



Critical systems software testing and QA

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Course organization

- **Office hours:**
Thursdays, 15:15-17:00 hrs
- **Practicals (labs & project):**
Dr. **Adam Łukasz Kaczmarek**,
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Course organization

- Objectives:
 1. Present software development standards in the European space industry and techniques of their implementation.
 2. Learn how to assess and manage critical system software quality in an IT project.
 3. Gain basic hands-on experience in bug tracking and reporting in a software project.

Course content

1. Development of high-quality IT systems in a systematic way
2. ECSS standards: series „E” and „Q”
3. Software product life cycle vs. testing cycle.
4. Validation, verification and testing (VVT) processes in a software product lifecycle.
5. Planning of VVT processes.
6. Static analysis techniques of software systems.
7. Error, program and environment models in software testing.
8. Black-box (functional) software testing strategies.
9. White-box (structural) software testing strategies

Literature

- IEEE Software and Systems Engineering Standards, http://standards.ieee.org/findstds/standard/software_and_systems_engineering.html
- Space engineering – Software, ECSS-E-ST-40C, 6 March 2009, European Cooperation for Space Standardization, ESA-ESTEC, <http://ecss.nl/standards/ecss-standards-on-line/active-standards>
- Space product assurance - Software product assurance, ECSS-Q-ST-80C Rev.1, 15 February 2017, European Cooperation for Space Standardization, ESA-ESTEC, <http://ecss.nl/standards/ecss-standards-on-line/active-standards>

Grading

Z#	Week	%	opis
L1	8	15	Definition of tests for selected functionalities
L2	8	15	Test execution and reporting
P	15	30	Documentation of the testing process according to the ESA standard (ECSS)
T	8/15	40	All weeks (lecture part)
	=	100	...of the final score

Pass/fail criteria

1. Total score of 50% minimum
2. Attending the final test (any non-zero score accepted)
3. All assignments must be submitted in the due time. No late assignments accepted, except of a valid medical excuse.

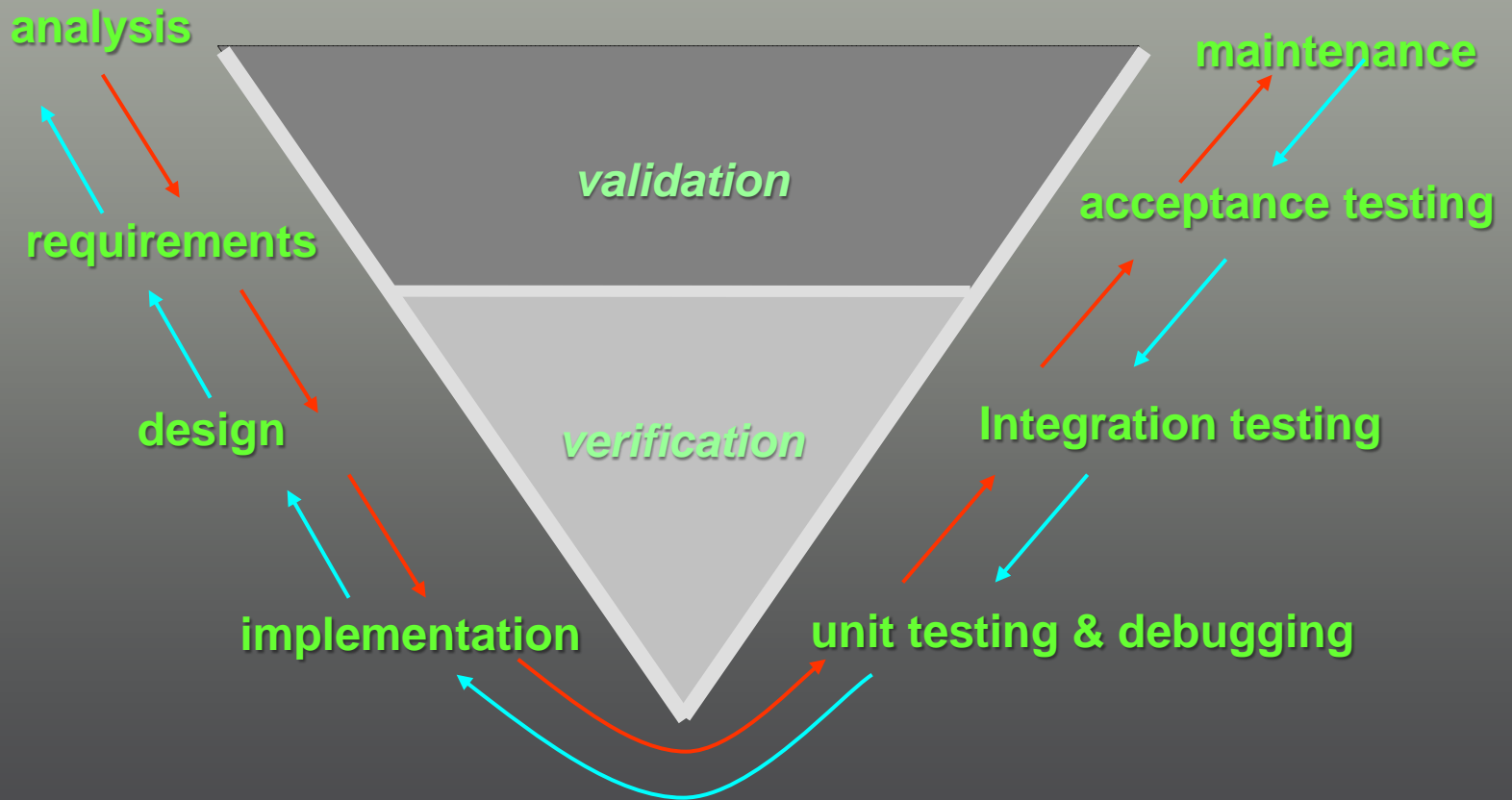
Systematic approach

- A. Product life-cycle vs. its testing cycle
- B. VVT processes
- C. Planning of VVT processes
- D. Static analysis techniques
- E. Error, program and runt-time environment models
- F. Black-box (functional) testing
- G. White-box (structural) testing



A. Product life-cycle vs. its testing cycle

Model "V"



Objectives

- Validation

Assess whether the system (or its component) meets its requirements specification

→ *Are we building the right product?*

Objectives

- Verification

Assess whether the product of a given phase meets the assumptions made at the beginning of this phase

→ *Are we building the product right?*

Objectives

- **Testing**

Analysis of the system behavior (or its component) in order to measure (assess) its quality

→ *How good is (or will be) the system?*

Example

- Object:

→ *A library routine for sorting matrices*

Example

- Object:

- *A library routine for sorting matrices*

- Testing

- *Does the object return a sorted matrix?*

Example

- Object:

- *A library routine for sorting matrices*

- Testing

- *Does the object return a sorted matrix?*

- Verification

- *Does the object sort matrices?*

Example

- Object:

- *A library routine for sorting matrices*

- Testing

- *Does the object return a sorted matrix?*

- Verification

- *Does the object sort matrices?*

- Validation

- *Can the procedure be included in the existing system library?*



Systematic approach

Systematic approach

bugs

Systematic approach

run-time environment
models

bugs

Systematic approach

run-time environment
models

program
models

bugs

Systematic approach

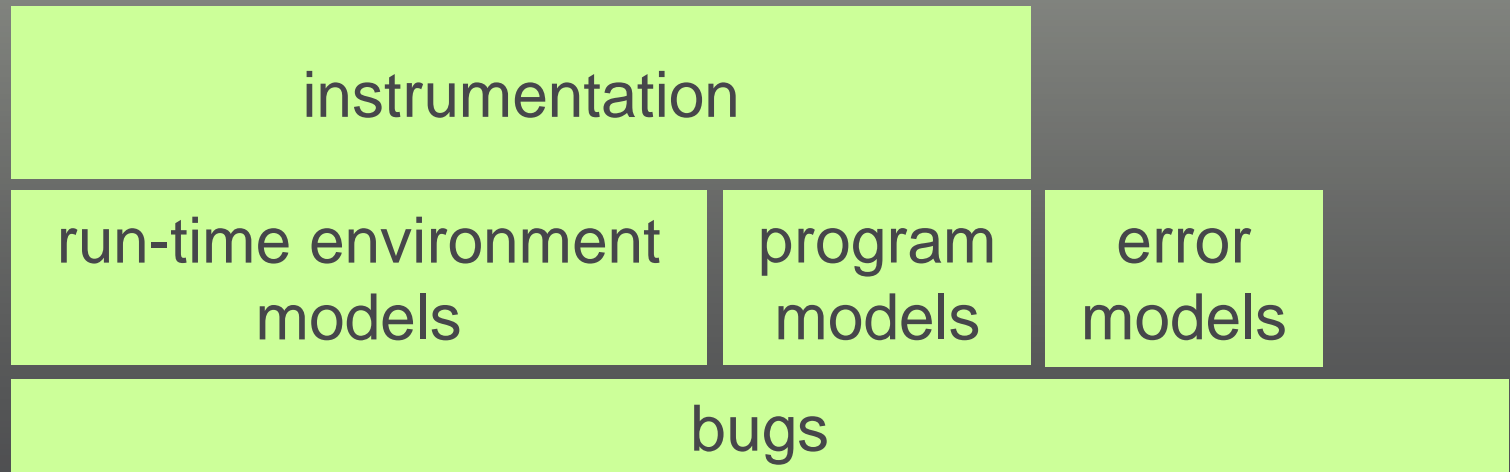
run-time environment
models

program
models

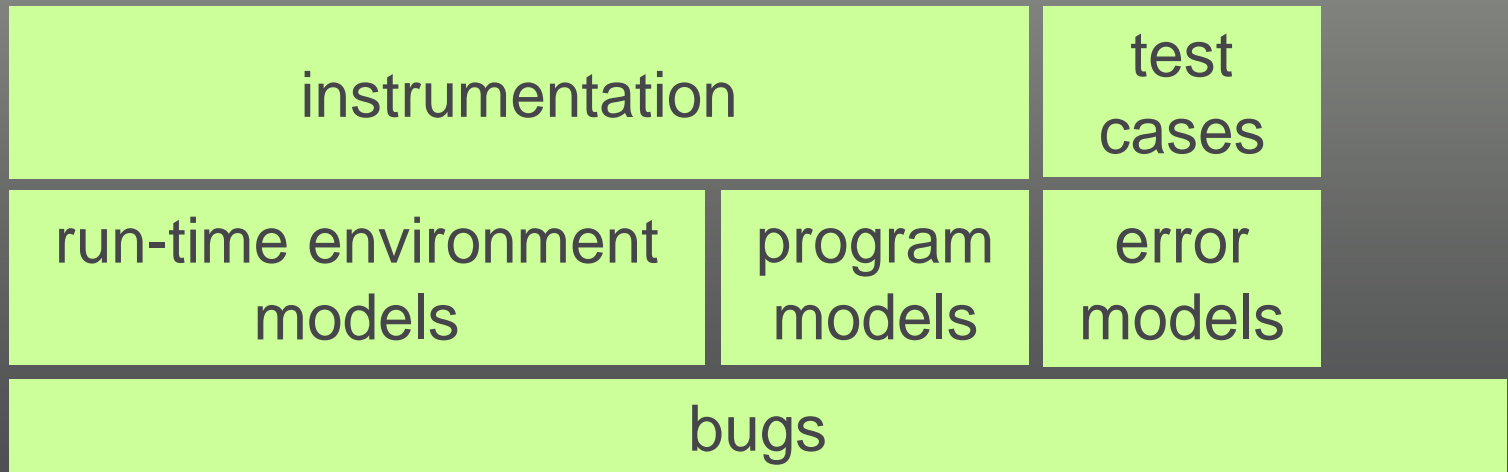
error
models

bugs

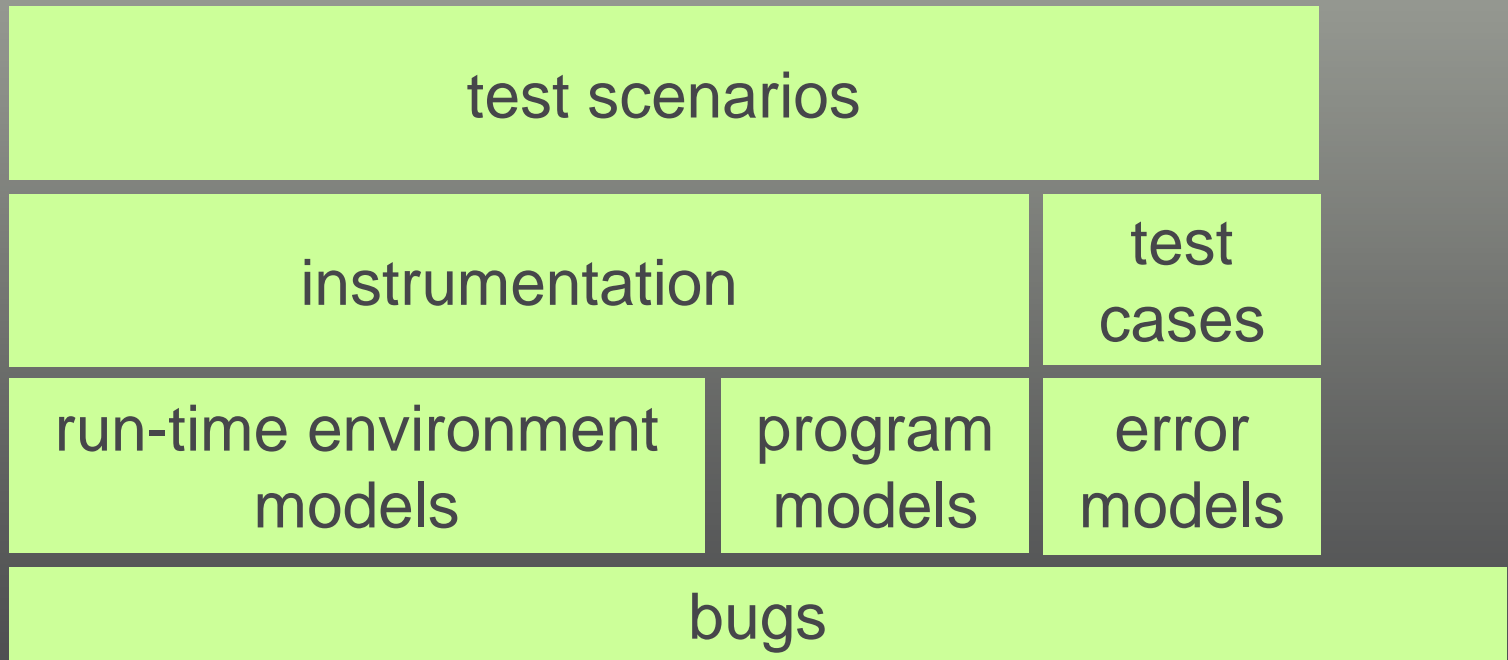
Systematic approach



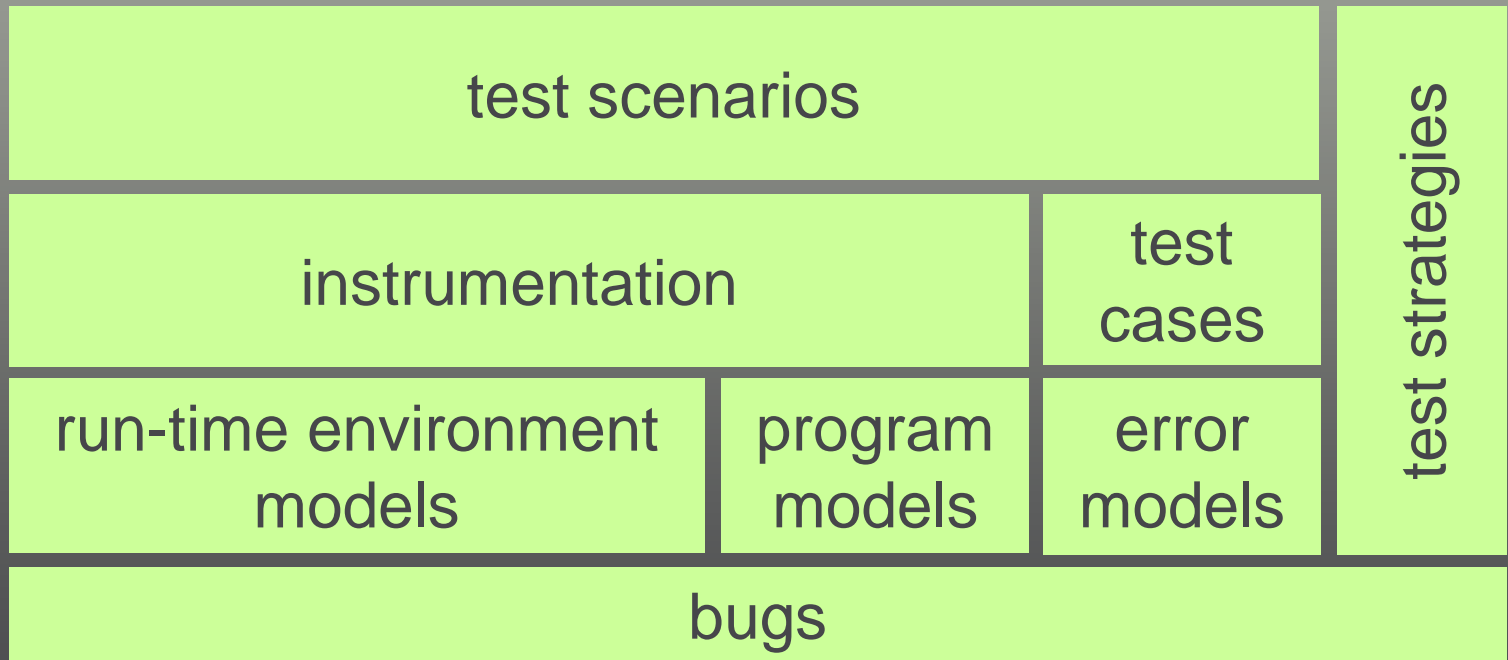
Systematic approach



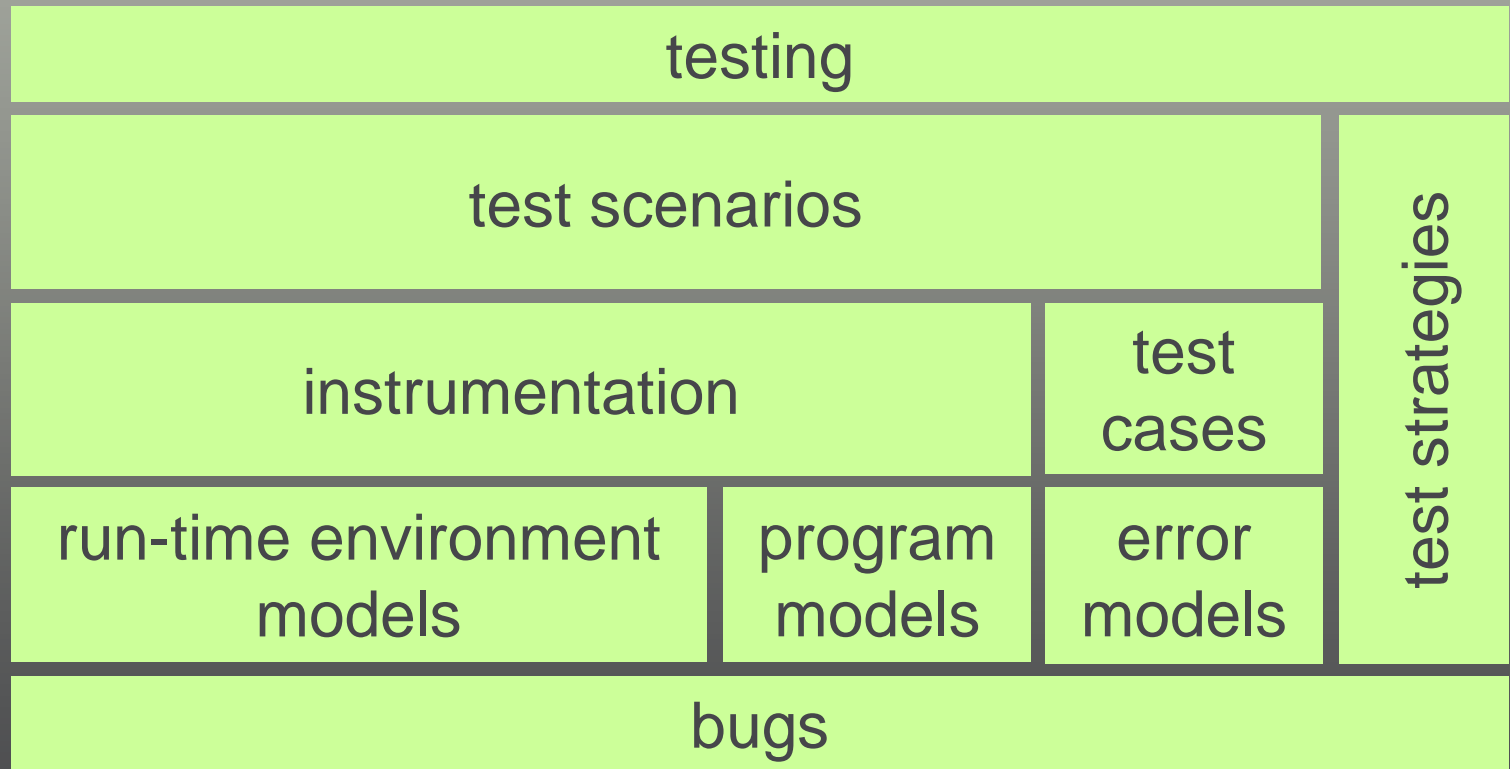
Systematic approach



Systematic approach



Systematic approach



Dynamic analysis

- Test case

A single element selected from an enumerable set of program behaviors

Dynamic analysis

- Test completion criterion

A set of test cases defined based on the program behavior model

Dynamic analysis

- Testing strategy

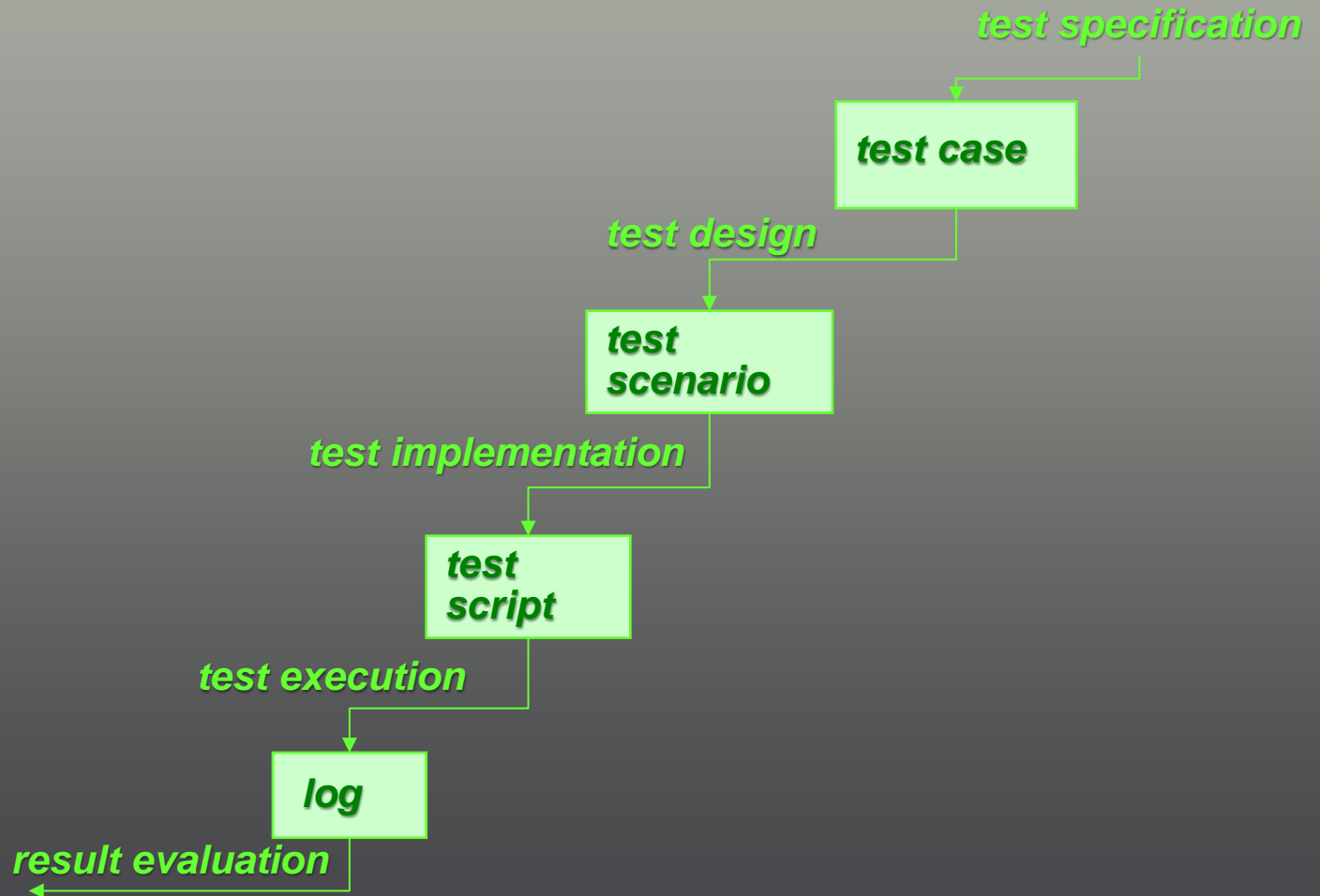
A set of rules for selecting test cases to a (possibly finite) set according to some adopted criterion

