many-times (OtMt): single process path testing



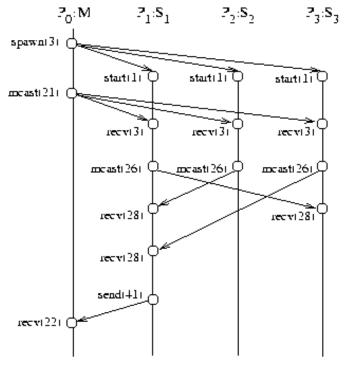
 Many-threads-Many-times (MtMt): event monitoring



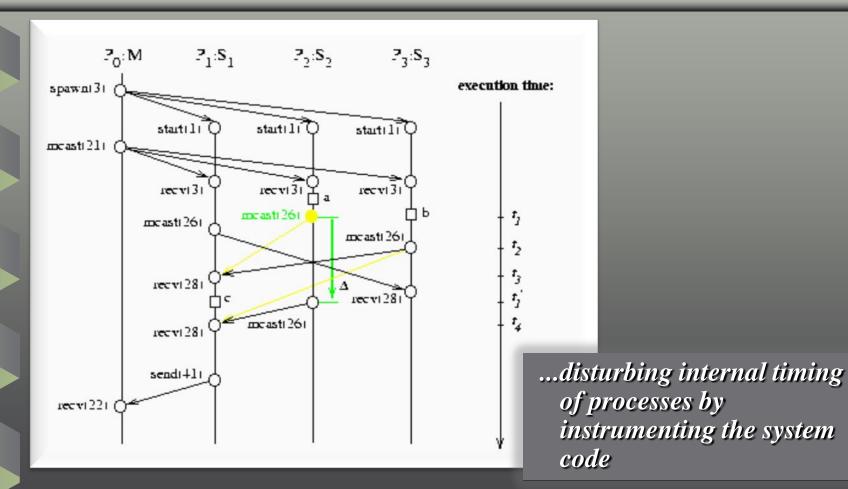
# Instrumenting code and environment



- mcnst[0,21] - recv[1,3] - recv[2,3] - recv[3,3]



### Probe effect



## Log structure

- Heading:
  - Unique identifier
  - Comment
  - Records (table of content)
- Record:
  - date, time, test case ID,
  - event, local state, context
- Event:
  - Statement executed, signal sent/received, exception raised, variable value changed
- State:
  - Object memory content
- Context:
  - history, condition, global state

## What is worth logging?

#### Potential error occurrences:

- Arithmetic instructions (function calls, assignments),
- Predicate (condition) evaluation,
- Type conversion, actual vs formal parameters,
- Return statements,
- Dynamic variables,
- Systems diagnostics, exception handlers,
- Message packing/unpacking,
- Message tagging,
- Races,
- Communications actions matching

### Error localization

(!) Knowing that the program has a bug doesn't mean knowing what causes it

### Debugging:

- Post-mortem print-out, core dump,
- Trace file (log)
- Building a hypothesis,
- Elimination of hypotheses

#### Tools:

- Print-out
- Breakpoint trap
- Instant replay

# Is it possible to do without testing?

- Programmers make mistakes when, when creating a program, they are unable to remember all the details needed to make it correct
- There are no bug-free programs, they are only poorly tested
- Programs considered correct may still have errors
- We can mistake correct program behavior for a wrong one (and vice versa)
- Errors reveal throughout the entire life of a program