## Ex. 2. Probability distribution for discrete random variables

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$$
\begin{aligned}
& \text { For discrete random variable } X, F(x)=P(X \leq x) \text {. } \\
& \text { For discrete random variable } X, E X=\sum_{i} x_{i} p_{i}=m \text {. } \\
& \text { For discrete random variable } X, D^{2}(X)=\sum_{i}\left(x_{i}-m\right)^{2} p_{i} \vee D^{2}(X)=E\left(X^{2}\right)-(E X)^{2} \\
& \qquad \begin{array}{l}
P(X \leq x)=\lim _{k \rightarrow x^{+}} F(k)=F(x+) \\
\qquad P(X>x)=1-F(x+) \\
\qquad P(X<x)=F(x) \\
\quad P(X=x)=F(x+)-F(x) \\
P(a \leq X<b)=F(b)-F(a) \\
P(a<X \leq b)=F(b)-F(a)+P(X=b)-P(X=a) \\
P(a \leq X \leq b)=F(b)-F(a)+P(X=b) \\
P(a<X<b)=F(b)-F(a)-P(X=a)
\end{array} \\
& \hline
\end{aligned}
$$

Task 1. A die is tossed. Let $x$ be the number of spots observed on the upturned face of the die.
a) Find the probability distribution of $x$ and display it in the tabular and graphical form.
b) Find the cumulative disribution function and display it in the tabular and graphical form.
c) Find the expectation of $X$ and the variance of $X$.
d) Find $P(1 \leq X<4), P(X>3), P(1<X<3), P(X=4)$.

Task 2. Three fair coins are tossed. Let $x$ be the numer of heads.
a) Find the probability distribution of $x$ and display it in the tabular and graphical form.
b) Find the cumulative distribution function and display it in the tabular and graphical form.
c) Find the expectation of $X$ and the variance of $X$.
d) Find $P(1 \leq X<4), P(X>3), P(1<X<3)$.

Task 3. Probability distribution of accidents at work during one day is shown in the table.
a) What is the variable X ?
b) Find the cumulative disribution function and display it in the tabular and graphical form
c) Find the expectation of $X$ and the variance of $X$.
d) Find $P(2<X \leq 4), P(X<3), P(X \geq 1)$.

| $\mathbf{x}$ | 0 | 1 | 2 | 3 | 4 | 5 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{p}$ | 0.02 | 0.18 | 0.28 | 0.25 | 0.2 | 0.07 |