Dynamic analysis

- Test scenario

Systematic observation of the expected behavior of an IT product conducted in a supervised mode

Test case "life cycle"



Testing levels

- Unit/module testing
- Integration testing
- System testing
- Acceptance testing
- Alfa/Beta-testing

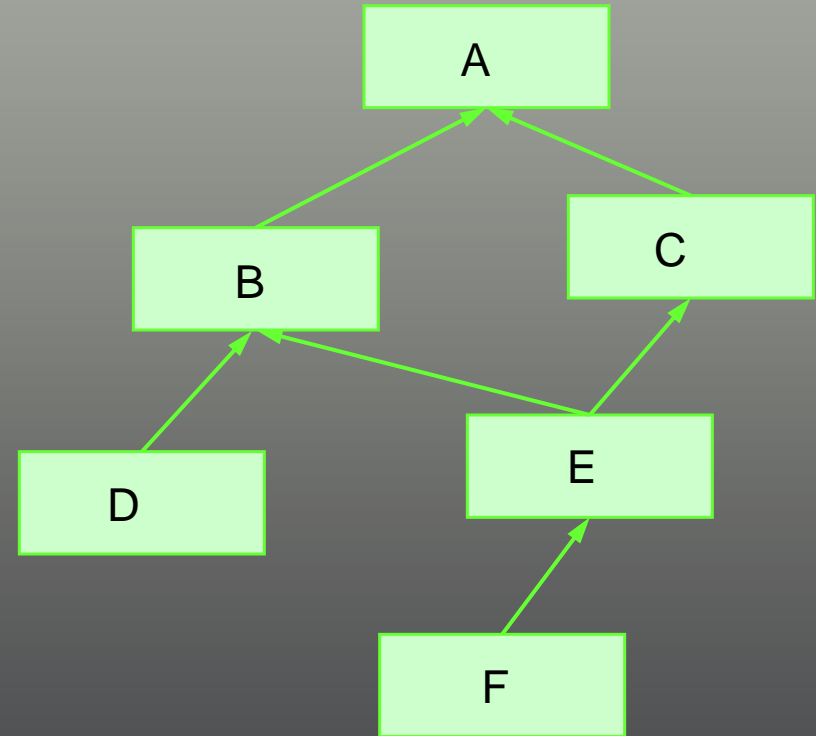


Unit testing

- Locating and removing errors
- Test completion
- Regression testing
- Test harness

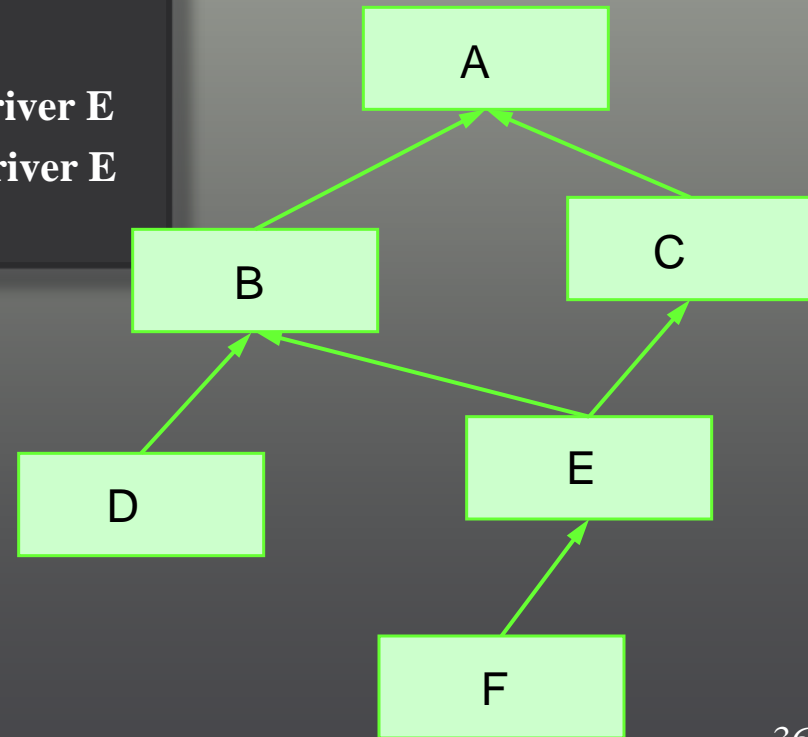
Integration testing

- **Strategies:**
 - incremental
 - big-bang



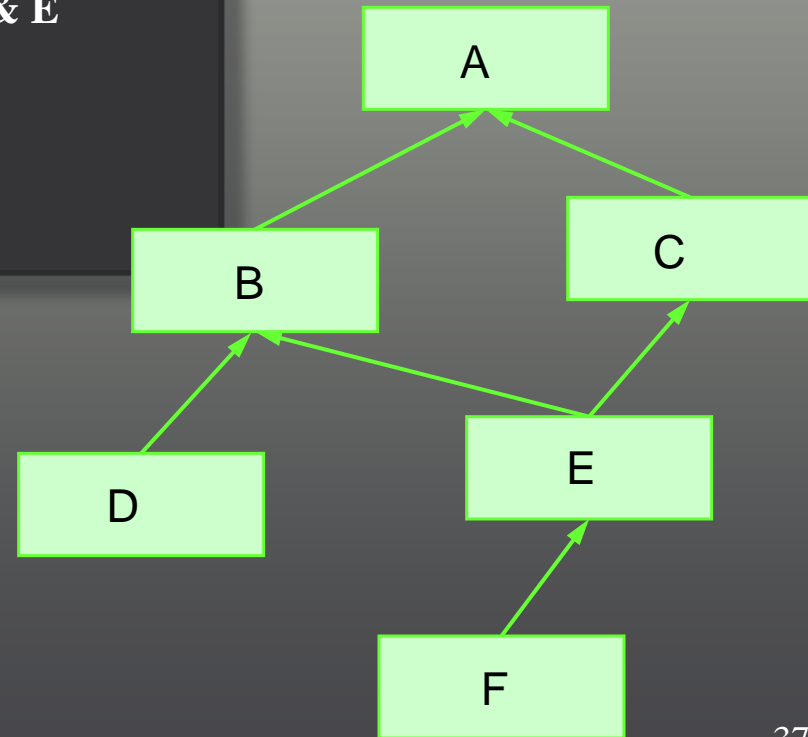
Bottom-up method

step	environment
1 unit D	driver D
2 unit F	driver F
3 connected units E+F	driver E
4 connected units D+E+F+B	driver B, driver E
5 connected units C+E+F	driver C, driver E
6 connected units A+B+C+D+E+F	--



Top-down method

step	environment
1 unit A	stubs B & C
2 connected units A+B	stubs C, D & E
3 connected units A+B+C	stubs D & E
4 connected units A+B+C+D	stub E
5 connected units A+B+C+D+E	stub F
6 connected units A+B+C+D+E+F	--



System testing

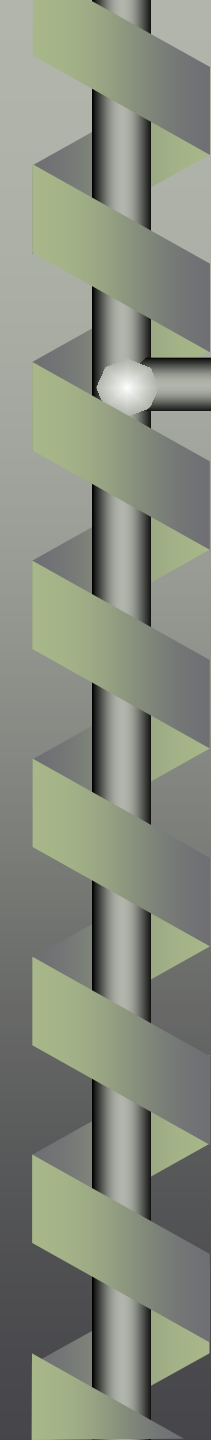
<i>category</i>	<i>features</i>	<i>systems</i>
functionality	every "what" the system does	dedicated systems
volume stress	voluminous input data input data of high intensity	file/Big Data systems RT (control) systems
usability	user-friendliness	system HCI
security	break-in attempts	secure systems
performance	system dynamics measurements	RT (control) systems
storage	memory use	memory critical systems
configuration	optional system configurations	S/H upgrades

System testing

<i>category</i>	<i>features</i>	<i>systems</i>
compatibility	older versions data	new releases
installability	installation procedures	complex installation
reliability	statistics (logs, incident	characteristics (MTTF, MTTR)
recovery	„destructive’ data	fault tolerant systems
serviceability	maintenance procedures	administered systems
documentation	useful in testing?	administered systems
procedure	required personnel activities	command/decision systems

Acceptance testing

- Ownership rights transferred from the developer to the client
- Demonstration that all acceptance criteria have been met
 - requirements specification
- Acceptance: phased, final
- “ α -testing”: customers test the product at the developer's facility (laboratory).
- “ β -testing”: customers test the product at their own facility (laboratory)

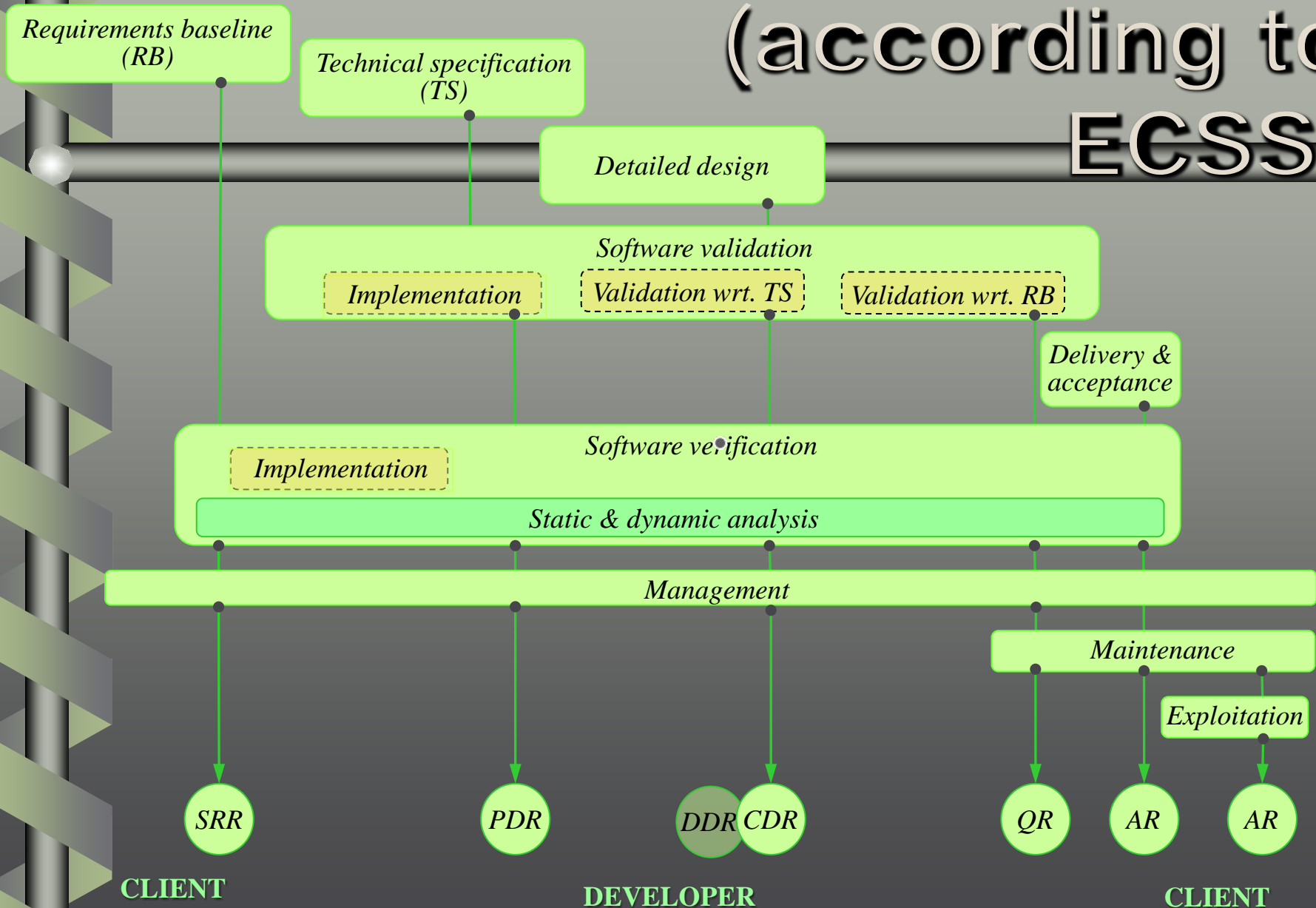
A decorative vertical bar on the left side of the slide, featuring a grey sphere at the top and a series of overlapping, semi-transparent green and grey rectangular bands that create a spiral or ribbon-like effect.

B. VVT processes: life-cycle validation, verification and testing

Responsibility, time schedule

- VVT processes:
 - early error detection
 - continuity of the development activities
 - better understanding of the product
 - decision criteria for the life-cycle phases

Life-cycle phases (according to ECSS)



Life-cycle processes (ECSS)

- Requirements baseline (RB)
 - functional and performance requirements for the planned software provided by the client
- Technical specification (TS)
 - a formal specification (logical model) of **what** the software is supposed to do,
 - physical design of the software structure mapping individual functions of the logical model to its components,
 - definition of control and data flows between them, the first part of the answer to the question of **how** the software is supposed to do something).

Life-cycle processes (ECSS)

- Detailed design
 - design of algorithms and data structures (physical model), the second part of the answer to the question of **how** the software is supposed to do something,
 - justification of **all** design decisions,
 - implementation of units (code writing/generation),
 - testing of code units to demonstrate their compliance with requirements.
- Software validation
 - Demonstrating that the system meets all assumed quality goals → **quality attributes**

Life-cycle processes (ECSS)

- Detailed design

- design of algorithms and data structures (physical model), the second part of the answer to the question of **how** the software is supposed to do something,
- justification of **all** design decisions,
- implementation of units (code writing/generation),
- testing of code units to demonstrate their compliance with requirements.

- Software validation

- Demonstrating that the system meets its goals → **quality attributes**

- Functionality
- Performance
- Dependability
- Security
- Usability

Life-cycle processes (ECSS)

- Detailed design

- design of algorithms and data structures (physical model), the second part of the answer to the question of **how** the software is supposed to do something,
- justification of **all** design decisions,
- implementation of units (code writing/generation),
- testing of code units to demonstrate their compliance with requirements.

- Software validation

- Demonstrating that the system meets its goals → **quality attributes**

RAMS:

- reliability,
- availability,
- maintainability
- safety

Life-cycle processes (ECSS)

- **Software verification**
 - confirm that for each activity (phase) of the life cycle there is an appropriate set of documents specifying the requirements for the product of a given phase,
 - demonstrate that the product of a given phase is correct and fully compliant with these requirements.
- **Implementation**
 - create code units (coding, adaptation, modification, automatic code generation),
 - integrate system units

Life-cycle processes (ECSS)

- **Maintenance**

- keep the system running after bug fixes, modifications, reinstallations, hardware replacements, etc.

- **Delivery and acceptance**

- Install the system in its target environment,
- Assess it formally based on the created documentation (RB & TS).

- **Exploitation**

- Provide support to the end system user (installation, ongoing administration, etc.).

Life-cycle processes (ECSS)

- **Management**

- project planning (activities, checkpoints, products, techniques and procedures),
- risk identification, countermeasure methods,
- principles of organizing and conducting reviews,
- management of configuration and information flow in the team, time, budget and risk
- ECSS management standards ('M' series):
 - ECSS-M-ST-10-01C – Organization and conduct of reviews
 - ECSS-M-ST-10C – Project planning and implementation
 - ECSS-M-ST-40C – Configuration and information management
 - ECSS-M-ST-60C – Cost and schedule management
 - ECSS-M-ST-80C – Risk management

Life-cycle milestones

- SRR - system requirements review:
 - The developer and client agree on the requirements baseline specification (is complete and consistent).
- PDR - preliminary design review:
 - The developer and client agree that the technical specification correctly reflects all basic requirements
- DDR - detailed design review:
 - Assessment of the possibility of moving to the next phase (all units designed correctly, realistic testing and integration plan, sufficient budget, unresolved issues addressed, existing software may be re-used)

Life-cycle milestones

- **CDR - critical design review:**
 - a key decision to continue or close the project
- **QR - qualification review:**
 - The tools are adequate and the product is mature enough (TRL-8) for acceptance.
- **AR - acceptance review:**
 - all required test cases performed and completed correctly by a given software version in its target environment,
 - final approval of the product.

Product maturity

- Technology readiness levels (NASA):

TRL 9

• Actual system “flight proven” through successful mission operations

TRL 8

• Actual system completed and “flight qualified” through test and demonstration (ground or space)

TRL 7

• System prototype demonstration in a space environment

TRL 6

• System/subsystem model or prototype demonstration in a relevant environment (ground or space)

TRL 5

• Component and/or breadboard validation in relevant environment

TRL 4

• Component and/or breadboard validation in laboratory environment

TRL 3

• Analytical and experimental critical function and/or characteristic proof-of-concept

TRL 2

• Technology concept and/or application formulated

TRL 1

• Basic principles observed and reported

Quality attributes of a critical software system

- Basic (ECSS standard definitions):
 - reliability
absence of errors that prevent the system from properly performing all functions required in its RB
 - safety
no threat to its environment (people, environment, property and infrastructure)
 - maintainability
can always be brought to a state in which any required function will be performed properly
 - security
correctly and completely achieves only the goals consistent with the owner's intentions

Quality attributes of a critical software system

- Complex (ECSS standard definitions):
 - availability
System is capable of performing the required function at a given moment or time interval
 - dependability
Ability to build trust in the quality of system services in the long term
- RAMS characteristics
 - **reliable + available + maintainable + safe**

Classification of critical systems

- Severity number (SN):

Effect	SN	Dependability	Safety
Catastrophic	1	Progressive break-down (propagation of a series of failures)	Loss of life, health or permanent disability of crew members or ground staff
			Loss of the system
			Permanent loss of connection to the manned flight control system
			Destruction of the launch pad
			Serious damage to the natural environment

Classification of critical systems

- Severity number (SN):

Effect	SN	Dependability	Safety
Critical	2	Mission loss	Temporary inability to perform certain activities or illness of crew or ground staff
			Serious damage to the link to the manned flight control system
			Serious damage to ground infrastructure
			Significant damage to private or public property
			Other environmental damage

Classification of critical systems

- Severity number (SN):

Effect	SN	Dependability	Safety
Significant	3	Significant threat to the mission	Mission dependent
Negligible	4	Minor threat to the mission	Mission dependent

Classification of critical systems

- Non-execution or incorrect execution of the code and other anomalies in its operation cause the system to fail with the following consequences:
 - catastrophic (category 'A')
 - critical (category 'B')
 - significant (category 'C')
 - negligible (category 'D')



C. Planning of VVT processes

Verification process

- Verification of the Requirements Baseline (RB) document by **recipients** (to do list):
 - Comprehensive description of the operating (target) environment
 - Characteristics of the system and devices
 - Key points where to control the system and observe its operation
 - Possible system malfunctions and ways to eliminate their effects
 - Specification of the initial system settings
 - Specification of user scenarios

Verification process

- Verification of the Technical Specification (TS) document by **recipients** (to do list):
 - System hardware and software requirements are consistent
 - Software requirements are verifiable
 - System architecture is feasible
 - All hardware and software implementation limits have been identified
 - An appropriate verification method is defined for each requirement

Verification process

- Verification of the system architecture design by **developers** (to do list):
 - System architecture design accurately reflects the requirements
 - Detailed system design is implementable
 - all dynamic aspects of system operation are correctly considered (processes/threads, their priorities, synchronization mechanisms, resource sharing management)

Verification process

- Verification of the system detailed design by **developers** (to do list):
 - Is correct, internally consistent and clearly follows the system architecture design
 - Is testable:
 - *data entry points and triggers, measurement data collection points*
 - *temporary and invariant values in key places of the system structure*
 - *fault injection possible*
 - ability to perform maintenance and operational activities
 - all dynamic aspects of system operation are correctly considered (processes/threads, their priorities, synchronization mechanisms, resource sharing management)

Verification process

- System code verification by **developers** (to do list):
 - its structure and content consistent with requirements (TS, RB), architecture and detailed design
 - is correct, testable and compliant with established coding standards
 - all possible consequences of run-time errors are under control of the code
 - there are no memory leaks
 - 100% code execution coverage for assignment and conditional statements in the event of possible catastrophic (category 'A') or critical (category 'B') consequences

Verification process

- Verification of the unit testing plan and results by **developers** (to do list):
 - unit tests are consistent with the system design and requirements documents
 - Each unit test ensures examining (at least):
 - *execution of each conditional code statement (while, for, if) for the limit values of its predicate*
 - *access (read or write) to each global variable*
 - *input data outside of their valid ranges, causing incorrect function computations*
 - *high volume/intensity data inputs to test the unit's performance limits as specified in the requirements*
 - all results obtained are as expected and the completion criteria for each test have been met
 - all unexpected results and anomalies of each tested unit are documented in the report.

Verification process

- Verification of the system integration by **developers** (to do list):
 - consistency with the system architecture design document
 - testing objectives for system interfaces (adequate and complete list)
 - obtained results obtained are consistent with the expected ones

Verification process

- Verification of the system validation process by **developers** wrt RB and TS documents (to do list):
 - results of the validation process were obtained based on test cases, test procedures, inspections and design reviews covering the entire scope of requirements included in TS/RB documents
 - all obtained results of the validation process are consistent with the expected ones

Verification process

- Verification of the system documentation by **developers** (to do list):
 - the content of the documentation is adequate, complete and consistent
 - all documents are prepared within the deadlines set up in the project time schedule
 - management of the process of creating/merging documents follows the previously defined procedures

Verification process

- Hard real-time system analysis:
 1. the system is predictable, all worst case scenario events are handled within the required time limits (TS, RB)
 - *an adequate analytical model was used,*
 - *alternatively (if not possible) valid simulation experiments were carried out*
 - *feasibility of the architectural structure design demonstrated*
 2. time analyzes were updated at the detailed construction stage...
 3. ... and (again) repeatedly, during code verification, unit testing, and integration phases (based on information collected during dynamic analysis of the target system code).

Validation process

- TS validation activities:
 - Test specification (test cases)
 - ✓ *for each requirement of each code unit (input data, expected results, test completion criteria)*
 - Test design (test scenarios)
 - ✓ *volume and stress tests, data limit and/or special values*
 - ✓ *testing the system ability to isolate or reduce the effects of errors (soft-fail systems, fault tolerant systems, interactive systems)*
 - ✓ *correct operation in various valid configurations of the target environment (supervised mode)*
 - ✓ *data interfaces (protocols, data ranges, time dependencies)*
 - ✓ *user interfaces (average user error rate, average time to learn)*

Validation process

- RB validation activities:
 - Test specification (test cases)
 - ✓ *for each single requirement - the mission's intended inputs, expected results, and acceptance criteria*
 - Test design (test scenarios)
 - ✓ *volume and stress tests, data limit and/or special values*
 - ✓ *testing the system ability to isolate or reduce the effects of errors (soft-fail systems, fault tolerant systems, interactive systems)*
 - ✓ *correct operation in various valid configurations of the target environment (random mode)*
 - ✓ *data interfaces (protocols, data ranges, time dependencies)*
 - ✓ *user interfaces (average user error rate, average time to learn)*

Delivery and installation process

- **Activities:**
 - Installation in the target environment
 - ✓ *installation plan and installation procedures development*
 - ✓ *testing of installation procedures (installed code, databases and services can be properly activated to function and close afterwards)*
 - ✓ *conducting introductory training for the end user staff (or even cyclic if requested in RB)*
 - ✓ *providing resources and information necessary to carry out the installation*
 - ✓ *testing the system ability to isolate or reduce the effects of errors (soft-fail systems, fault tolerant systems, interactive systems)*
 - ✓ *documenting all relevant events (incidents) during installation*

Acceptance process

- **Activities:**
 - the recipient (client) prepares the acceptance testing plan
 - the recipient performs all tests specified in the acceptance testing plan
 - ✓ *the tests must include generation of any executable code from the source code (!)*
 - ✓ *evaluation of all obtained test results must refer to RB*
 - developer and recipient perform a formal acceptance review
 - ✓ *after completion of the software delivery, installation and acceptance processes*

Experiment management

1. Quality objectives

- compliance with functional specifications, performance characteristics, code characteristics (Halstead. McCabe), test completion degree, etc.,

2. Anticipated problems

- description of properties and how they could occur

3. Testing strategies

- capable of detecting anticipated problems should affect their definition
- project plan, Pareto effect

Experiment management

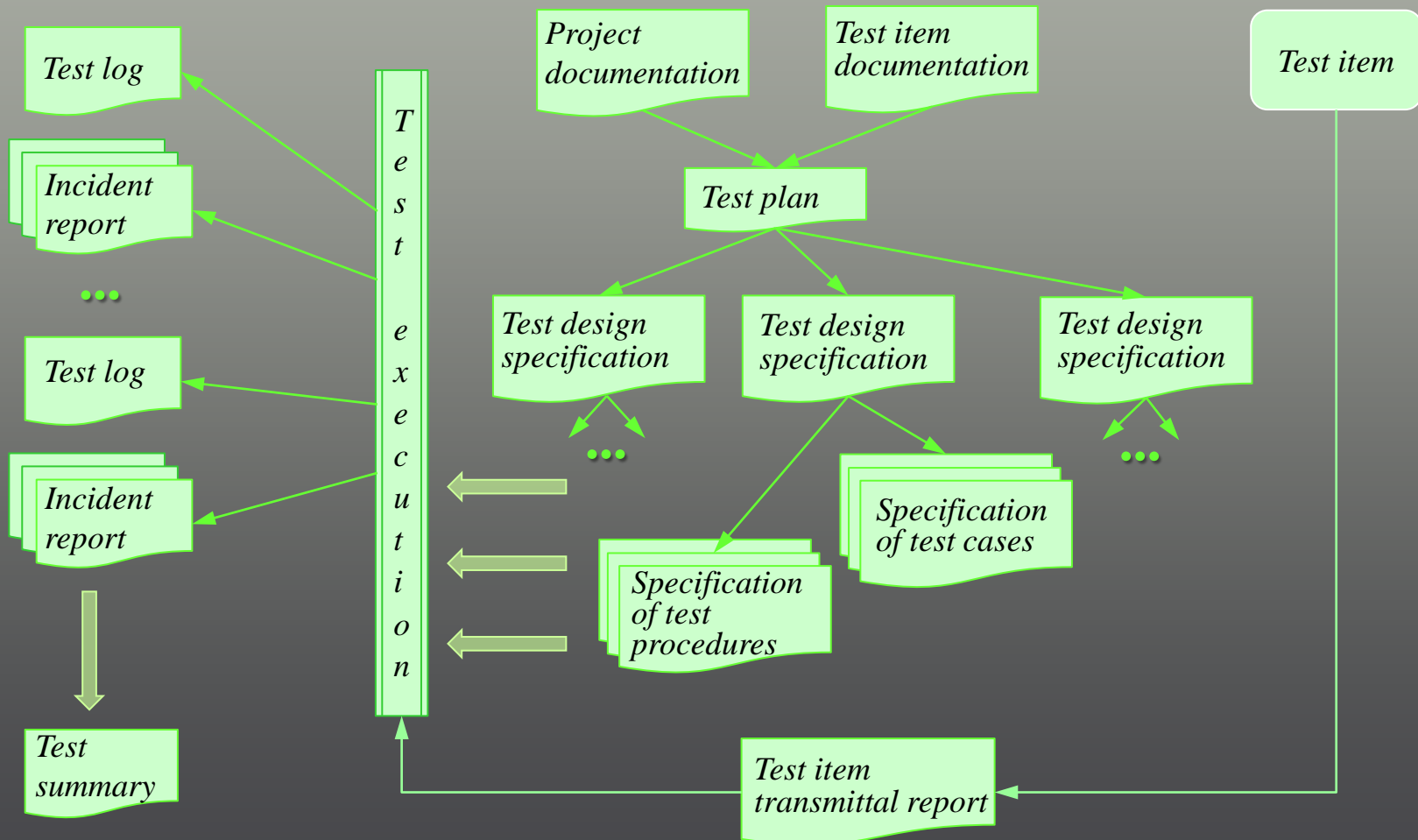
4. Product delivery

- incremental integration with ongoing analysis/testing, monitoring trends of detected anomalies

5. Change management, staff training, tools

- project plan, Pareto effect

Test documentation (IEEE std.)



Permanent (static) part of test documentation

- Test plan
 - Time schedule, milestones/checkpoints, management rules
- Test design specification
 - Rationale, explanation and justification of test cases structure
- Specification of test cases
 - Input data and expected results, entry and exit conditions, events and expected reaction

Permanent (static) part of test documentation

- Specification of test procedures
 - how to perform experiments and measure their advance
- Test completion criteria
 - Conditions to be met by each test procedure
- Test item transmittal report
 - method of delivery and format of items to be tested

Variable (dynamic) part of test documentation

- Test log
 - recorded activities and data
- Incident report
 - list of incidents requiring further investigation
- Test summary
 - decision of the project management staff and conclusions

Test procedures

- Disposition of test items
- Exceptional situations
- Experiment costs
- Acceptance criteria

Disposition of test items

- Item identifier
- Item:
 - version, documentation, responsible person
- Method of delivery:
 - localization, medium
- Status:
 - deviations from documentation, previous version and/or plan, any modifications in progress
- Authorization:
 - person approving disposition

Exceptional situations

- Any incident during the experiment requiring explanation:
 - input data, expected results, observed anomalies, date and time, step in the scenario, state of the environment, repetition attempts, people performing the test, witnesses
- Determining consequences wrt:
 - continuation of the test plan, test design, scenarios, etc.



D. Static analysis techniques

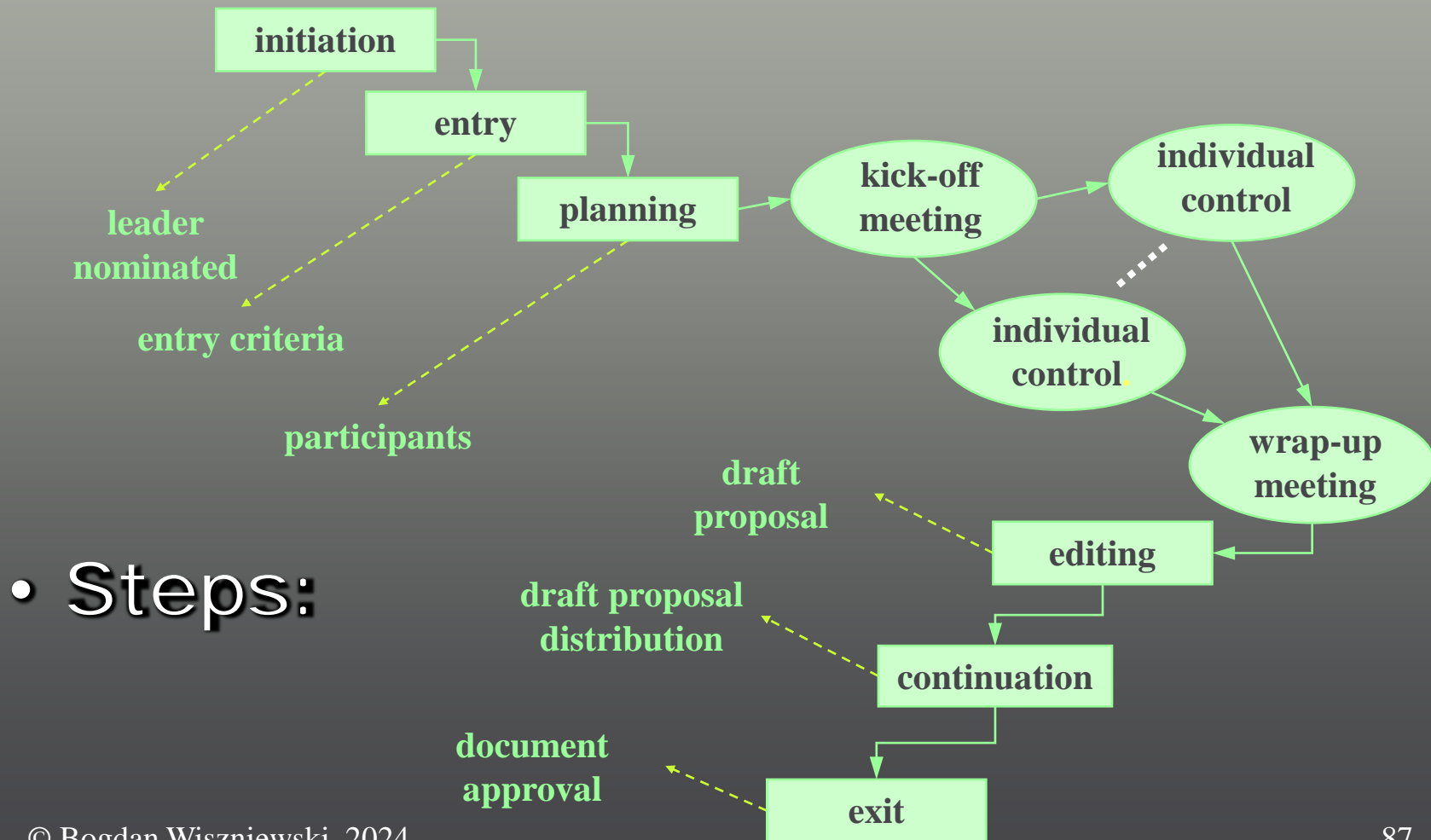
Software inspections

- Visually inspect the code or design of a system component to detect:
 - errors,
 - deviations from project standards,
 - missing or incorrect comments,
 - potential portability problems,
 - other problems not "machine checkable"

Software inspections

- Inspection is not a part of the design process:
 - decisions are not made, focus on individual issues only, does not suggest changes or corrections, **but**
 - allows to detect, identify and remove defects and formally confirm product quality

Software inspections



Software inspections

- Inspection team members (roles)
 - **Author:** *created the work product being inspected.*
 - **Moderator (leader):** *plans the inspection and coordinates it.*
 - **Inspector:** *examines the work product to identify possible defects.*
 - **Reader:** *reads through the documents, one item at a time. The other inspectors then point out defects.*
 - **Recorder/Scribe:** *documents the defects that are found during the inspection.*

Reviews

- Developer (programmer) leads the team through a selected fragment of code
- The team asks questions and comments on potential errors

(!) a narrow and highly interactive technique

Software audits

- Assessing software processes and products for compliance with requirements, standards, and contractual agreements;
- Ensuring software quality, accuracy, and functionality while reducing legal risks and optimizing performance efficiency;
- Strictly defined criteria and goal, independent assessment team

Software audits

- Types:
 - **Technical audit:** the software is developed with respect to industry standards.
 - **Security audit:** the software can protect sensitive information.
 - **Usability and accessibility audit (UX audit):** there are no issues with User Experience in the already-deployed software.

Identification of critical elements

- Failure Mode and Criticality/Element Analysis (FMECA/FMEA)
 - NASA since the 1960s, currently the space, aviation, nuclear and automotive industries
 - ECSS standard, ISO 9000 norm
 - analysis of the effects of **defects** revealing individually in the **products** of the architectural/detailed design phases, production phases (coding, testing, integration) as well as flaws of the **production process** itself
 - most (>80%) defects are detected in the production phase

Failure mode and effects analysis (FMEA)

- Steps:

1. Identification of system elements and activities of the production process
2. List all potential product defects and errors in the activities of individual phases of the production process
3. List all probable consequences of the potential defects and errors
4. List possible causes of the identified defects and errors
5. Analyze all identified defects to :
 - a. assess the materialization of risks
 - b. planning risk mitigation
6. Implementation of preventive actions and monitoring their effectiveness.

Failure mode and effects analysis (FMEA)

- Criticality (CN) is the combination of end effect probability (PN) and severity (SN), $CN = SN \times PN$
 - **Criticality number (CN)** to rank the risk level;
 - **Severity number (SN)** to rank severity for the worst-case scenario adverse end effect or state, e.g. catastrophic (4), critical (3), significant (2), negligible (1);
 - **Probability number (PN)** to classify of the ranges of probabilities of propagation of the effects of revealing a defect beyond the analyzed system unit, e.g.

Level	Range	PN
High	$P > 10^{-1}$	4
Moderate	$10^{-3} < P \leq 10^{-1}$	3
Low	$10^{-5} < P \leq 10^{-3}$	2
Negligible	$P \leq 10^{-5}$	1

Analysis of critical system elements

- Identification of critical elements:

Effect	SN	Probability levels			
		10^{-5}	10^{-3}	10^{-1}	1
		PN			
		1	2	3	4
Catastrophic	4	4	8	12	16
Critical	3	3	6	9	12
Significant	2	2	4	6	8
Negligible	1	1	2	3	4

- the analyzed unit is critical when:

can always lead to a system catastrophic failure regardless of the defect propagation probability level or its index $CN \geq 6$



E. Models for dynamic analysis:

- error,
- program,
- environment

Where do errors come from?

- The error concept
- Error detection
- Characteristics of code objects under test
- Sources of errors

The concept of a program error

- **Program error**
 - an event initiated by a user or the program environment,
 - the program code produces an unexpected result
- **Program failure**
 - the program crashes
 - the program is unable to perform some of its functions correctly

Error detection

- Proof of correctness:

Objective: *to prove that the program is free of errors (is correct)*

Environment: *axiomatic*

Reasoning: *deduction*

Error detection

- Testing:

Objective:

*to demonstrate
that the program
has errors*

Environment:

testing or target

Reasoning:

inductive

Error detection

- Performance testing:

Objective: *measure physical parameters*

Environment: *testing or target*

Reasoning: *metrics, characteristics*

Characteristics of code objects

- **Linguistic metrics:**
 - Lines of code (LOC),
 - Statement count (SC),
 - Halstead's metrics.
- **Structural metrics:**
 - Cyclomatic complexity (McCabe)
- **Functional metrics:**
 - Computational complexity (time, memory)

Halstead's metrics

- Program length

$$N_{lok} = N_1 + N_2$$

- Estimated program length

$$HLOC = n_1 \cdot \log_2 n_1 + n_2 \cdot \log_2 n_2$$

N_1 operators, N_2 operands

n_1 unique operators, n_2 unique operands

Halstead's metrics

- Program volume

$$VOLM = (N_1 + N_2) \cdot \log_2(n_1 + n_2)$$

- Estimated number of errors

$$B = (N_1 + N_2) \cdot \log_2(n_1 + n_2) / 3000$$

N_1 operators, N_2 operands

n_1 unique operators, n_2 unique operands

Structural metrics

- Cyclomatic complexity (McCabe):

$$M = L - N + 2P$$

Number of edges (L),

Number of nodes (N),

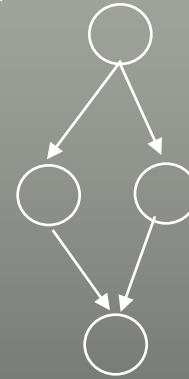
Number of connected components (P)

The maximum number of linear, independent paths through a program

Cyclomatic complexity



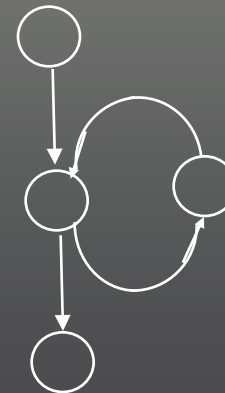
$$L = 2, N = 3, P = 1$$
$$M = 2 - 3 + 2 = 1$$



$$L = 4, N = 4, P = 1$$
$$M = 4 - 4 + 2 = 2$$



$$L = 4, N = 3, P = 1$$
$$M = 4 - 3 + 2 = 3$$



$$L = 4, N = 4, P = 1$$
$$M = 4 - 4 + 2 = 2$$

Cyclomatic complexity

- Text (decision instructions) and detailed design
→ Missing or redundant path
- Number of (paths) test cases $\geq M$
(!) Control flow direction is not taken into account, e.g. $M(\text{if-then-else}) = M(\text{while-do})$
- Ignore language (syntax) complexity

Functional metrics

- Complexity level (algorithms):

<i>Symbol</i>	<i>Complexity</i>	<i>Example</i>
$\Theta(1)$	constant	hash tables
$\Theta(\log n)$	logarithmic	binary search
$\Theta(n)$	linear	GCD of n-digit numbers
$\Theta(n \log n)$	linearithmic	Fast Fourier Transform (DFT)
$\Theta(n^c)$	polynomial	path tracking (robots)
$\Theta(c^n)$	exponential	generation of prime numbers

Sources of errors

- Requirements specification:
 - completeness
 - consistency

Sources of errors

- Design:
 - correctness
 - testability

Sources of errors

- Coding ("translation" of an algorithm into some program code):
 - textual (typos, omissions, etc.)
 - misunderstanding semantics of the implementation language,
 - not understanding semantics of the algorithm,
 - not understanding (knowing) the requirements.

Models

- Program:
 - Control flow,
 - Events,
 - Data flow,
 - State transitions

Models

- **Error:**
 - Control flow errors
 - Data flow errors
 - State errors
 - Text anomalies

Models

- Run-time environment:
 - Sequential (stream) processing
 - Event driven sequential processing
 - Concurrent processing
 - Parallel processing
 - Distributed processing

Example

```
public class Buffer {
int N = 10; //total buffer capacity
ipt = 0; //input index
opt = 0; //output index
len = 0; //current buffer load

/** shared resource */
char *pool = new char[N];

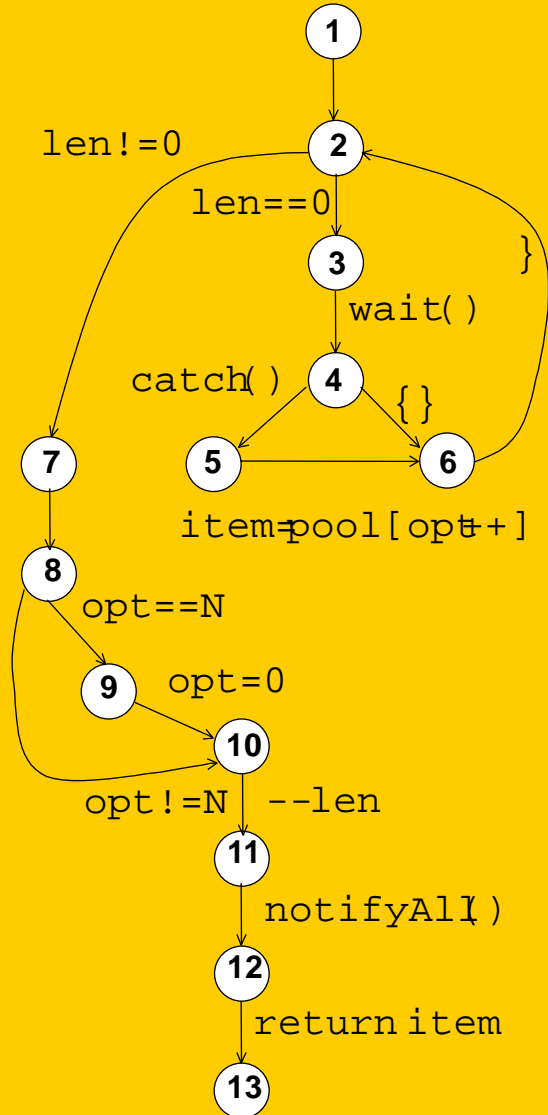
/** consumer */
/* 1 */ public synchronized char get(){
    char item;
/* 2 */ while (len == 0){
/* 3 */     try {wait(); //buffer is empty
/* 4 */     }catch(InterruptedException){
/* 5 */     }
/* 6 */ } //semaphore opened
/* 7 */ item = pool[opt++];
/* 8 */ if (opt == N)
/* 9 */     opt = 0; //modulo N
/*10 */ --len; //one element taken
/*11 */ notifyAll(); //buffer is not full
/*12 */ return item;
/*13 */ }

/** producer */
/* 1 */ public synchronized void put(char item){
/* 2 */ while (len == N){
/* 3 */     try {wait(); //buffer full
/* 4 */     }catch(InterruptedException){
/* 5 */     }
/* 6 */ } //semaphore opened
/* 7 */ pool[++ipt] = item;
/* 8 */ if (ipt == N)
/* 9 */     ipt=0; // modulo N
/*10 */ ++len; // one element added
/*11 */ notifyAll(); //buffer is not empty
/*12 */ }
}
```

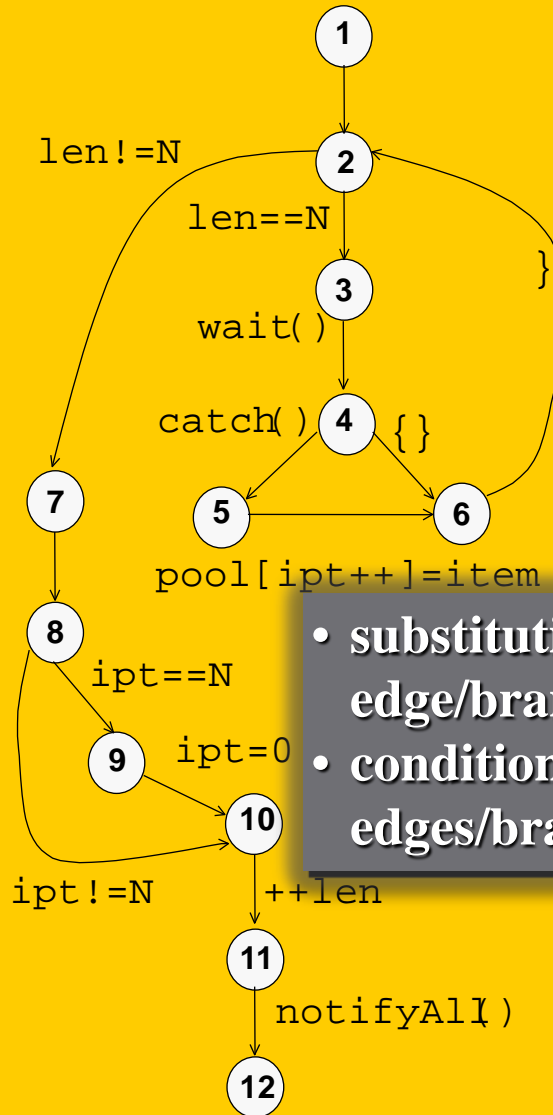
- Shared table `pool` with `N` elements
- Method `Buffer.get()` to fetch one character
- Method `Buffer.put()` to insert one character

Control flow

Buffer.get()



Buffer.put()



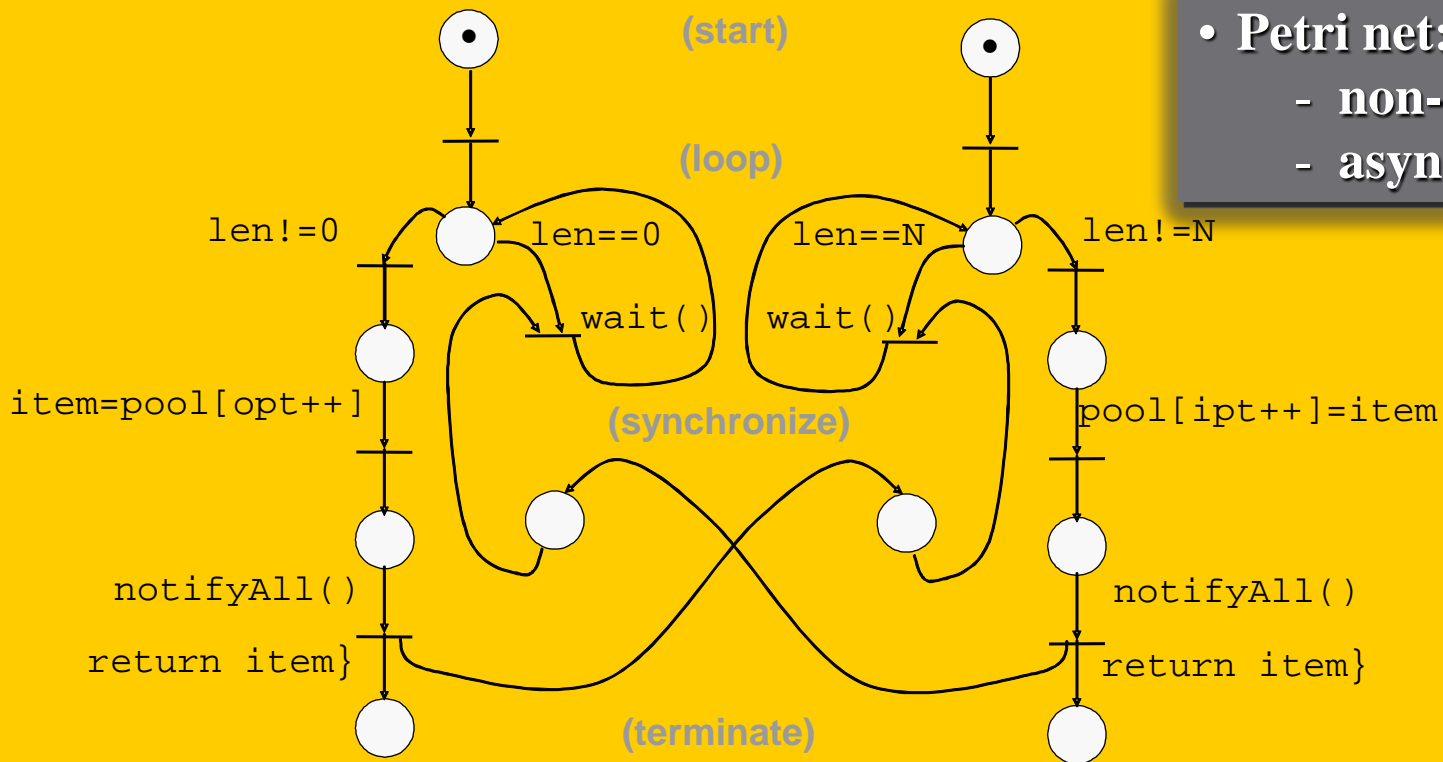
- substitution (none or one outgoing edge/branch)
- conditional (two or more outgoing edges/branches)

Events

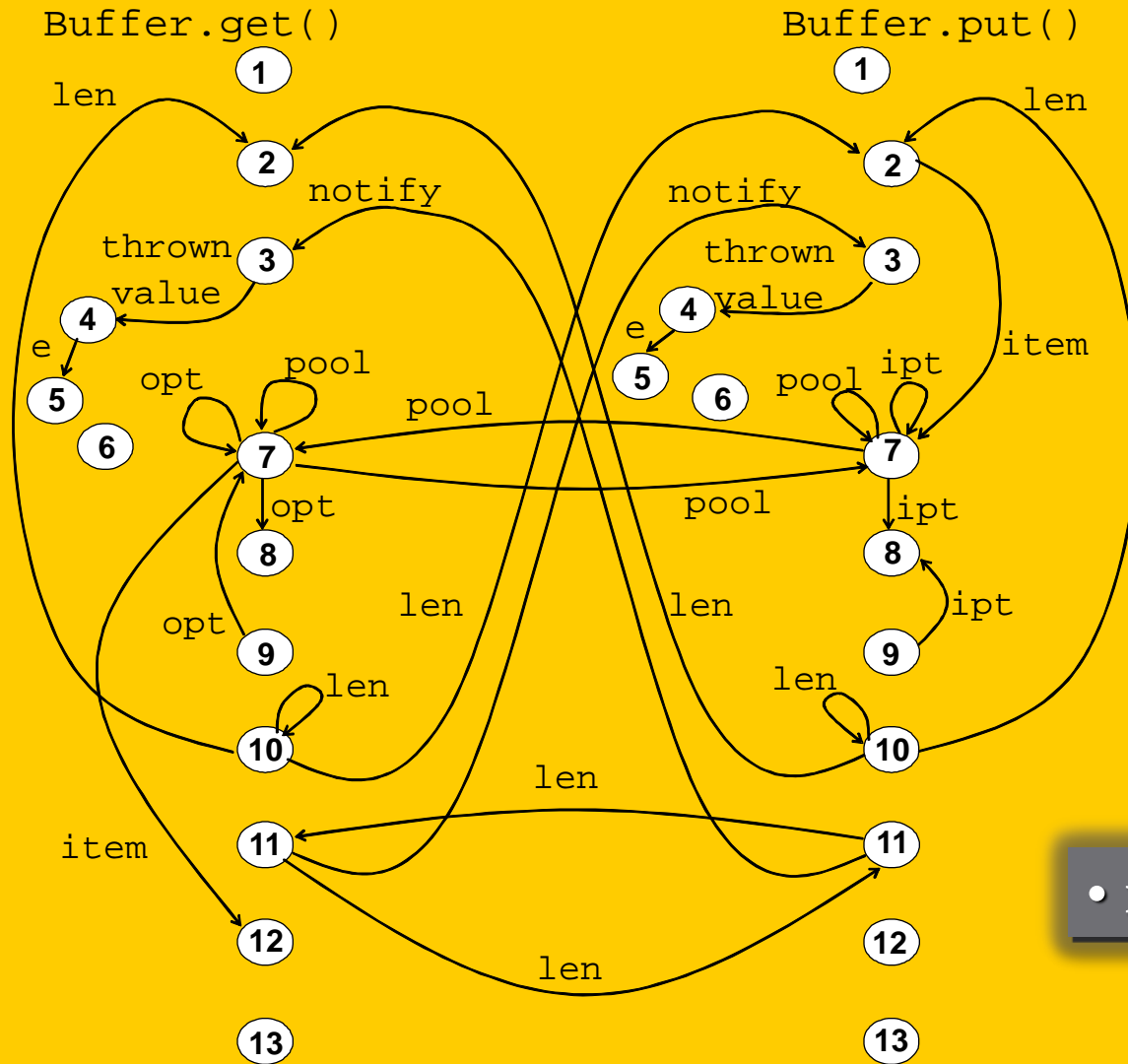
Buffer.get()

Buffer.put()

- Petri net:
 - non-determinism
 - asynchronism



Data flow

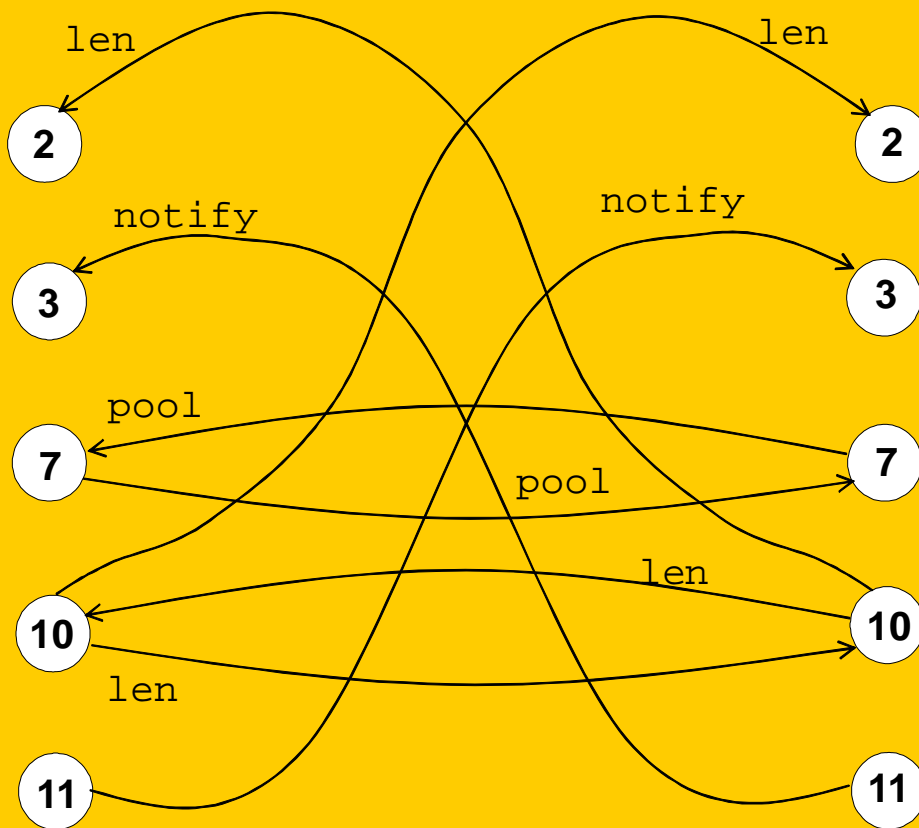


• instruction level

Data flow

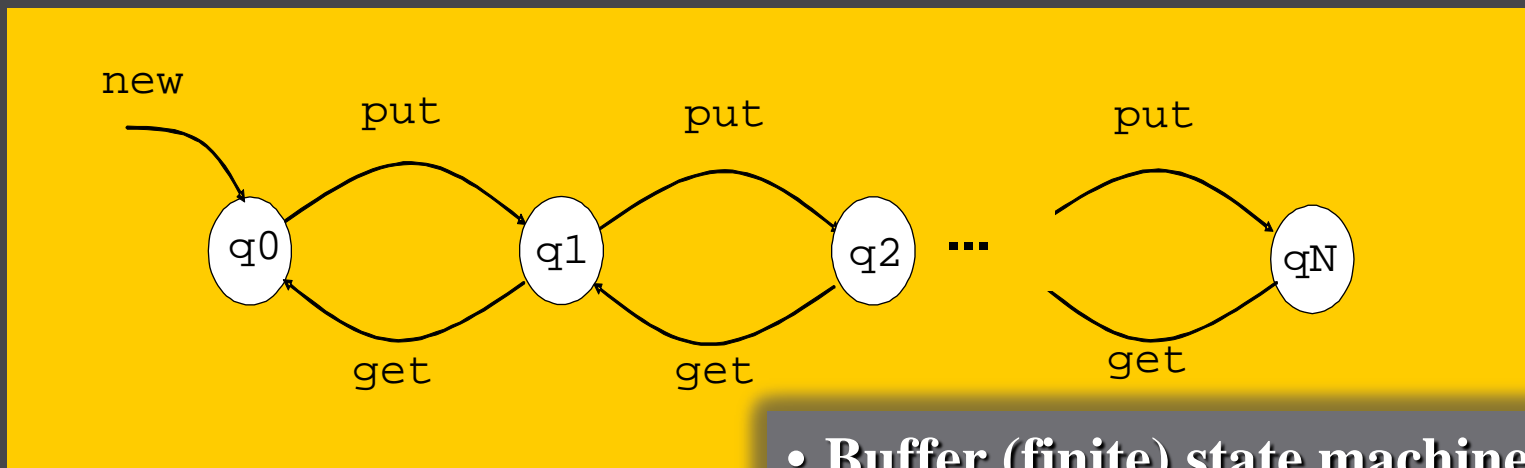
Buffer.get()

Buffer.put()

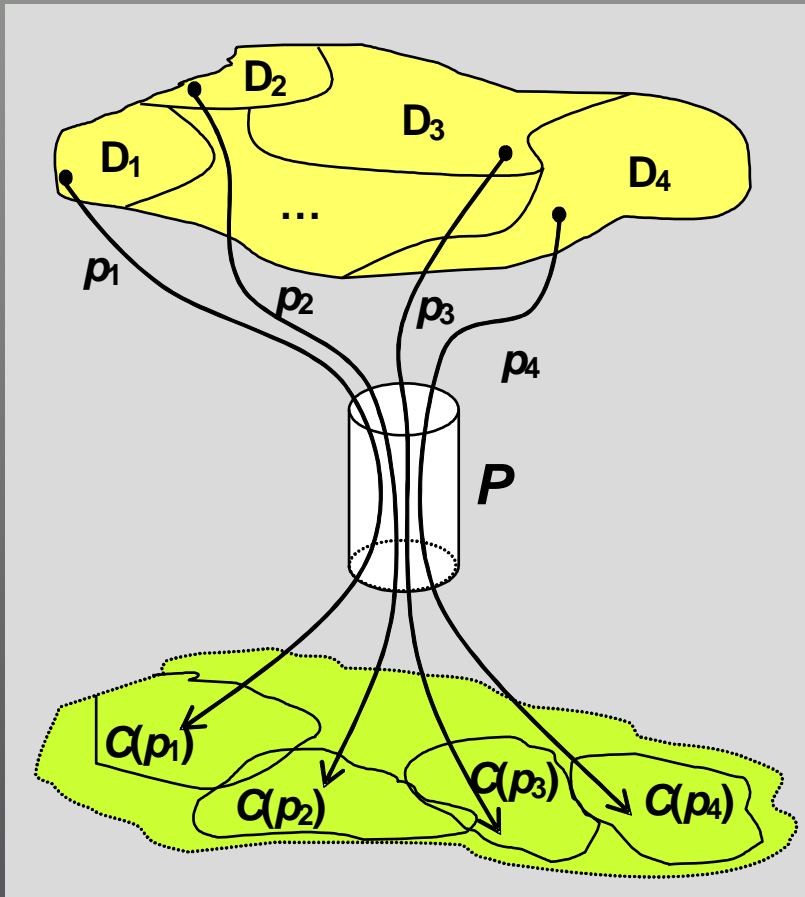


- communication level (threads)

State transitions



Control flow errors



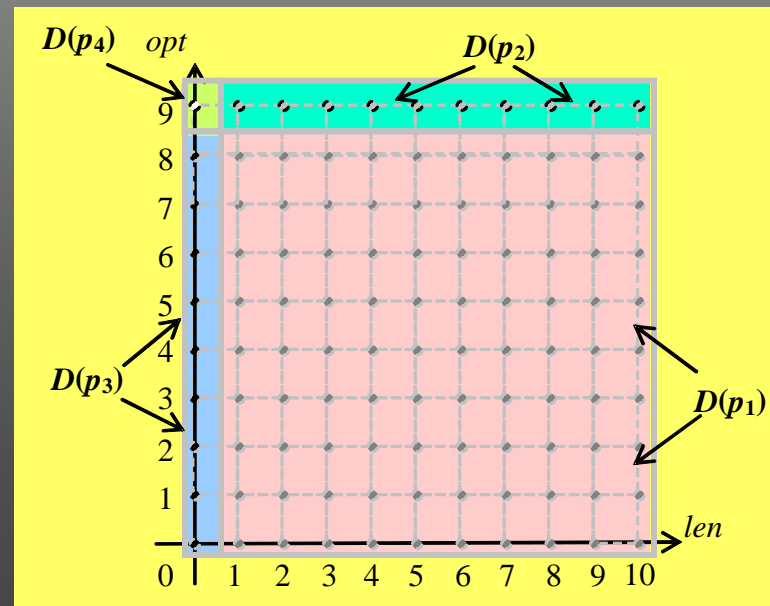
Path (execution) conditions:

$$p_1(\bar{x}) = (len_0 \neq 0) \wedge (opt_0 + 1 \neq 10)$$

$$p_2(\bar{x}) = (len_0 \neq 0) \wedge (opt_0 + 1 = 10)$$

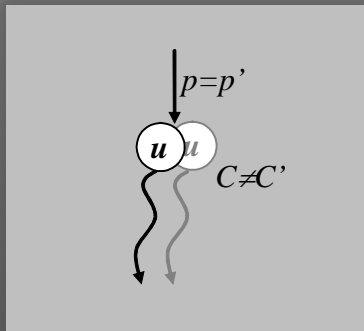
$$p_3(\bar{x}) = (len_0 = 0) \wedge (opt_0 + 1 \neq 10)$$

$$p_4(\bar{x}) = (len_0 = 0) \wedge (opt_0 + 1 = 10)$$

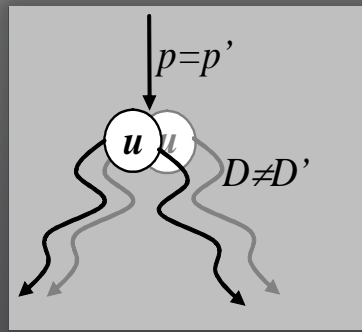


Control flow errors

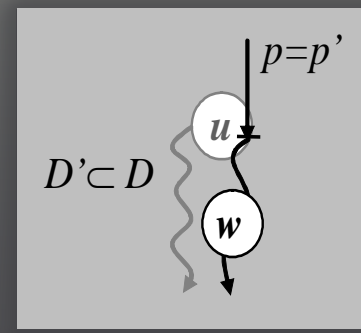
1. Path 'computation' error:



2. Path 'domain' error:

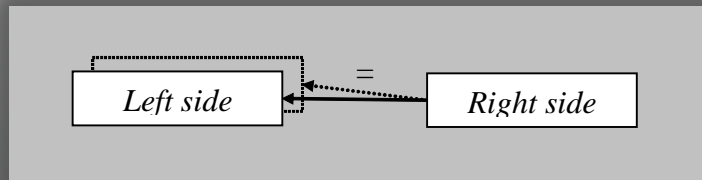


3. 'Subcase' (missing path) error:

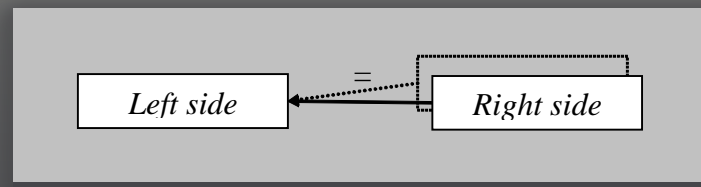


Control flow errors

1. Value assigned to a wrong variable:



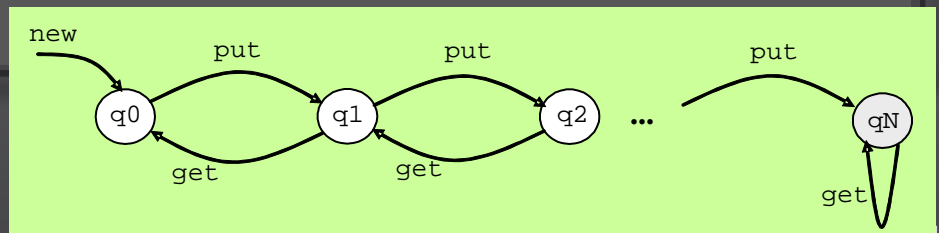
2. Variable assigned a wrong value:



State errors

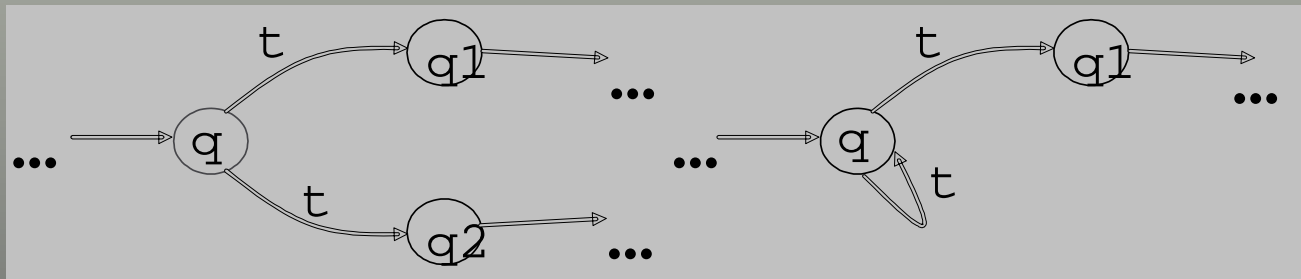
- **Deadlock**

```
public synchronized char get() {  
    char item;  
    while (len == 0) {  
        try {  
            wait(); //buffer is empty  
        } catch (InterruptedException e) {}  
    } //semaphore opened  
    item = pool[opt++];  
    if (opt == N) opt = 0; // modulo N  
    --len; //one element taken  
    /* notifyAll(); //buffer is not full */  
    return item;  
}
```

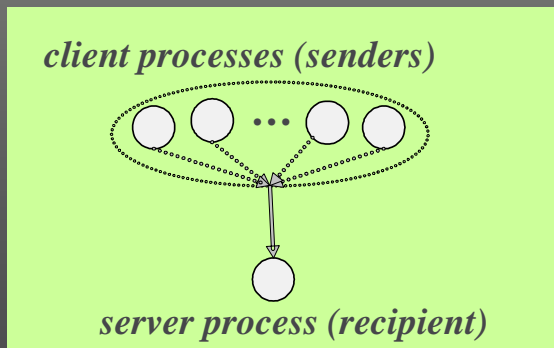


State errors

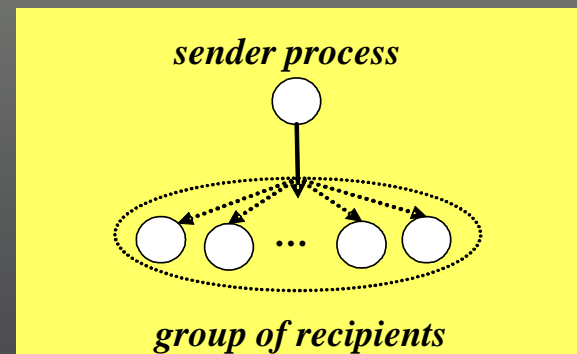
- Races



- on reception:



- on sending:



Text anomalies

- Interpretation of syntax

```
public synchronized char get() {
    char item;
    while (len == 0);
        try {
            wait(); //buffer is empty
        } catch (InterruptedException e) {}
    } //semaphore opened
    item = pool[opt++];
    if (opt == N);
        opt = 0; // modulo N
    notifyAll(); //one element taken
    --len; //one element taken
    return item;
}
```

redundant semicolon

empty statement

redundant semicolon

empty statement

Text anomalies

- Side effects

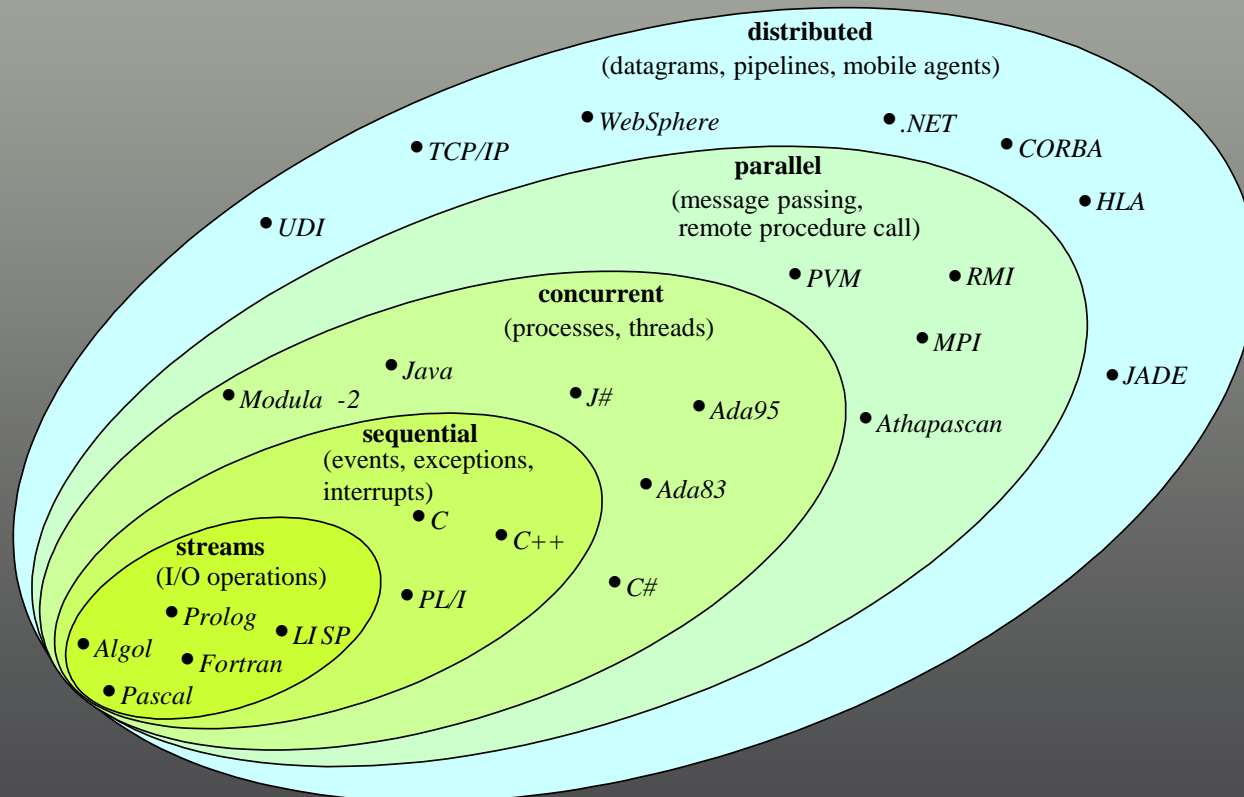
```
int main() {  
    int x,y;  
    int *z;  
    z=&x;  
    z++=1; /* initialization of x */  
    z=2; /* alleged initialization of y */  
}
```

Text anomalies

- Implicit type conversion

```
...
void ff(int); // function with one int argument
...
int ival=3.14; // value 3.14 narrowed to 3, ival=3;
ff(3.14); // value 3.14 narrowed to 3,
           // ff(3) called;
ival=4.0; // conversion of 4.0 to 4 (not narrowed),
ival=4;
...
double fval=5; // promotion of 5 to 5.0 of a „wider“
               // type, fval=5.0;
int val=1;
fval=val+3.14; // promotion of 1 to 1.0 of a „wider“
              // type, fval=1.0+3.14;
...
}
```


Run-time environment models



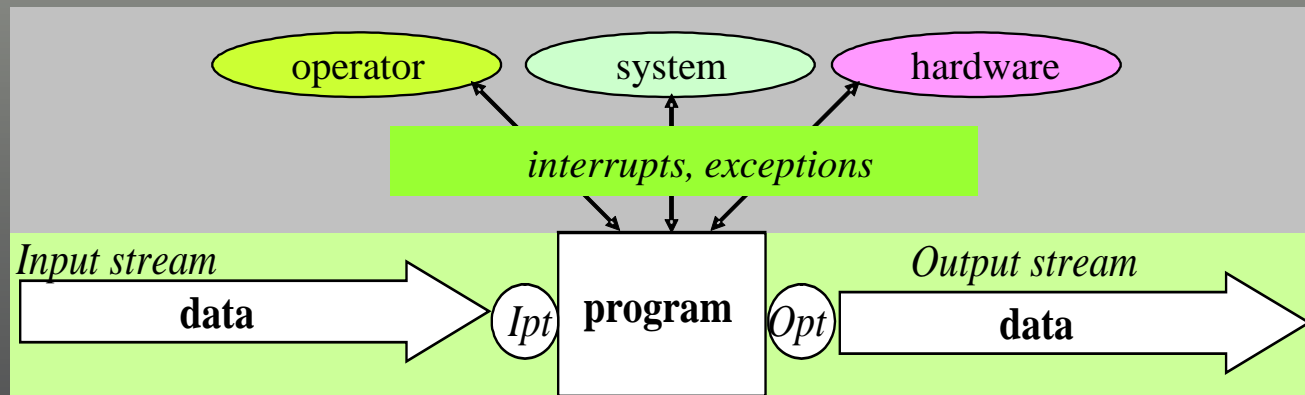
Run-time environment models

- Sequential stream processing



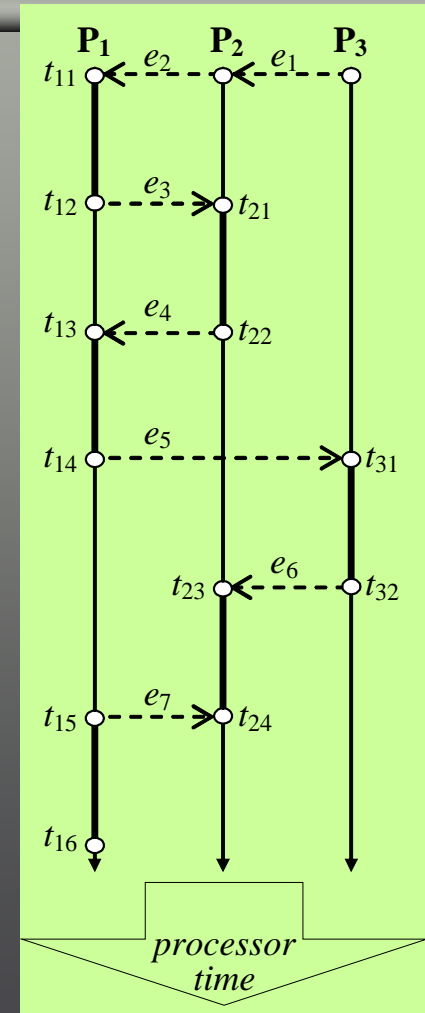
Run-time environment models

- Event driven sequential stream processing



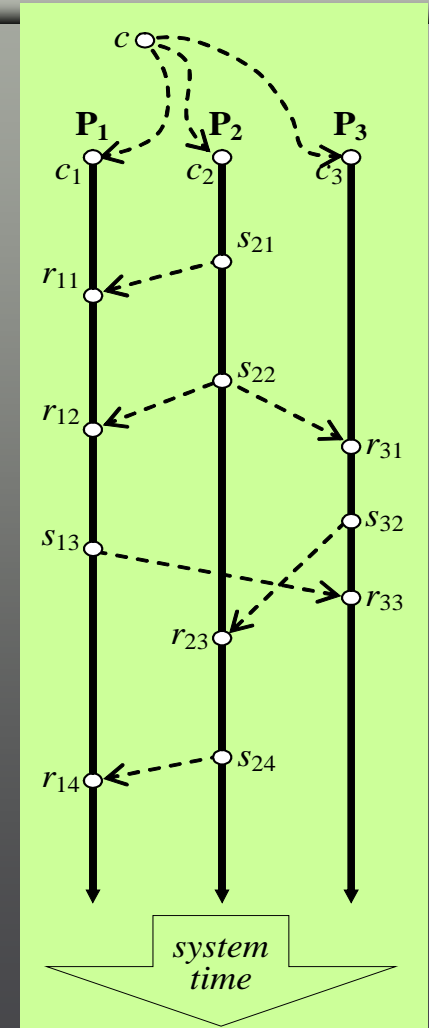
Run-time environment models

- Concurrent processing



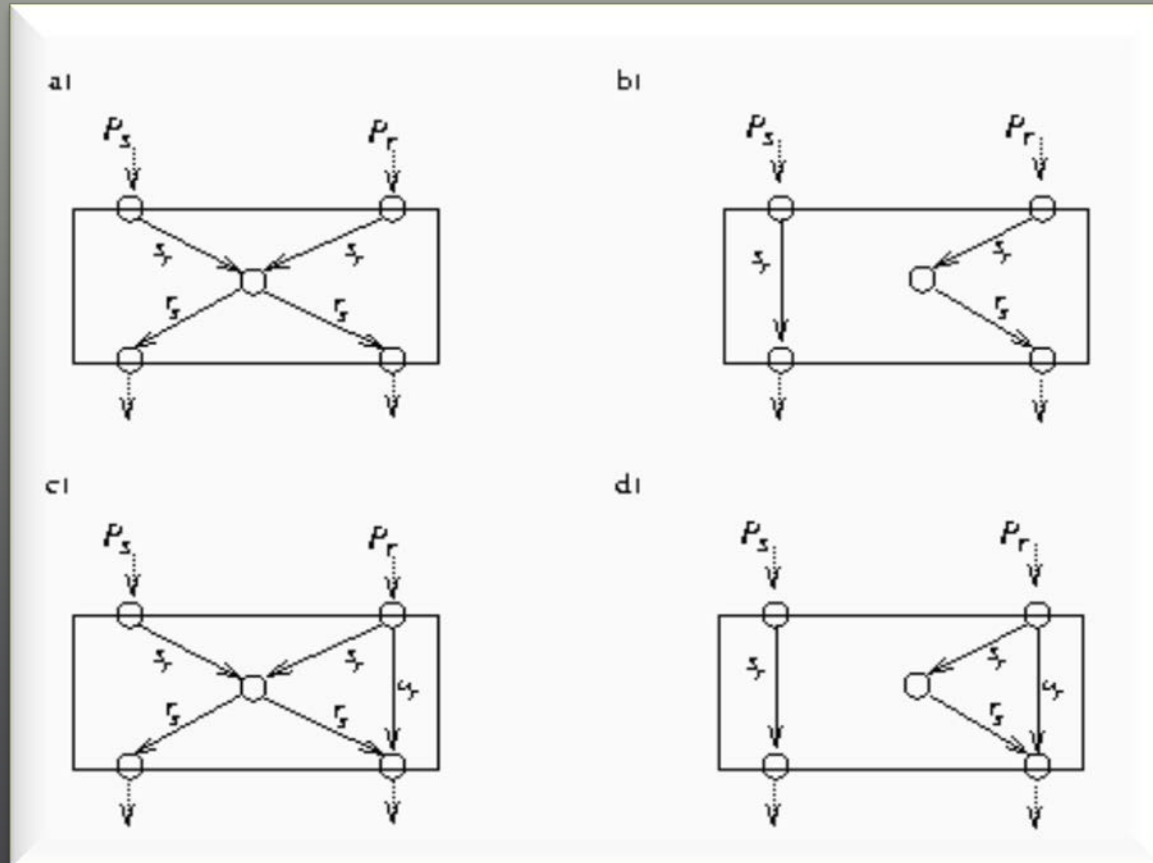
Run-time environment models

- Parallel processing



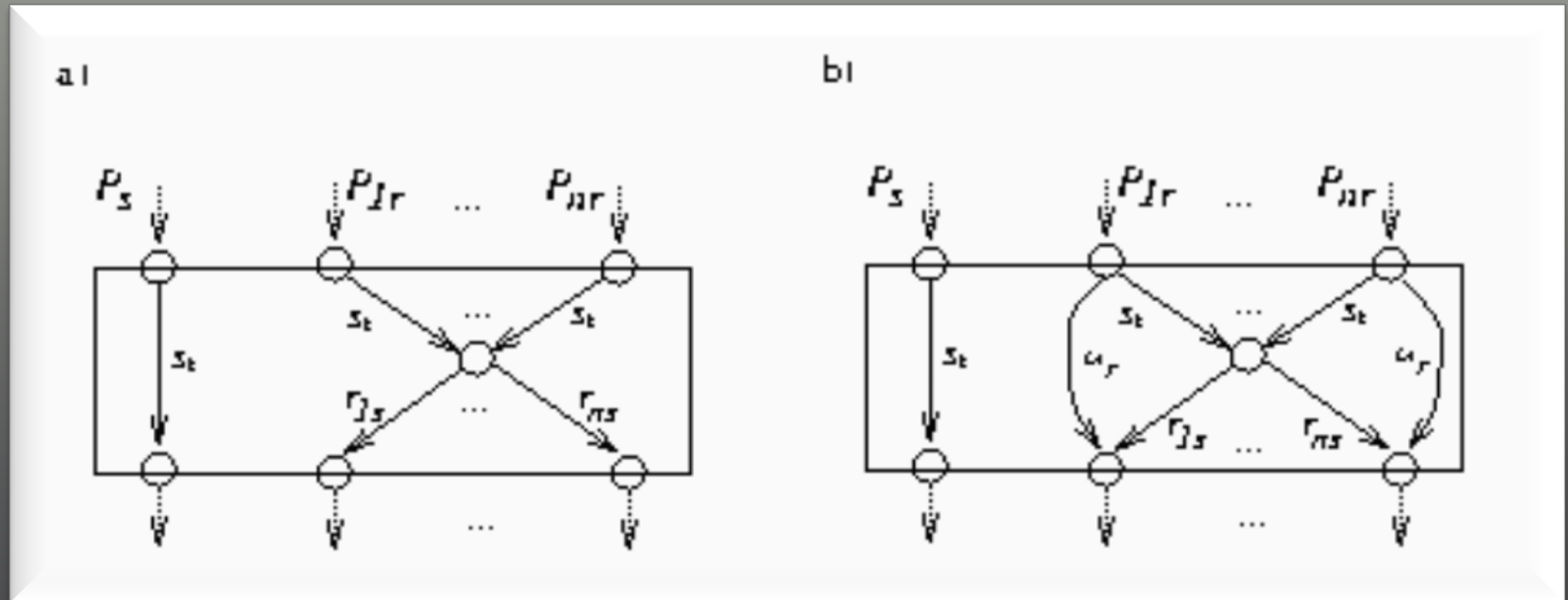
Run-time environment models

- Communication events (1-1)



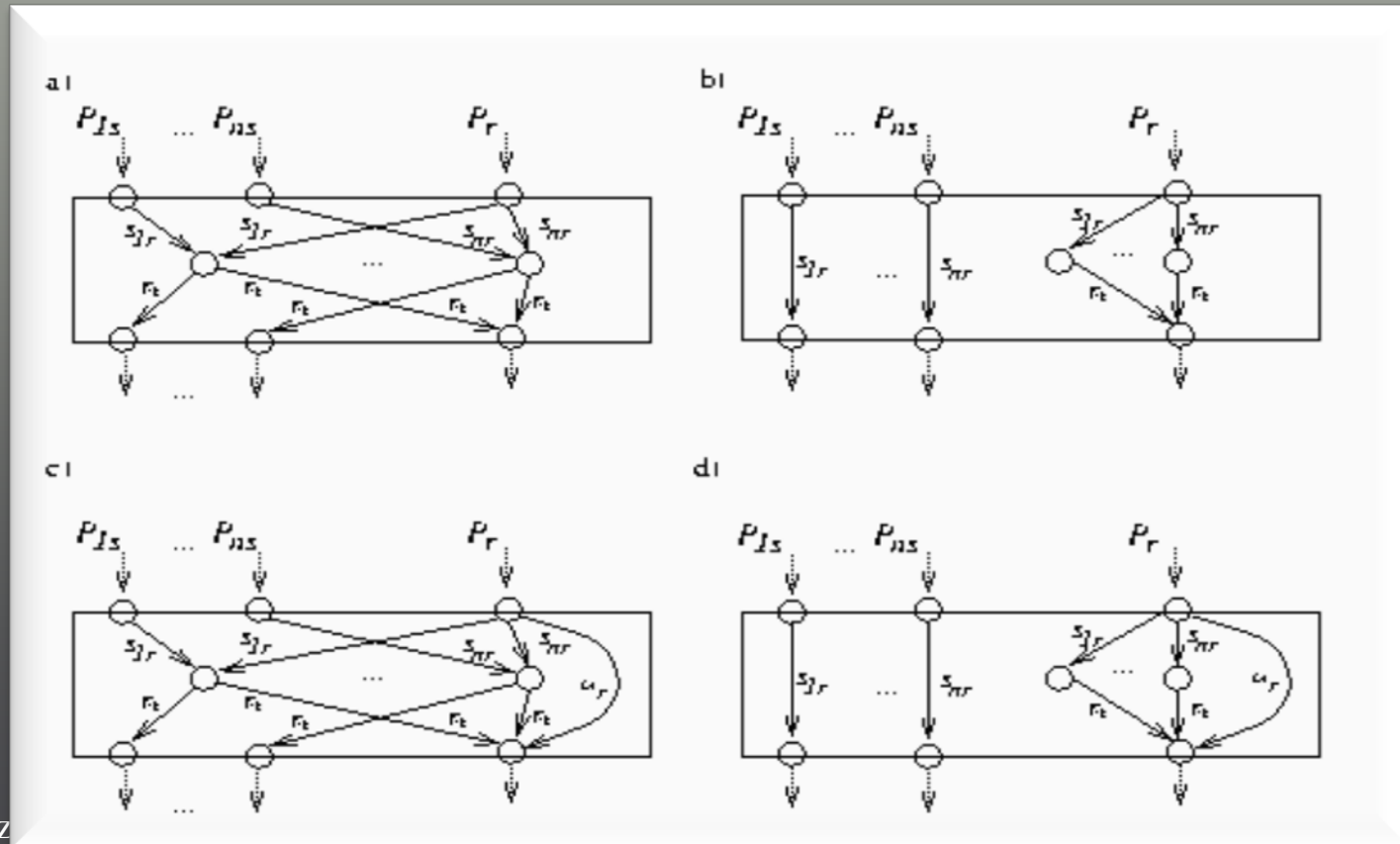
Run-time environment models

- Communication events (1-n)



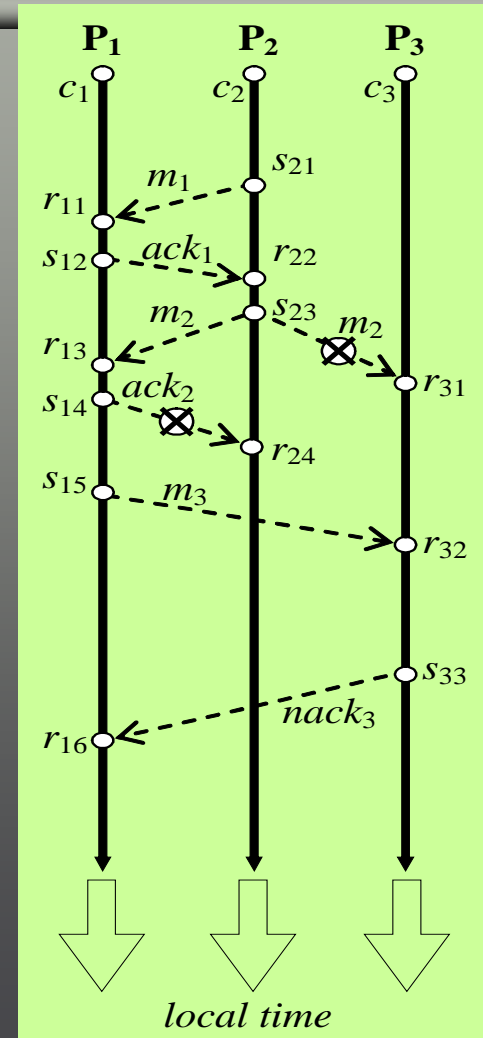
Run-time environment models

- Communication events (n-1)



Run-time environment models

- Distributed processing



Dynamic analysis techniques

- Black-box testing:
 - Program = function,
 - Test cases based on requirements specification
 - Potentially all errors but practically in an infinite time

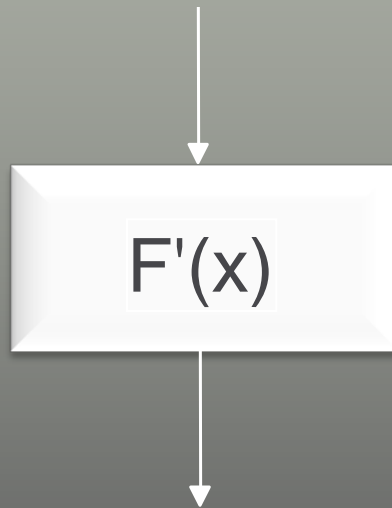
Dynamic analysis techniques

- White-box (structural) testing:
 - Program = structure,
 - Test cases based on technical (architectural/detailed design) specification or the program code
 - Not all errors but in a (practically) predictable time



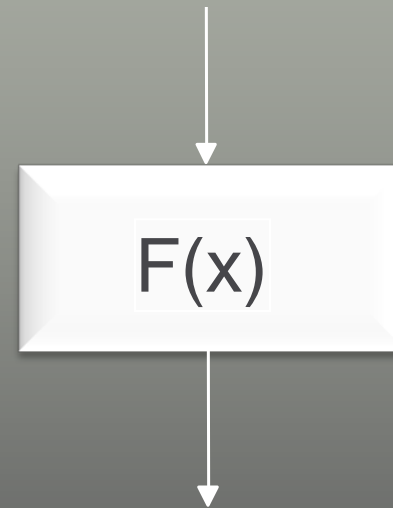
F. Black-box testing

Black-box strategies



specification

<u>input</u>	<u>output</u>
T1	R1
T2	R2
...	...
Tn	Rn



program

$T1, T2, \dots, Tn \rightarrow R1, R2, \dots, Rn$

Black-box strategies

- Mathematical property:

$$T = \{t_i \mid i=1, \dots, N\}, F'(T) = F(T) \Rightarrow F'(x) \equiv F(x)$$

- Limitations:

- ! Undecidability of function equivalence (even of primitive recursive functions!)
- ! Approximate binary arithmetic (floating point error, rounded value, register overflow error)

Black-box strategies

- Special values
- Transcendent values
- Polynomial equivalence
- Monte-Carlo testing

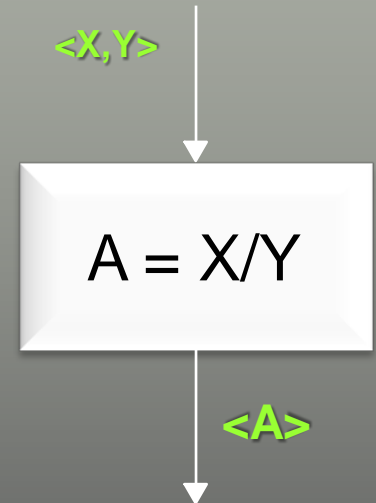
Special values

- Example

$\langle \dots, 1 \rangle ?$ $A=X, A=X*Y$
 $\langle 4, 2 \rangle ?$ $A=X-Y$
 $\langle 0, \dots \rangle ?$ $A=X, A=X*Y, \text{decl}(A)$

$\langle a, b \rangle$ $\langle a \neq 0, b = 0 \rangle$
 $\langle a \neq 0, b \neq 0, a > b \rangle, \text{np. } a=\text{max(float)}, b=\text{min(float)}$
 $\langle a = 0, b = 0 \rangle ?$

$\langle a \neq 0, b \neq 0 \rangle, b < a, b = \text{prime}$



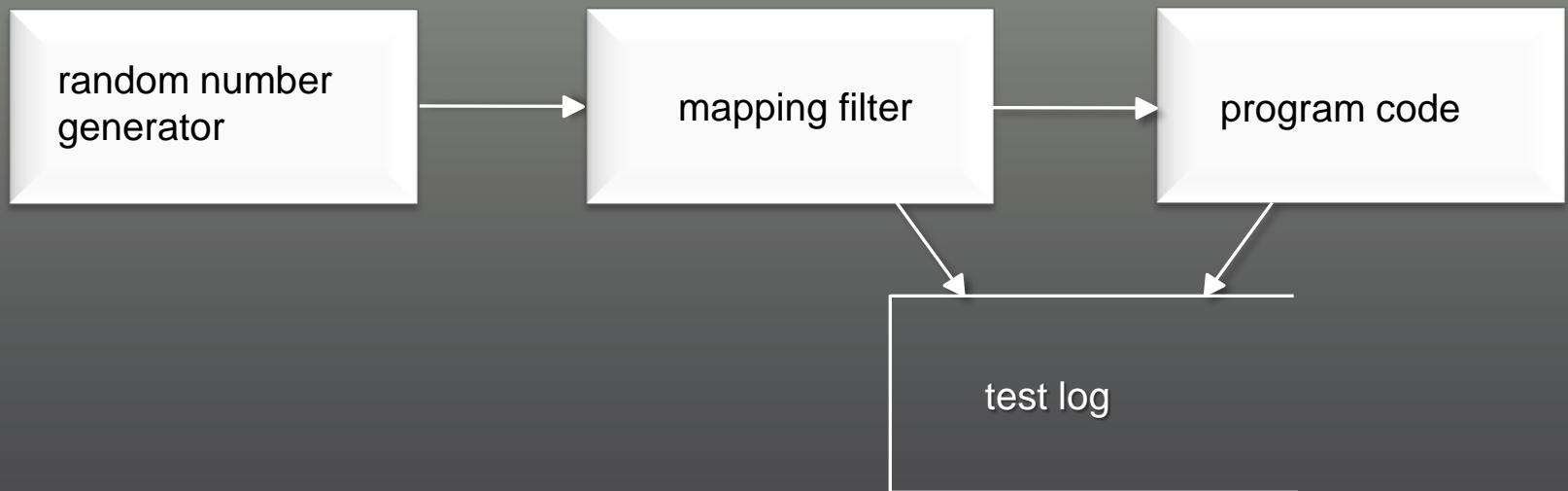
Polynomial equivalence

(!) Standard math functions are computed using polynomials

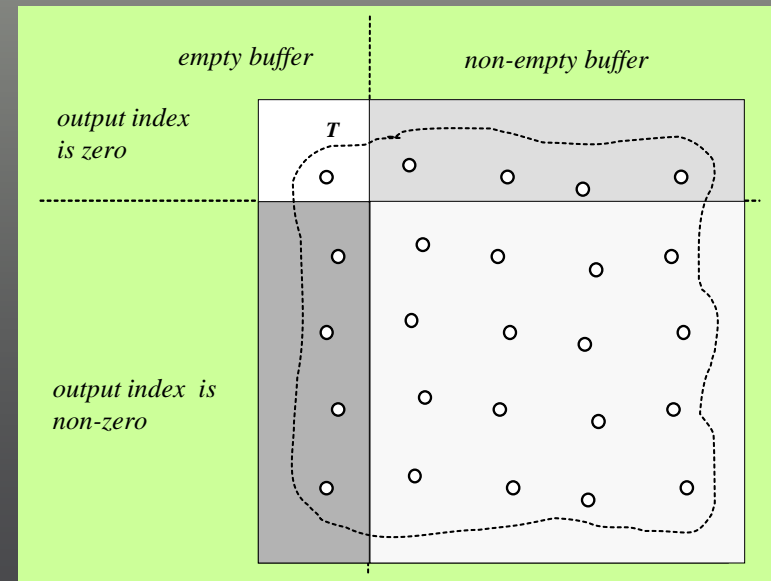
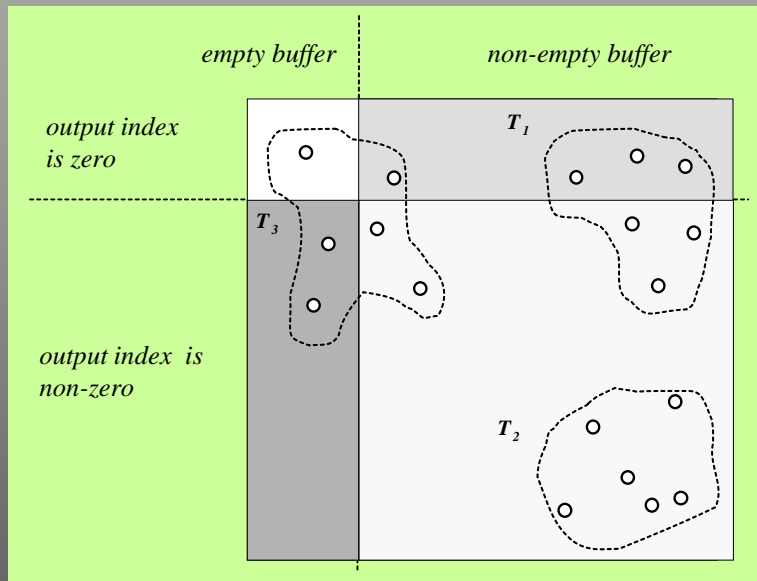
- **Classic polynomial algebra:**
 - Class of polynomials $cf(n,x)$,
 - Tested F , specified $F' \in CF$
 - $T = \{t_1, t_2, \dots, t_{n+1}\}$
 - $F'(T) = F(T) \Rightarrow F'(x) \equiv F(x)$

Monte-Carlo testing

(!) Exercise the program for its most typical and common input values



Monte-Carlo testing





G. White-box testing

White-box testing strategies

- Structural model (program, system)
 - control flow testing
 - data flow testing
 - mutation testing

White-box testing strategies

- Test evaluation:
 - quantitative (metrics) → *rule of thumb*
 - qualitative (model) → *errors are deviations*
- Passing a test:
 - all required test cases exercised
 - all results obtained consistent with the expected ones

→ *test strategy*

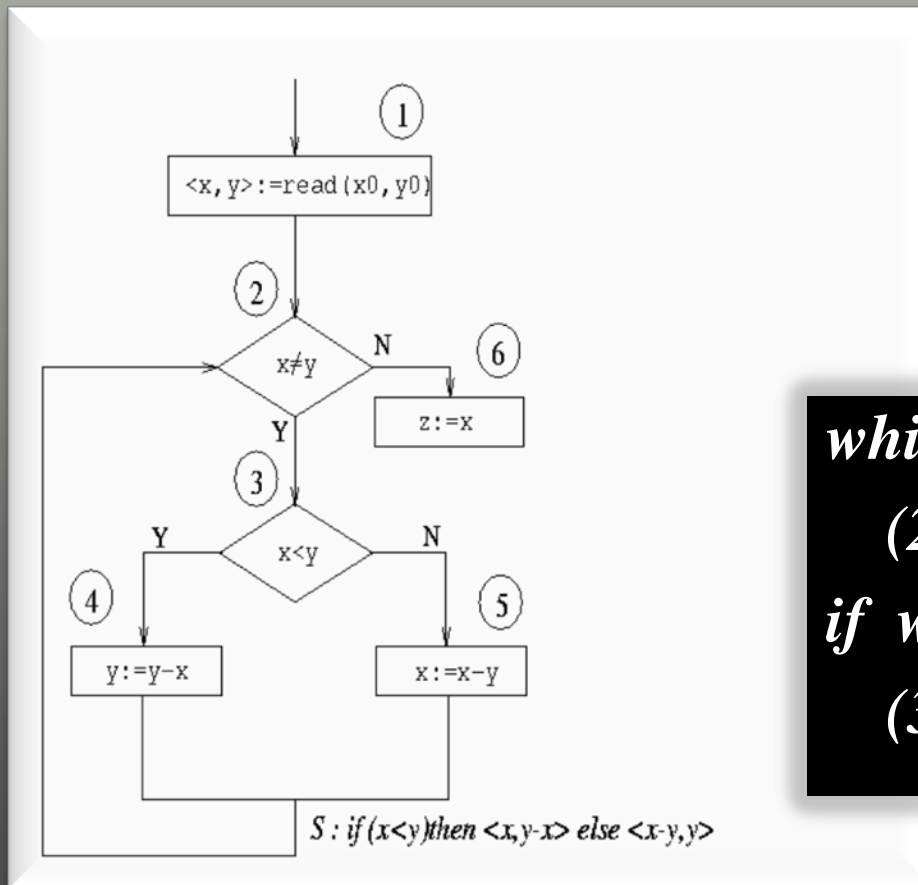
White-box testing strategies

- Branch testing
- Path testing
 - boundary-interior method
 - domain testing
 - computational equivalence of paths
 - simple loop patterns

White-box testing strategies

- Data flow testing
 - definition-use chains
- Mutation testing
 - Text anomalies

Branch testing



(!) Each predicate
„true” and „false”

while w. "2":
(2,3), (2,6)
if w. "3":
(3,4), (3,5)

Path testing

(!) Incorrect control flow implies incorrect results
(!) Paths can exercise control flow systematically

- Program model:

- Control flow graph:
- Input variables:
- Program (input) domain:
- Program path:
- Path condition:
- Path domain:
- Path computation:

$G(a,n,s,e)$

$x = \langle x_1, x_2, \dots, x_n \rangle$

$D = X_1 \times X_2 \times \dots \times X_n$

$p = (n_0, n_1, \dots, n_k)$

$p(x)$

$d(p) = \{ x \mid p(x) \}$

$c(p): d(p) \rightarrow R$

Path testing

- **Strategies:**
 - boundary-interior method
 - domain testing
 - computational equivalence of paths
 - simple loop patterns

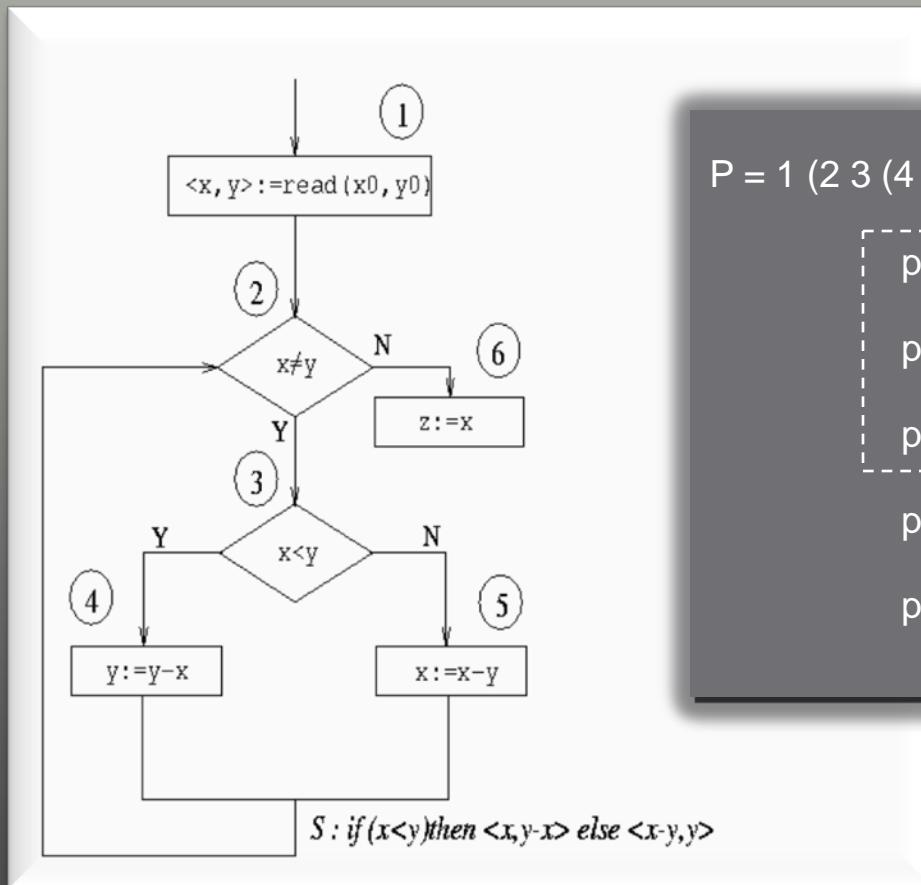
Boundary-interior method

(!) Problem with loops

- Intuitive criterion:
 - Each loop ZERO and non-zero number of iterations,
 - Each loop MAX number of iterations

→ Similar but more demanding than branch testing

Example



$$P = 1 (2 3 (4 \cup 5))^* 2 6$$

$$p_0 = 1 2 6,$$

$$p_1 = 1 2 3 4 2 6$$

$$p_2 = 1 2 3 5 2 6$$

$$p_3 = 1 2 3 4 2 3 5 2 6$$

$$p_4 = 1 2 3 5 2 3 4 2 6$$

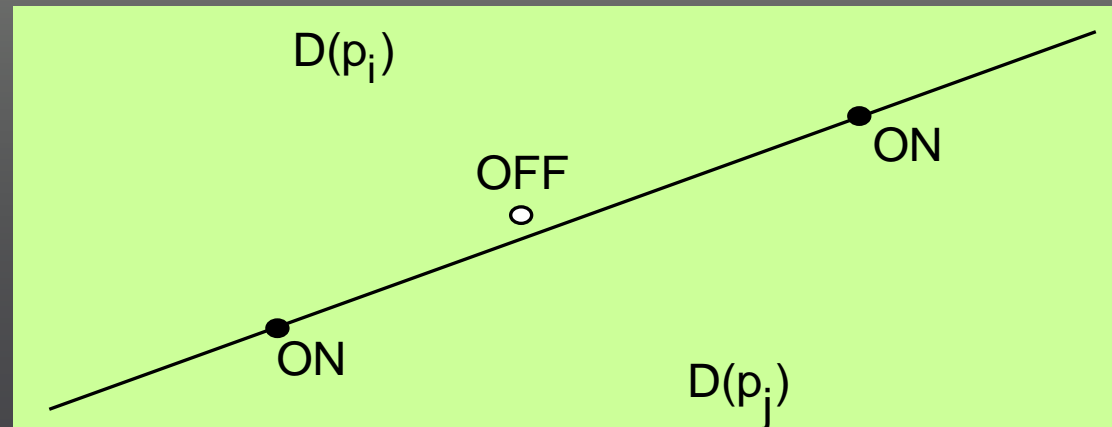
...

Domain testing

(!) Looking for domain errors

- Assumptions:

- Predicates $p(\underline{x})$ are linear functions on X ,
- Path computations $c(p)$ are different,
- No coincidental correctness.

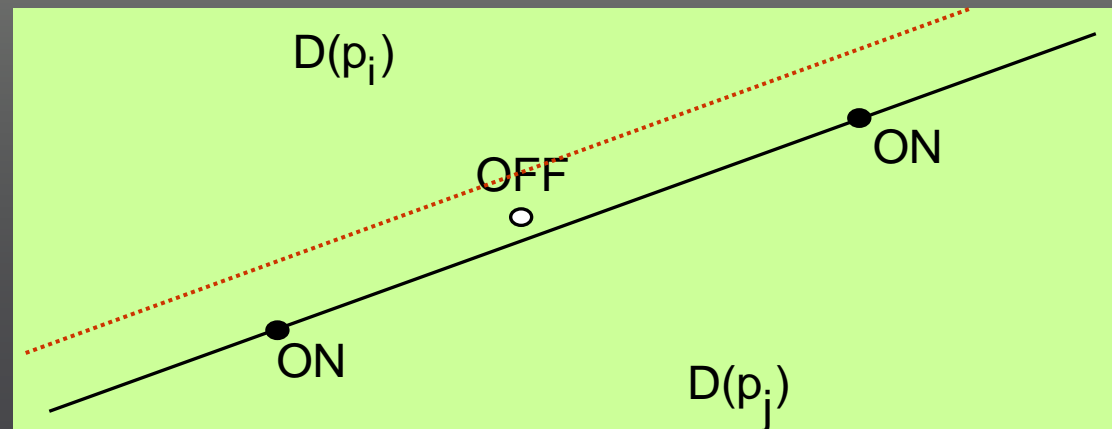


Domain testing

(!) Looking for domain errors

- Assumptions:

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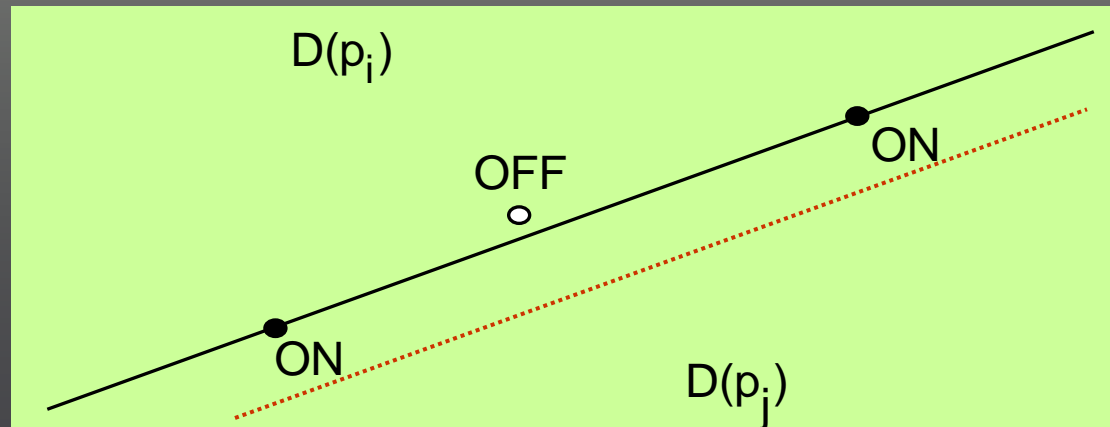


Domain testing

(!) Looking for domain errors

- Assumptions:

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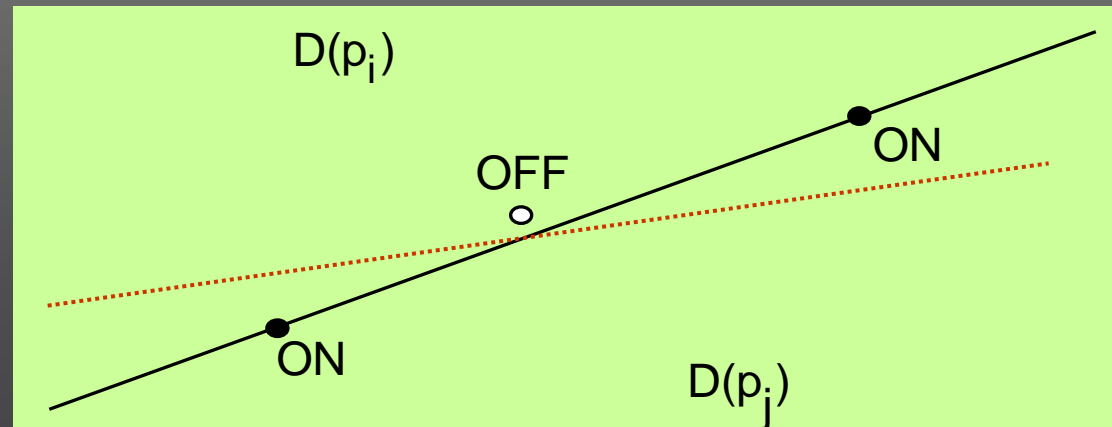


Domain testing

(!) Looking for domain errors

- Assumptions:

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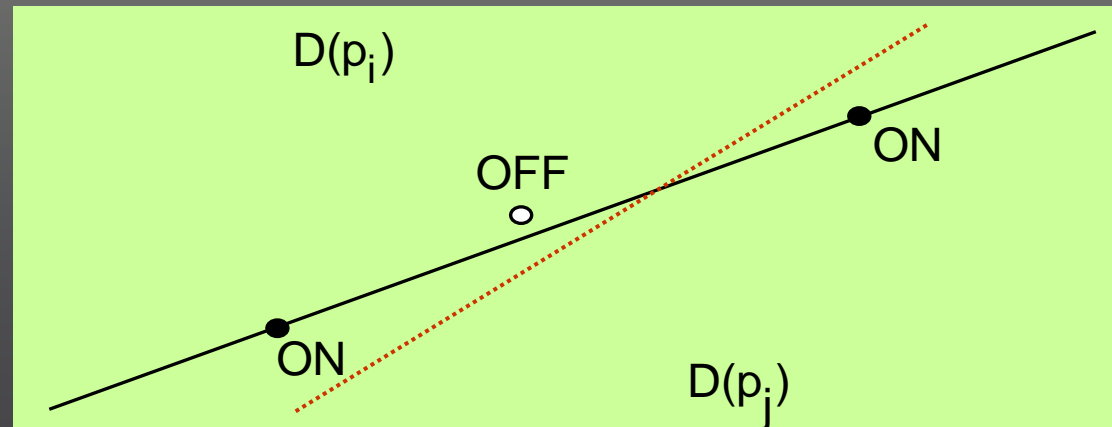


Domain testing

(!) Looking for domain errors

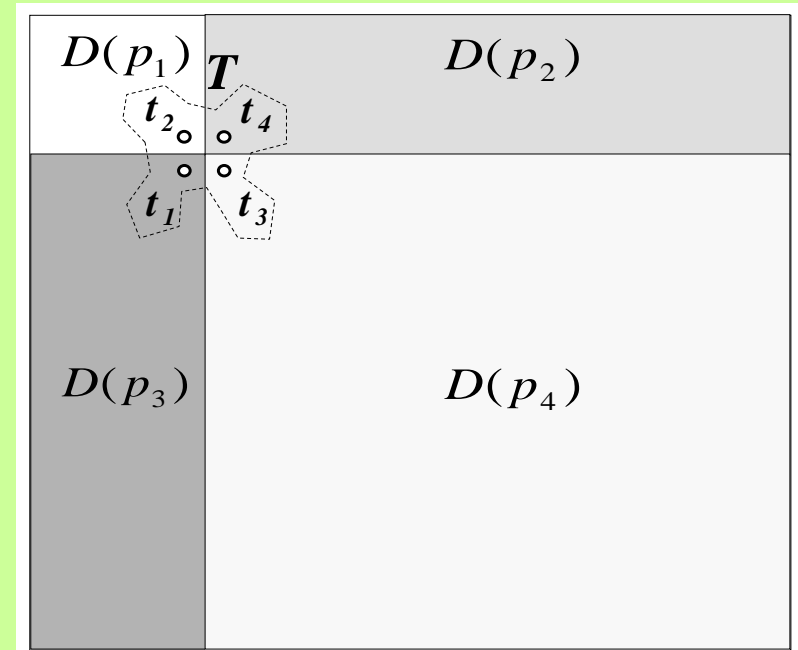
- Assumptions:

- Predicates $p(\underline{x})$ are linear functions on X ,
- Path computations $c(p)$ are different,
- No coincidental correctness.



Example

- Domain testing



Computational equivalence of paths

- Input data:
- Input domain:
- Output variables:
- Path computation space:

$$\mathbf{x} = \langle x_1, x_2, \dots, x_n \rangle$$

$$D = X_1 \times X_2 \times \dots \times X_n$$

$$\mathbf{y} = \langle y_1, y_2, \dots, y_m \rangle$$

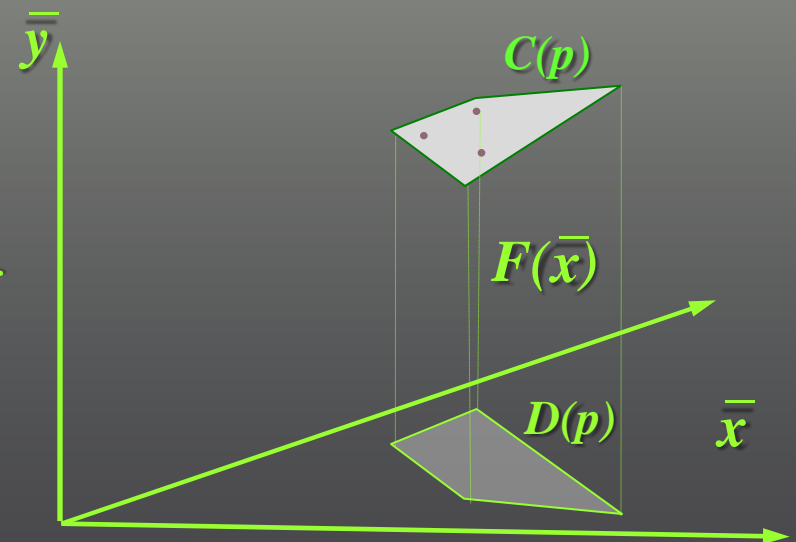
linear, (n+m)-dimensional

Test case:

path p

(n+m)-vector $\mathbf{t} = \langle d_1, d_2, \dots, d_n, r_1, r_2, \dots, r_m \rangle$

n+m vectors $\{t_1, t_2, \dots, t_{n+m}\}$



Example

- Path computation testing:

- path

p_1 : 1-2-7-8-10-11-12-13

- computation

$C(p_1) : \langle len_0, opt_0, item, e, pool[10], len_0, opt_0 \rangle \rightarrow \langle len_0, opt_0, item, e, pool[10], len_0 - 1, opt_0 + 1 \rangle$

- hyperplane

$$\begin{bmatrix} opt \\ len \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} opt_0 \\ len_0 \end{bmatrix} + \begin{bmatrix} 1 \\ -1 \end{bmatrix}$$

Simple loop patterns

- Input variables:
- Input domain:
- Program variables:
- Program computation space:

$$X = \langle X_1, X_2, \dots, X_n \rangle$$

$$D = X_1 \times X_2 \times \dots \times X_n$$

$$Z = \langle Z_1, Z_2, \dots, Z_k \rangle$$

(n+2k)-dimensional

$$f_0 = g_{sv} g_{ve}, \quad f_1 = g_{sv} h g_{ve}, \quad \dots, \quad f_n = g_{sv} h^n g_{ve}, \quad \dots$$

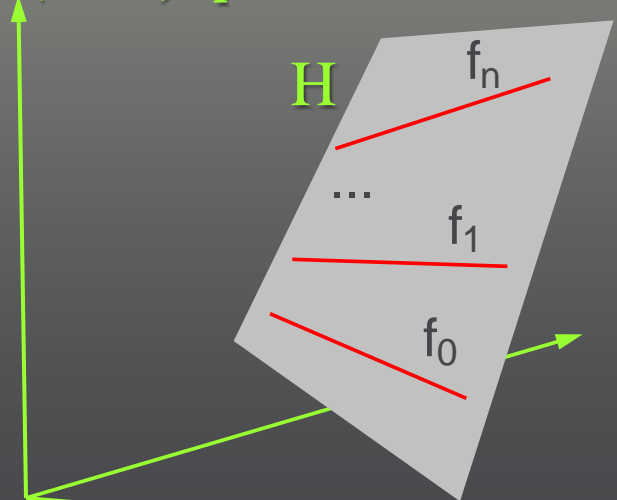
$$f_n = \begin{cases} f_0 & n=0 \\ f_{n-1} H & n>0 \end{cases}$$

$$H = (g_{ve})^{-1} h (g_{ve})$$

- test completion criterion:

$$S = 1 + \lceil (2k-1)/n \rceil \text{ paths}$$

(n+2k)-space



Example

```
1: 2      int asynBCD(int number,int count){
2: 3      char symbol;
3: 4      for(;;)
4: 5      {for(;;)
5: 6 7     {receive(symbol);
6: 11     if((symbol==SPACE) || (symbol==STOP))
7: 8      break;
8: 9 10    count++;
9:        if(count>9)
10:       return ERROR;
11: 12     }
12: 13 14  number=10*number+count;
13:       if(symbol==STOP)
14: 2      return (number);
15:       }
15:       }
```

Input variables:

symbol, number, count

→ $n=3$

Program variables:

number, count

→ $k=2$

Data flow

- Simple chain:

<definition, use>

ⓓ: $x = f(5)+3y$

...

Ⓤ: $z = 2x-y$

- Use chain:

<all-definition, use>

ⓓ: $x = f(5)+3y$

...

Ⓤ: $z = 2x-y$

...

ⓐ: $w = x*z$

- Live chain:

<all-definition, all-use>

ⓓ: $x = f(5)+3y$

...

Ⓤ: $z = 2x-y$

...

ⓐ: $w = x*z$

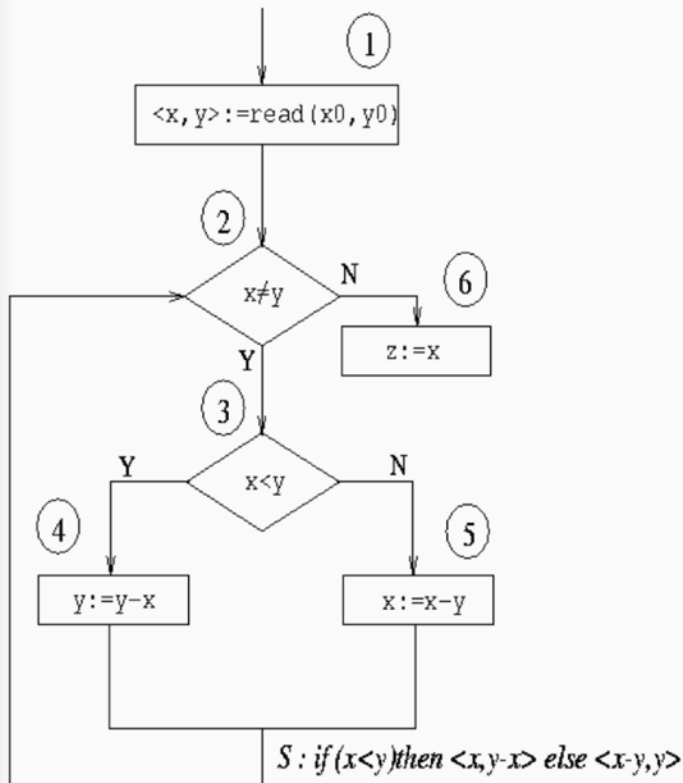
...

ⓑ: $y = x+w$

criterion

→ Exercise each chain

Examples



“d-u” chains (simple):

$\langle 1, 3 \rangle, \langle 4, 2 \rangle, \dots$

“ad-u” chains (use):

$\langle 1, 4, 3 \rangle, \langle 4, 5, 3 \rangle, \dots$

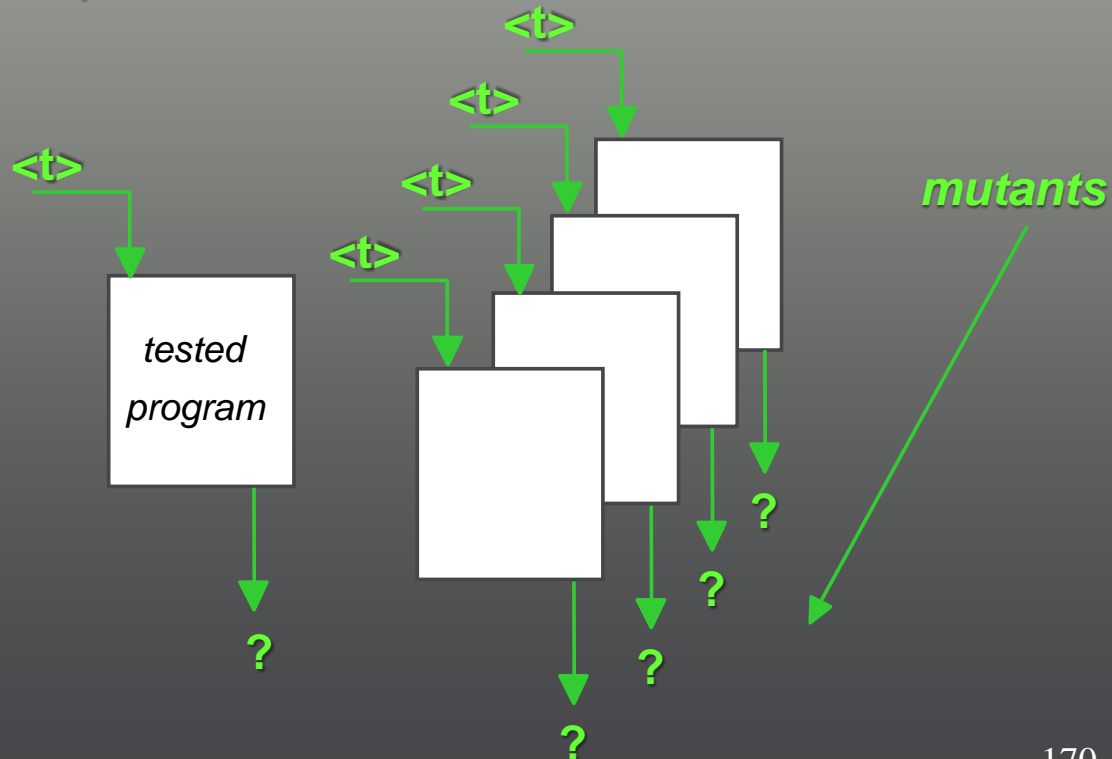
“ad-au” chains (live):

$\langle 1, 4, 6 \rangle, \langle 1, 5, 6 \rangle, \dots$

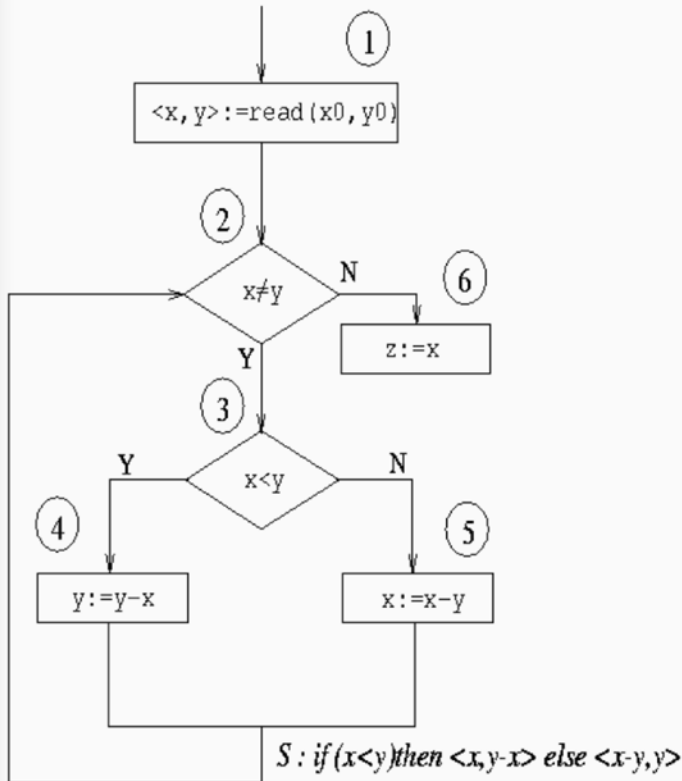
Mutation testing

(!) errors result from occasional "typos" in the program text

→ test harness, Monte-Carlo



Example



$M_1 \rightarrow \text{while } (x=y) \dots$
 $M_2 \rightarrow \text{if } (x=y) \dots$

$\langle x, y \rangle$	P	M_1	M_2
$\langle 9, 3 \rangle$	3	9	3
$\langle 9, 6 \rangle$	3	-	↑

Structure of test cases

- Input data
- Expected results
- Environment settings
- Scenario context

Test script

```
/* TeSS 1 */
{
  /* request the master to go first (1) */
  <
    (before 0 22 [])
  >
  /* reach the voting configuration by slaves (2) */
  <
    (before 1 26 [print stid; print ntid;])
    (before 2 26 [print stid; print ntid;])
    (before 3 26 [print stid; print ntid;])
  >
  /* reach the reporting configuration by slaves (3) */
  <
    (before 1 41 [print data;])
    (before 2 41 [print data;])
    (before 3 41 [print data;])
  >
}
```

Logging the state



Test script

```
/* TeSS 2 */
{
  /* request the master to go first (1) */
  /* spoil v_size of slave #3 before voting */
  <
    (before 0 22 [])(after 3 23 [set v_size=0;])
  >
  /* reach the voting configuration by slaves (2) */
  <
    (before 1 26 [])
    (before 2 26 [])
    (before 3 26 [])
  >
  /* reach the reporting configuration by slaves (3) */
  <
    (before 1 41 [print data;])
    (before 2 41 [])
    (before 3 41 [])
  >
  /* make slave #1 winning the race */
  <
    (after 0 22 [])(after 1 41 [])
  >
}
```

Value enforcement



Attributes of test cases

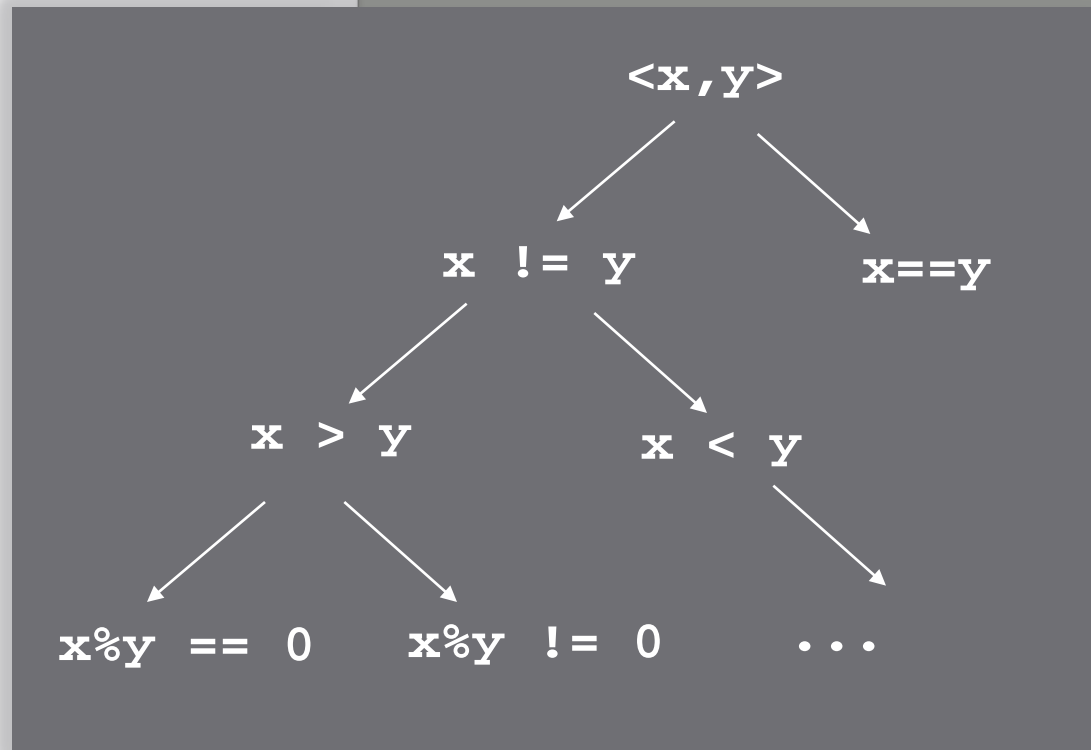
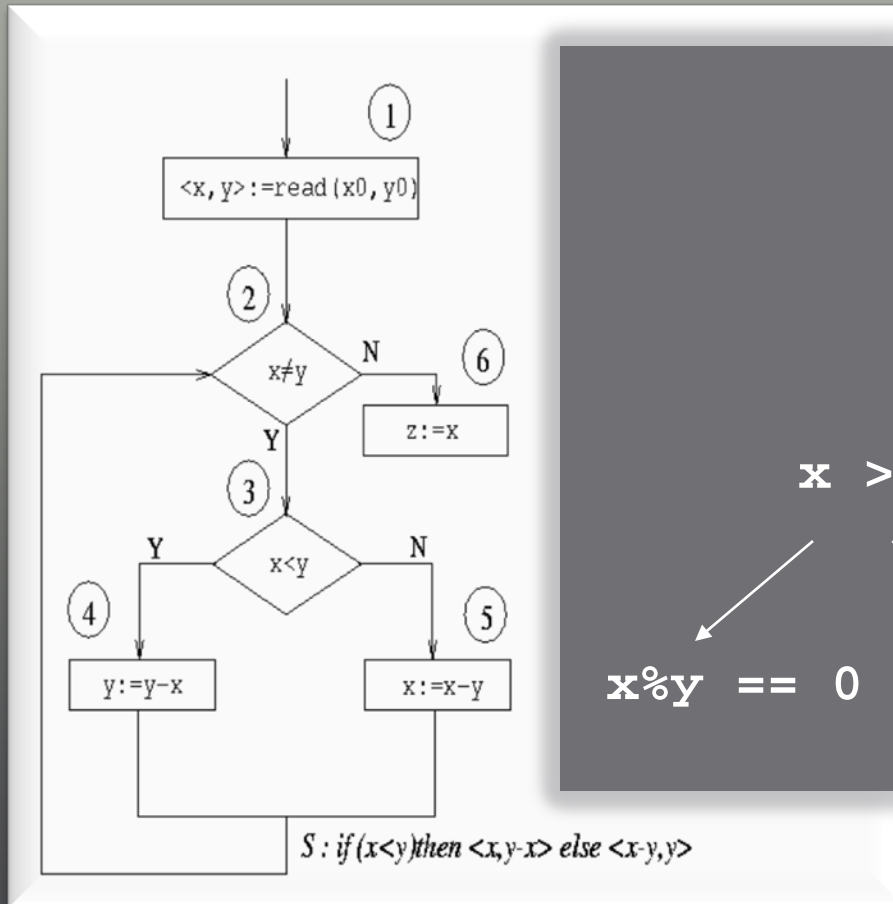
- Representativeness
 - A single case represents a subset
- Feasibility
 - Non-empty set of input data exists, eg. path condition is satisfied
- Observability
 - Deterministic automaton
- Reproducibility
 - All input data identified (path condition interpretation)
 - Timing conditions under tester's control

Feasibility

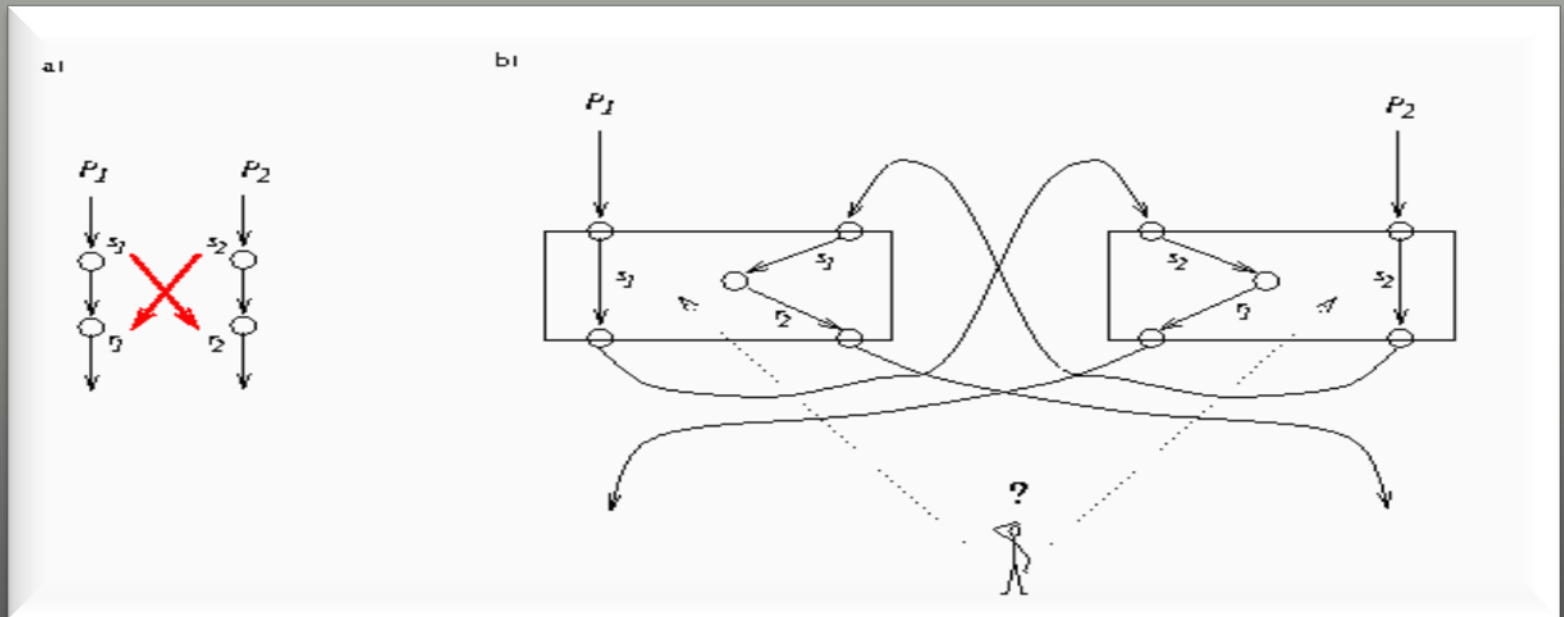
```
1: 2      int asynBCD(int number,int count){
2: 3      char symbol;
3: 4      for(;;)
4: 5      {for(;;)
5: 6 7     {receive(symbol);
6: 11     if((symbol==SPACE) || (symbol==STOP))
7: 8      break;
8: 9 10    count++;
9:      if(count>9)
10:     return ERROR;
11:     }
12:     number=10*number+count;
13:     if(symbol==STOP)
14:     return (number);
15:     }
16:     }
```

! ? p = 1 2 (3 4 5 7 8 10)¹⁰ 3 4 5 7 8 9

Representativeness

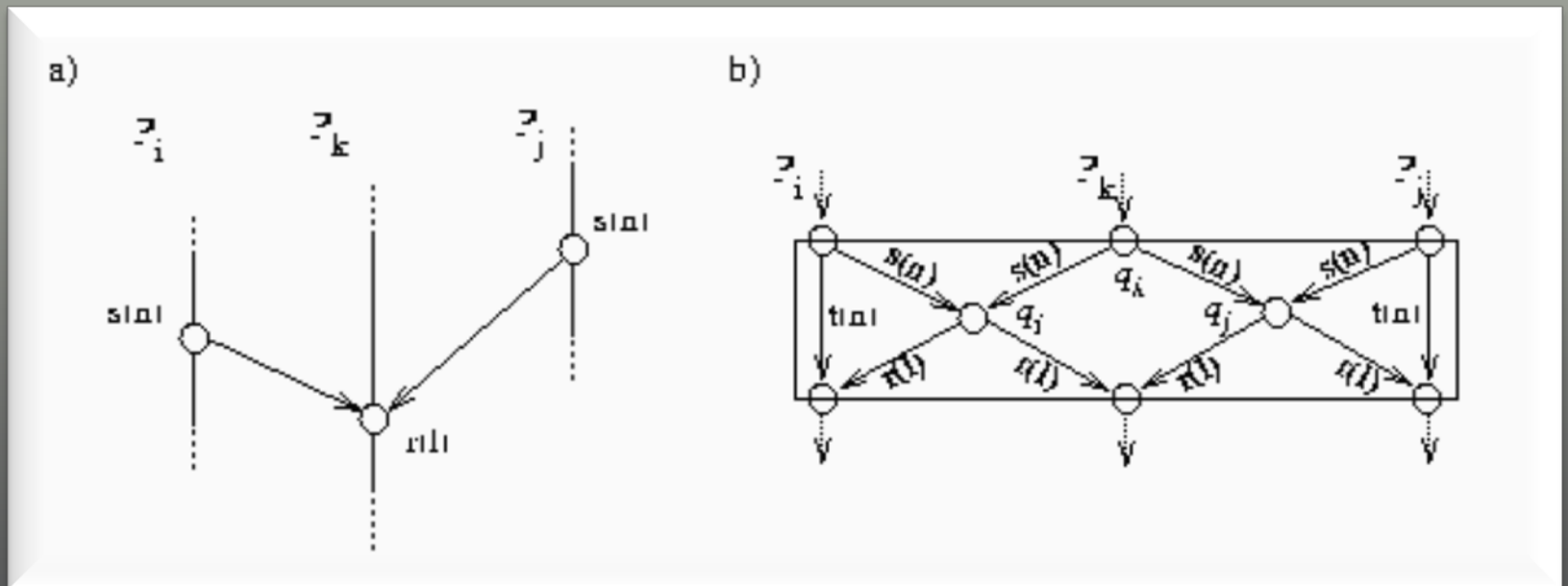


Observability



→ Testing error

Reproducibility

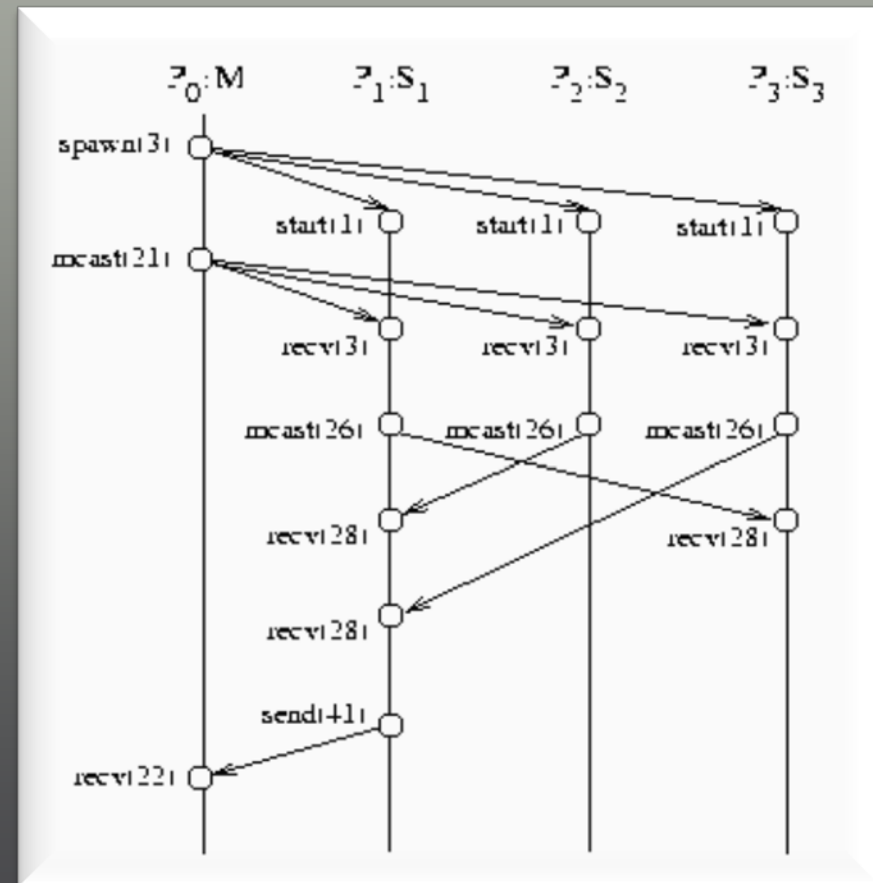


Logging results

- **Checkpoint**
 - static (“compiled in”)
 - dynamic (breakpoint)
- **Log**
 - centralized
 - distributed
- **Result analysis**
 - on-line (state or event detection),
 - off-line (% of test coverage, error localization)
 - replay (visualization, state recovery)

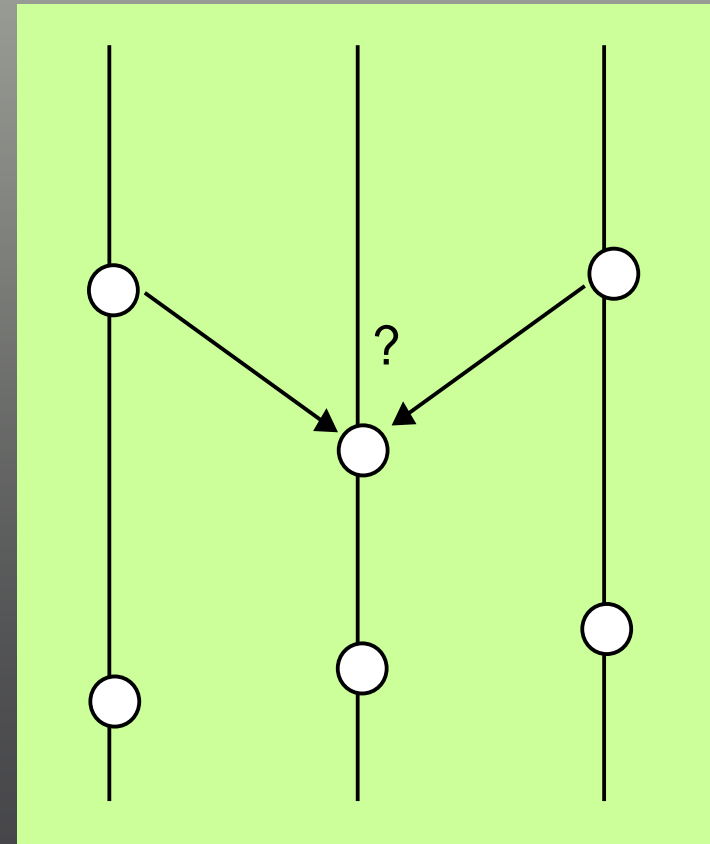
Test scenario execution mode

- random
- supervised
- deterministic



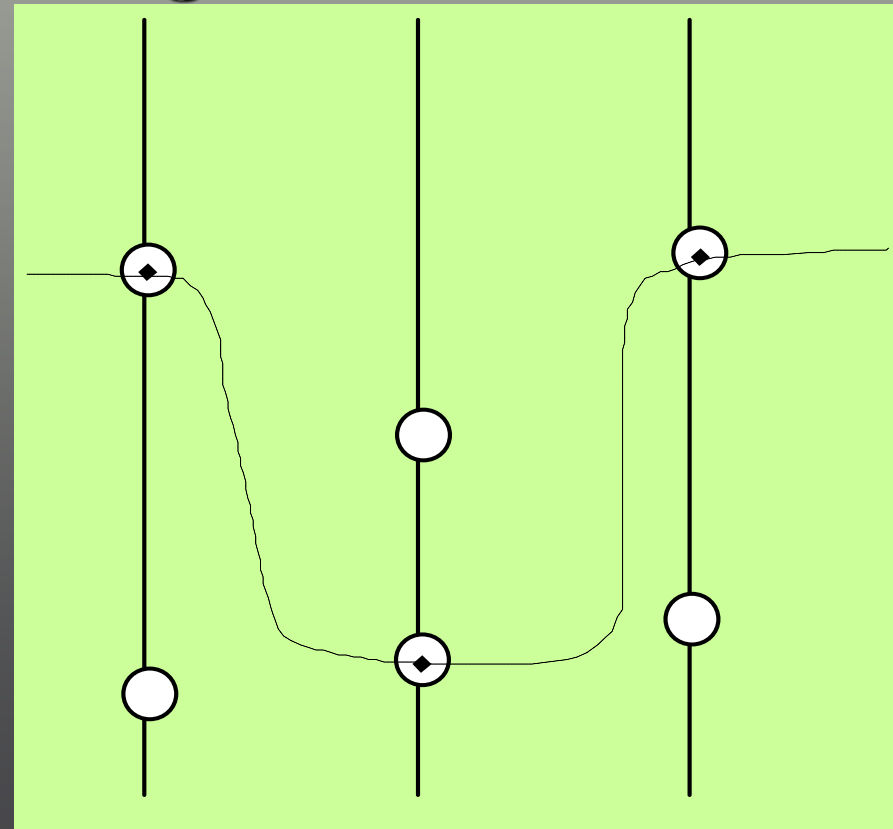
Test scenario types

- One-thread-One-time (OtOt):
race detection



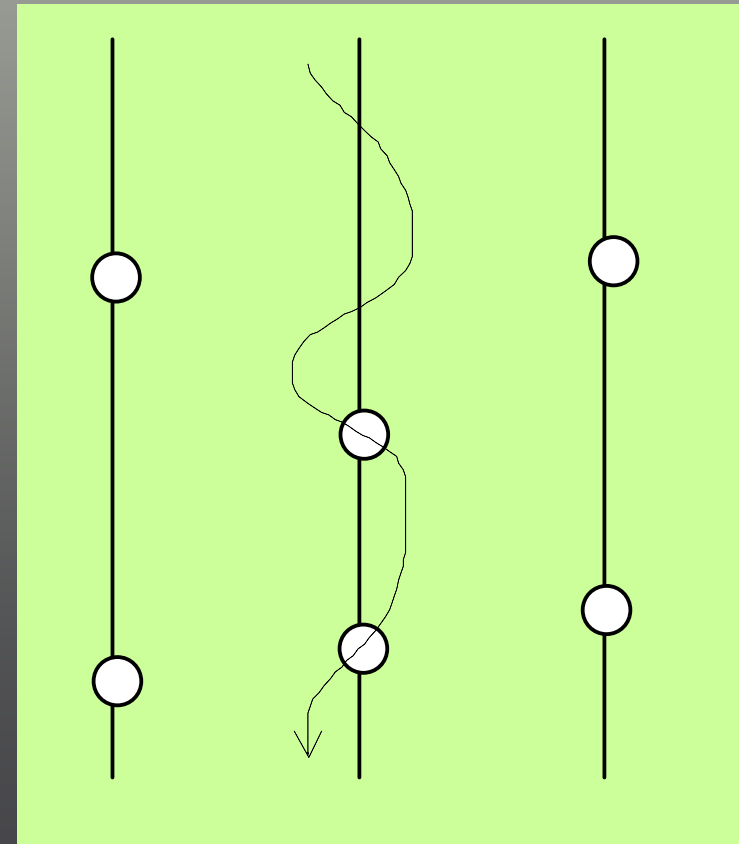
Test scenario types

- Many-threads-One-time (MtOt):
global state monitoring



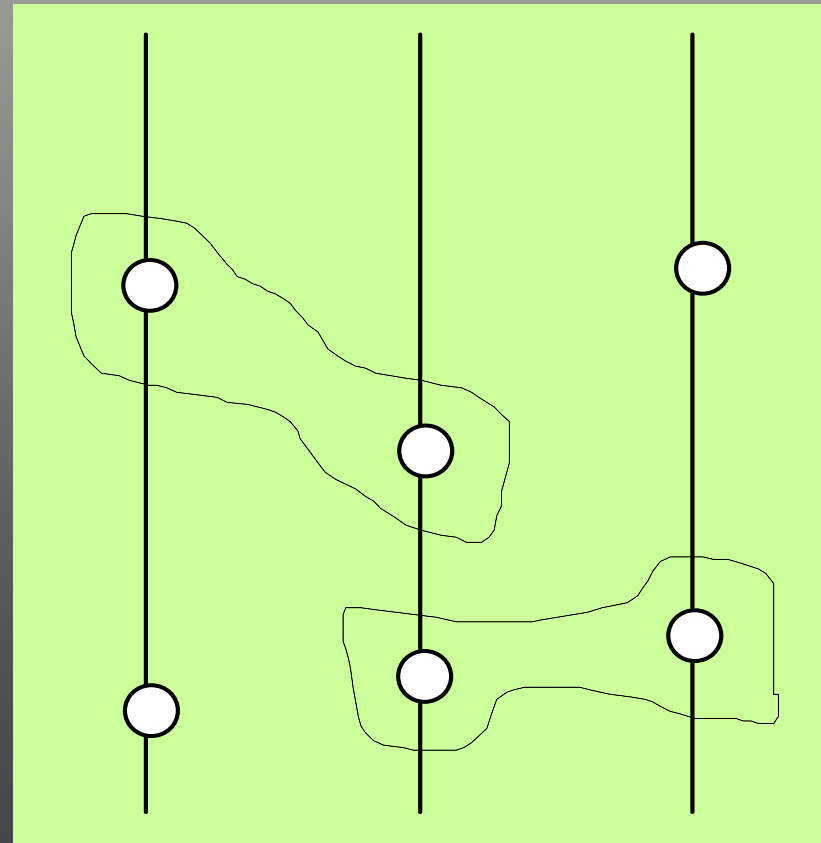
Test scenario types

- **One-thread-Many-times (OtMt):**
single process path testing

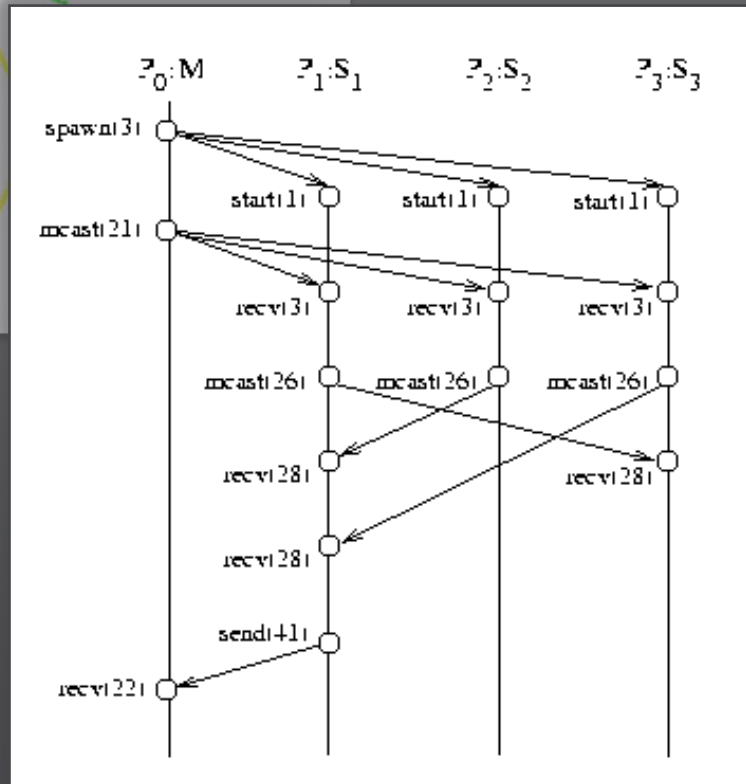
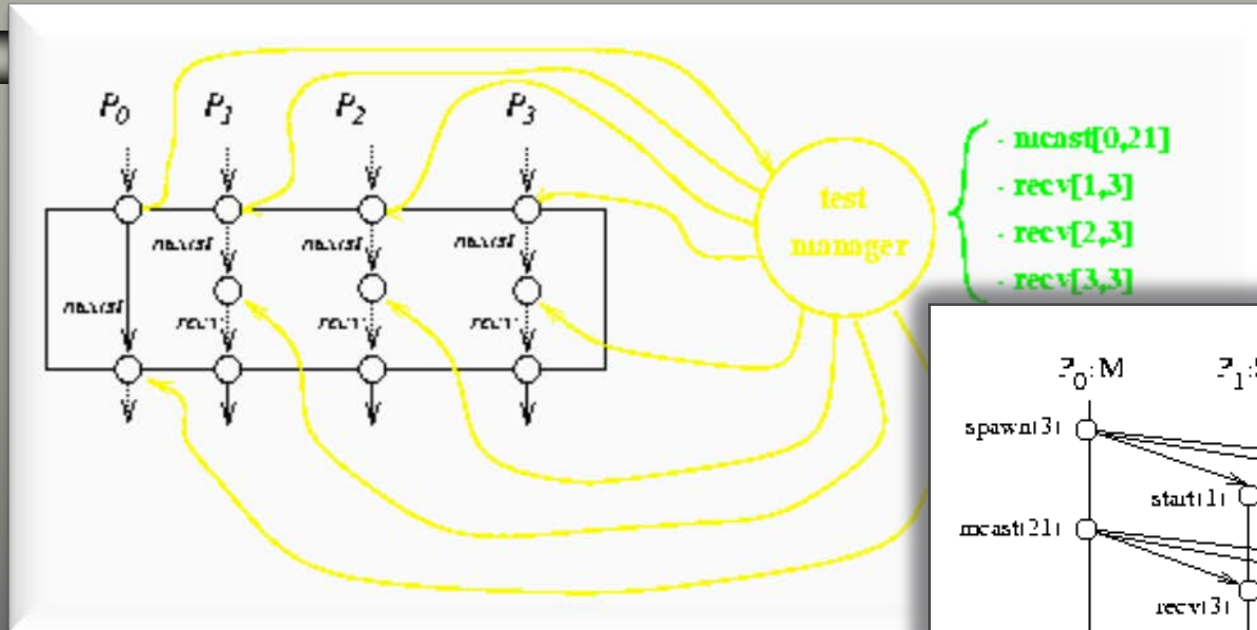


Test scenario types

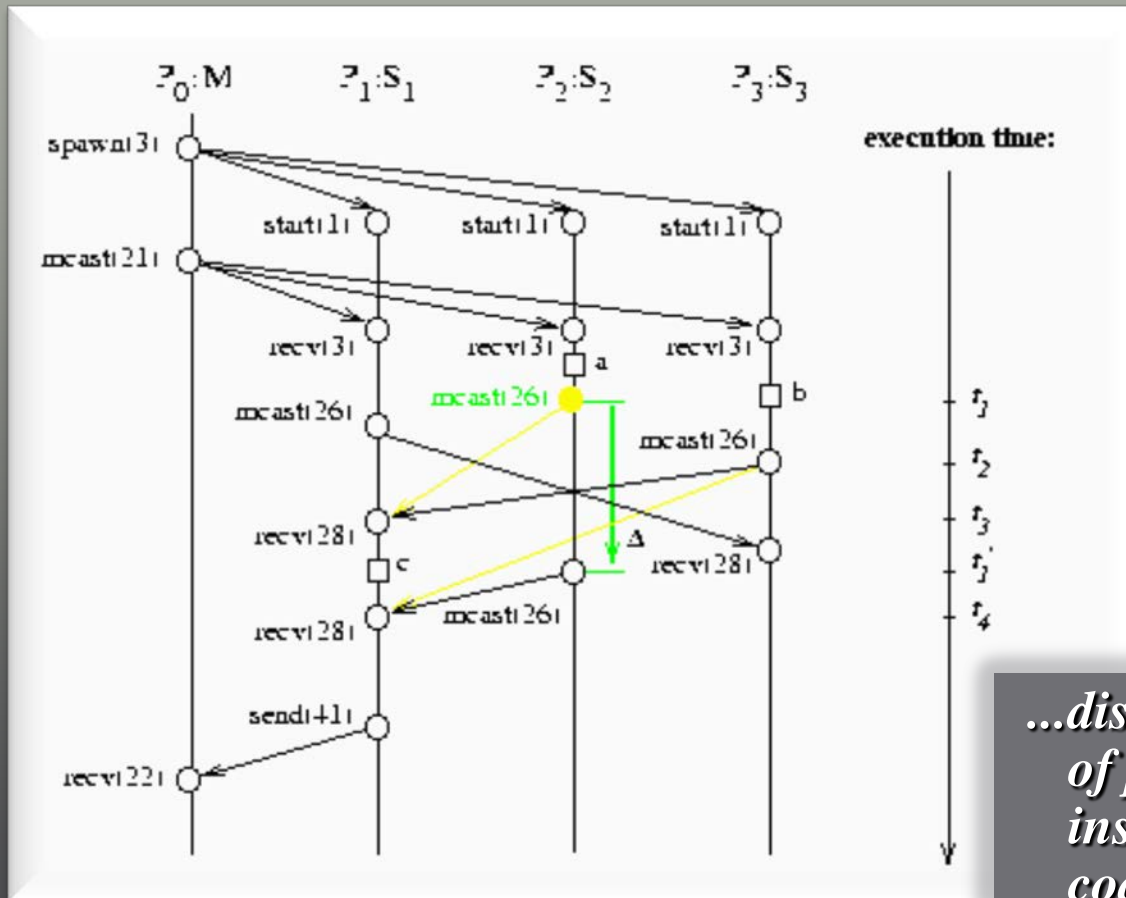
- Many-threads-Many-times (MtMt):
event monitoring



Instrumenting code and environment



Probe effect



Log structure

- **Heading:**
 - Unique identifier
 - Comment
 - Records (table of content)
- **Record:**
 - date, time, test case ID,
 - event, local state, context
- **Event:**
 - Statement executed, signal sent/received, exception raised, variable value changed
- **State:**
 - Object memory content
- **Context:**
 - history, condition, global state

What is worth logging?

- Potential error occurrences:
 - Arithmetic instructions (function calls, assignments),
 - Predicate (condition) evaluation,
 - Type conversion, actual vs formal parameters,
 - Return statements,
 - Dynamic variables,
 - Systems diagnostics, exception handlers,
 - Message packing/unpacking,
 - Message tagging,
 - Races,
 - Communications actions matching

Error localization

*(!) Knowing that the program has a bug
doesn't mean knowing what causes it*

- **Debugging:**
 - Post-mortem print-out, core dump,
 - Trace file (log)
 - Building a hypothesis,
 - Elimination of hypotheses
- **Tools:**
 - Print-out
 - Breakpoint trap
 - Instant replay

Is it possible to do without testing?

- Programmers make mistakes when, when creating a program, they are unable to remember all the details needed to make it correct
- There are no bug-free programs, they are only poorly tested
- Programs considered correct may still have errors
- We can mistake correct program behavior for a wrong one (and vice versa)
- Errors reveal throughout the entire life of a program